

*Lecture B1*

# RADIATION and PARTICLES

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**October 15, 2013**

# *OVERVIEW LECTURE 1*

***REMARKS ON RADIATION AND PARTICLES***

***HOW TO DETECT ?***

***HOW TO MEASURE ?***

***UNITS, CONSTANTS, RELATIONS, KINEMATICS***

# PARTICLES

particle



detector



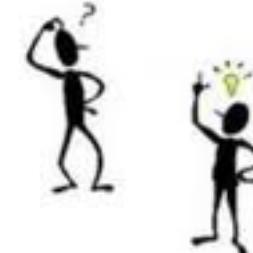
registration



Light



Heavy



# PARTICLES

*What characterizes a particle?*

*mass*

$M$

*charge*

$Q$

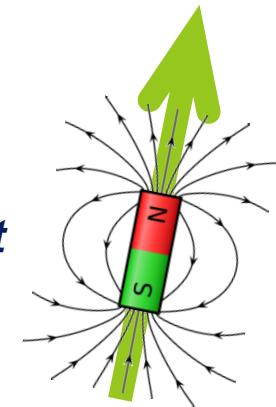
*Spin      intrinsic angular momentum*

$S$      $\Leftrightarrow$  *magnetic moment*

*life time*

$\tau_0$

*shape      for non elementary particles*       $\langle r^2 \rangle$



# RADIATION

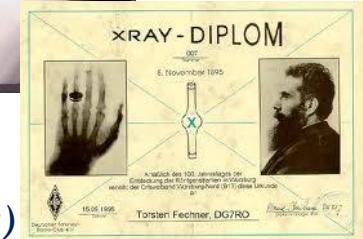
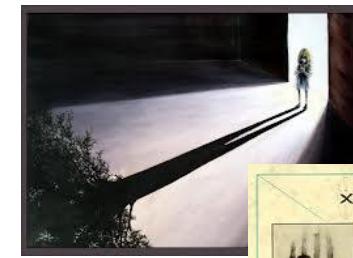
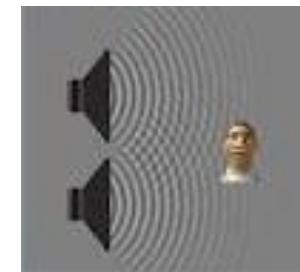
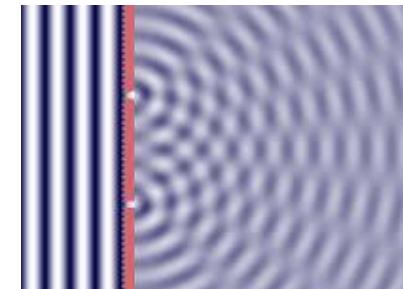
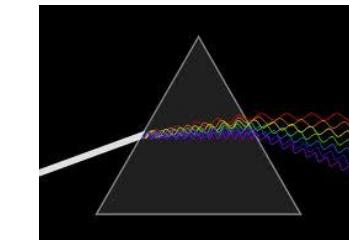
fluid



gas



„light“



*fundamental constant:  $c = \text{speed of light in vacuum} (\cong 30 \text{ cm} / \text{ns})$*

# RADIATION

**What characterizes waves?**

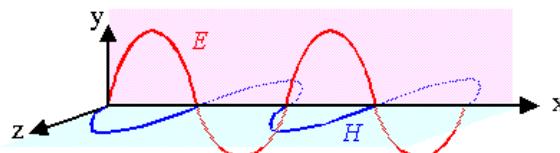
**ability to interfere**

**wave length**

$\lambda$

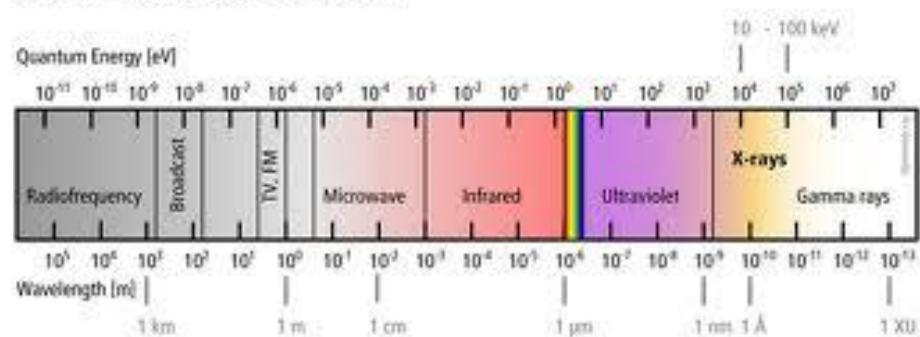
**frequency**

$\nu$



**one more degree of freedom: spin 1       $m = \pm 1, \text{ no } m = 0$**

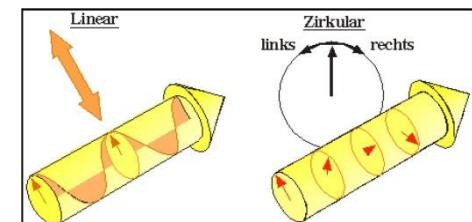
The Electromagnetic Spectrum



**wave propagation velocity in vacuum**       $c = \lambda \nu$

**“ “ “ in medium**       $c' = \lambda' \nu < c$

**index of refraction**       $n = c/c'$

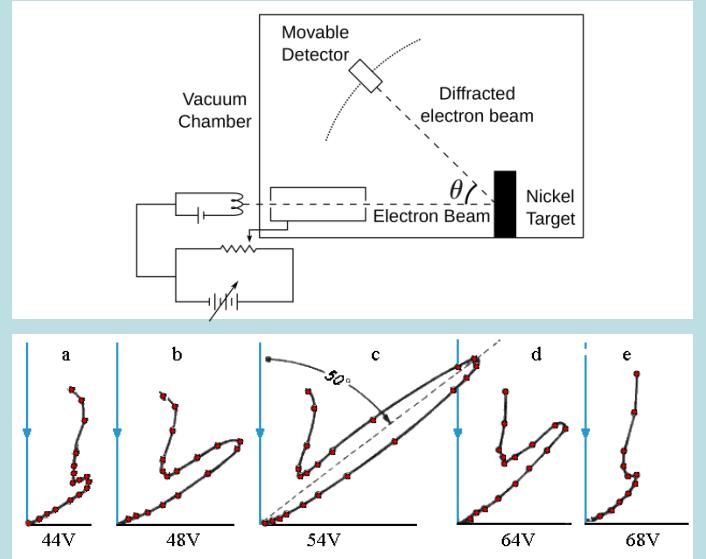


# MATTER or WAVES?

**particles, e.g. electrons, are diffracted**

54 eV electrons on a Ni crystal

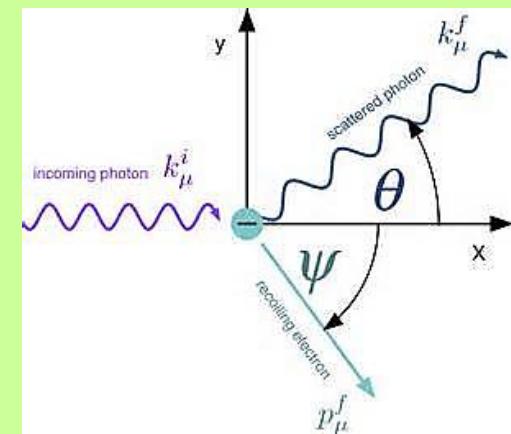
Davisson-Germer (1927)



**light – photons – play billiard**

X-rays on carbon

Compton (1922)



# ANSWER: BOTH! I

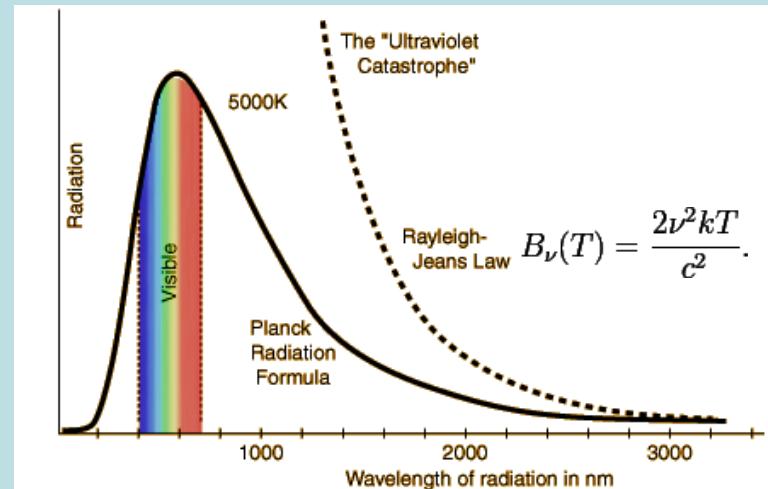
**Planck radiation law** 1900

$$B_\nu(T) = \frac{2h}{c^3} \cdot \frac{\nu^3}{e^{\frac{h\nu}{kT}} - 1}$$

energy density of blackbody radiation

**h: Planck constant**

quantized quantity is action  $S = \int E(t)dt$  [J·s]

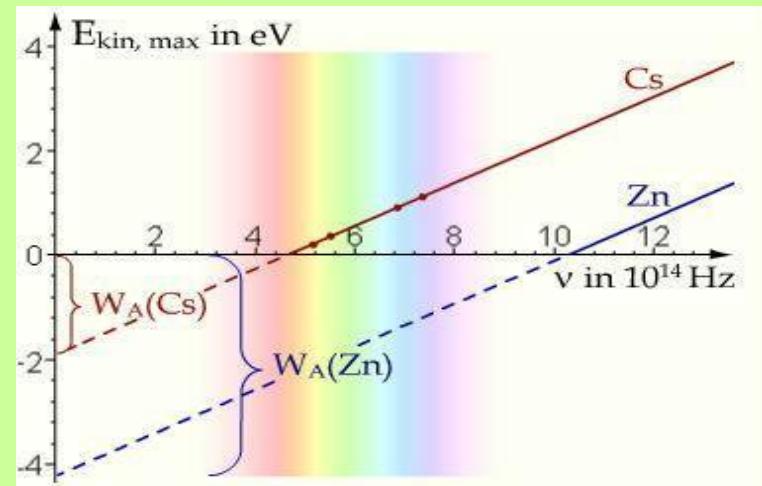


**Einstein equation for photo effect** 1905

$$h\nu = W_A + E_{kin, electron}$$

$$E_{photon} = h\nu \quad \text{„light particle“}$$

$$h = E \cdot T \quad \text{minimal action}$$



# ANSWER: BOTH! //

**particles are waves** de Broglie 1922

**special relativity**

$$E = \gamma \cdot m_0 \beta c^2$$

$$p = \gamma \cdot m_0 \beta c$$

$$\lambda = \frac{h}{p}$$

**photo effect**

$$E = h\nu = hc/\lambda$$

**uncertainty relation** Heisenberg 1927

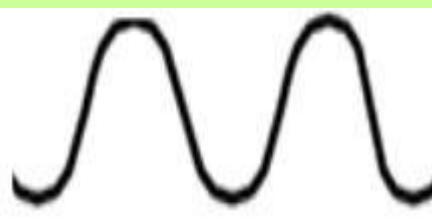
measuring time  $\rightarrow 0$   
energy information  $\rightarrow \infty$

$$\Delta E \cdot \Delta t \approx \hbar/2$$

$$\Delta x \cdot \Delta p \approx \hbar$$

$$\Delta J \cdot \Delta \varphi \approx \hbar$$

$$T = 1/\nu$$

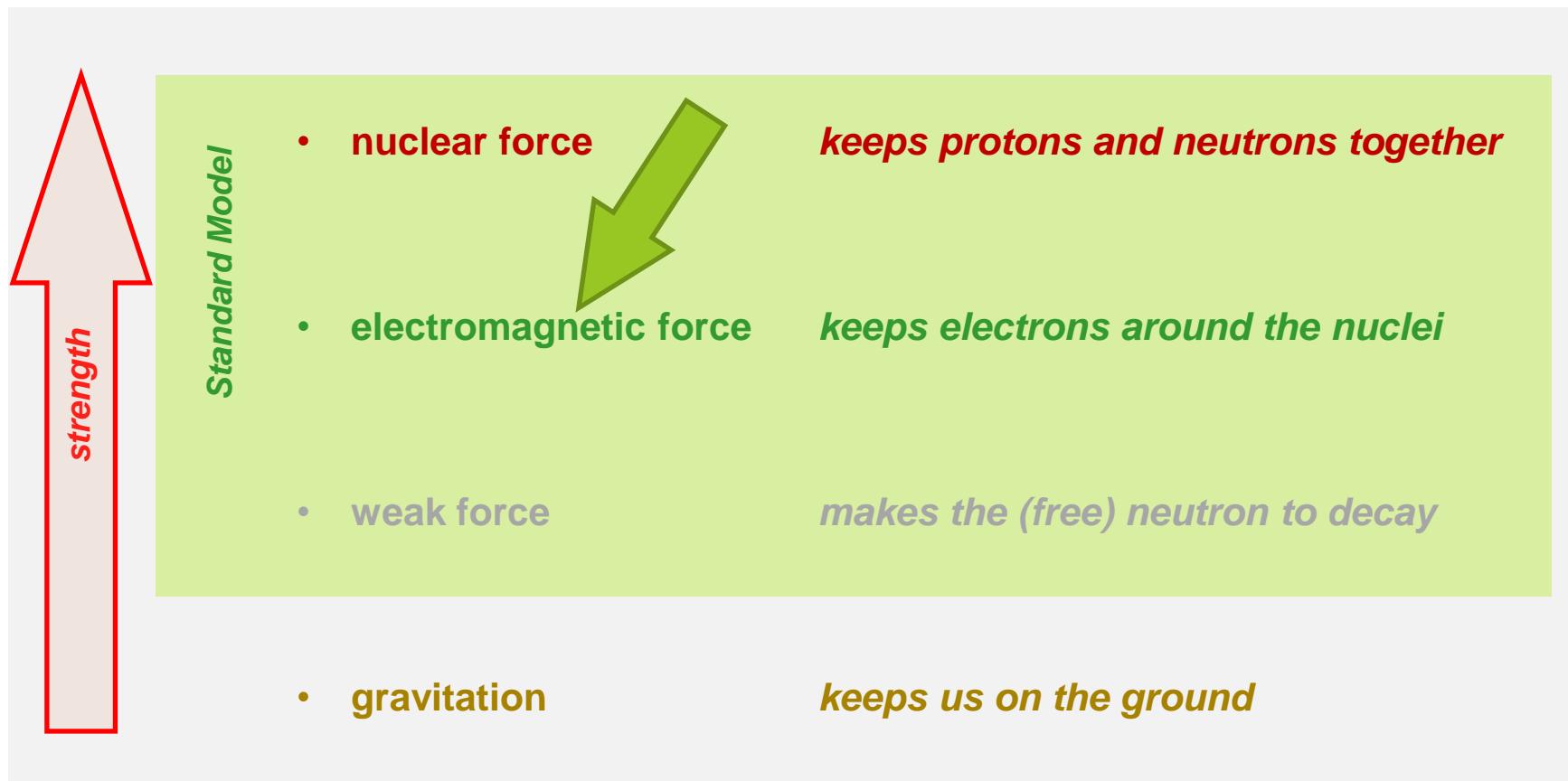


$$\lambda \cdot \nu = c$$

$$\Delta t \cdot \Delta E \approx \frac{\hbar}{2}$$

## HOW TO DETECT ?

*known forces – which one can be used ?*



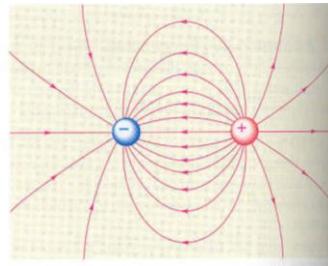
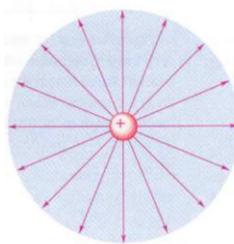
# ELECTROMAGNETIC FORCE

*a force is mediated*

**classical picture**

*by field around a source*

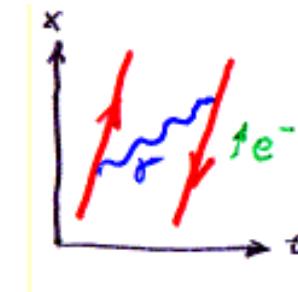
$$\mathbf{F}_{\text{Coulomb}} = \frac{1}{4\pi\epsilon_0} \cdot \frac{\mathbf{Q}_1\mathbf{Q}_2}{r^2}$$



**quantum world**

*field quanta = particles*

*,“light“ particles = photons  $\gamma$*



***electromagnetic radiation = E and B fields interact with electric charges***

# INTERACTION WITH ELECTRIC CHARGE

- electric field

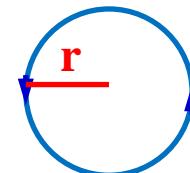
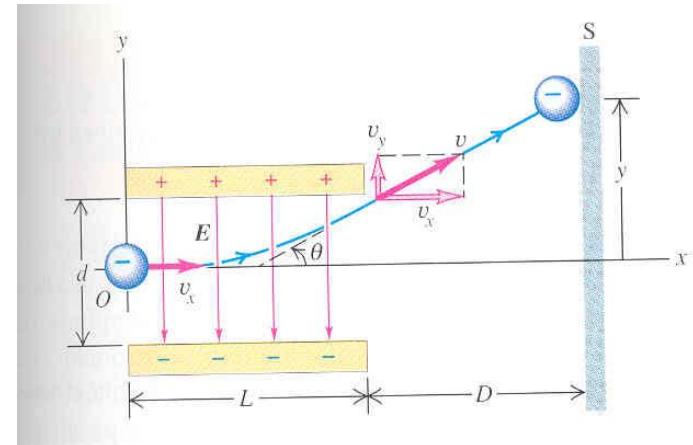
$$\vec{F} = m\ddot{\vec{x}} = Q \cdot \vec{E}$$

$$\Rightarrow \frac{Q}{M}$$

- magnetic field

$$\vec{F} = m\ddot{\vec{x}} = Q \cdot (\vec{v} \times \vec{B})$$

$$\Rightarrow p$$



$B = \text{const.}$   
 $\Rightarrow$  *circular motion*  
 $B \perp$  *plane of projection*

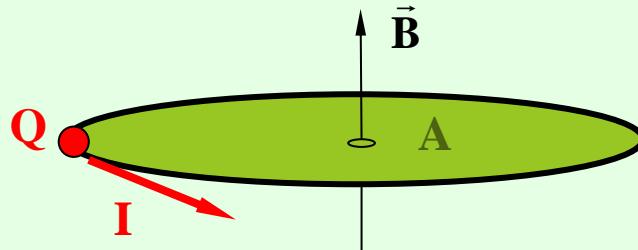
$$\omega = \frac{Q}{M} B \quad \omega = \frac{2\pi}{T}$$

$$mv^2/r = Q \cdot v \cdot B$$

$$p = Q \cdot B \cdot r$$

# INTERACTION WITH MAGNETIC MOMENT

„magneto-mechanical“ view of magnetic moment



magnetic dipole is produced by

$$\text{circular current} \quad I = \frac{Q \cdot \omega}{2\pi}$$

$$\text{magnetic moment} \quad \vec{\mu} \equiv I \cdot A = \frac{Q}{m} \cdot \vec{L}$$

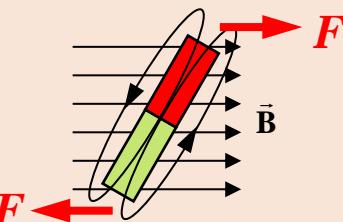
subatomic particles: possible without any mechanical analogon (extension)

$$\text{Bohr magneton} \quad \mu_B = \frac{e\hbar}{2m_e} \quad \mu_e = -g_e \cdot \mu_B \cdot \frac{S}{\hbar} \quad g_e = 2 + 2 \cdot 10^{-6} \quad \text{elementary particle}$$

$$\text{nuclear magneton} \quad \mu_N = \frac{e\hbar}{2m_p} \quad \mu_p = g_p \cdot \mu_B \cdot \frac{S}{\hbar} \quad g_p = 5.6 \quad \text{not an elementary particle}$$

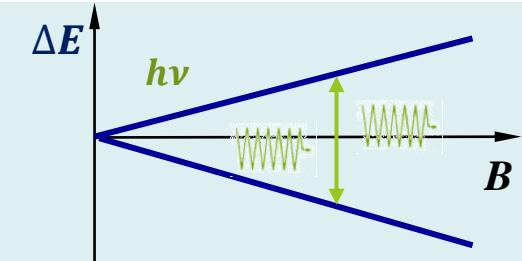
$$\text{torque} \quad \vec{M} = \vec{\mu} \times \vec{B}$$

change in units of  $g \mu_B / g \mu_N$



interaction energy

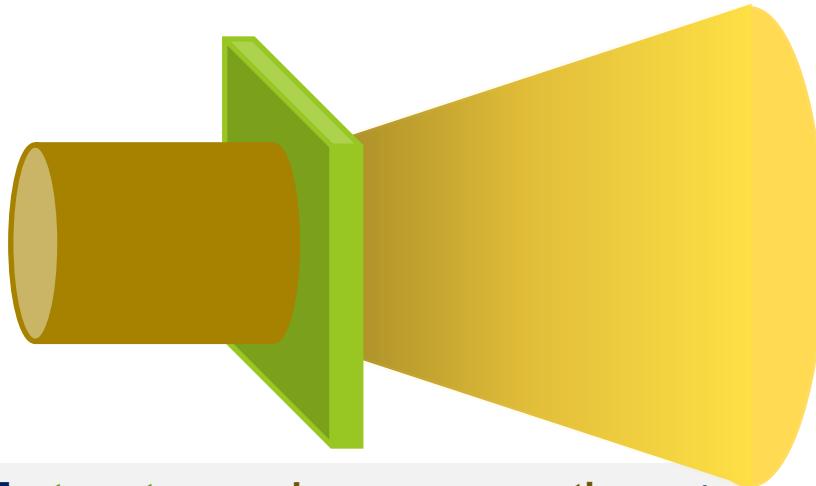
$$\Delta E = \vec{\mu} \cdot \vec{B}$$



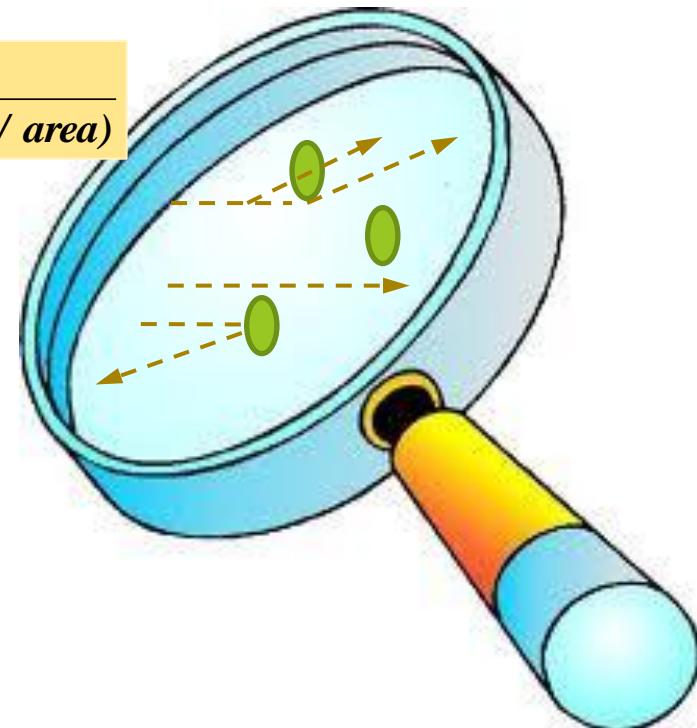
# HOW TO MEASURE: CROSS SECTION I

*measures the probability of a reaction*

$$\sigma = \frac{\text{reactions / time interval}}{(\text{incoming particles / time interval}) \times (\text{target particles / area})}$$



**F** = target area  $\cap$  beam cross section [cm<sup>2</sup>]



**particle**       $\sigma = \frac{N}{N_0} \cdot \frac{1}{n/F}$

*N<sub>0</sub> incoming particles in beam*

**wave**       $\sigma = \frac{I}{I_0} \cdot \frac{1}{n/F}$

*intensity I<sub>0</sub> of incoming radiation*

**$\rho$**  = target density [g / cm<sup>3</sup>]  
**n<sup>□</sup>** =  $n / F \times d$   
=  $\rho \cdot (N_A / A)$  [particles / cm<sup>3</sup>]  
**N<sub>A</sub>** = Avogadro constant  
**A** = mass number [g]

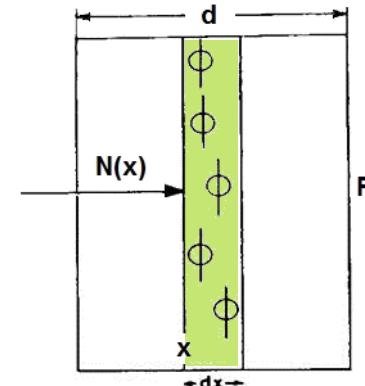
## CROSS SECTION II

*reaction rate*

„thin“ target *differential notation* ( $N \rightarrow dN$ )

$$- dN(x) = N(x) \cdot \left( \rho \cdot \frac{N_A}{A} \right) \cdot \sigma \cdot dx$$

↑                      ↑  
setup    „physics“



„thick“ target *integration over target thickness d*

$$N(d) = N(0) \cdot e^{-\rho \frac{N_A}{A} \sigma \cdot d} = \text{number of } \underline{\text{not interacting}} \text{ particles (transmission)}$$

$$R(d) = N(0) \cdot (1 - e^{-\rho \frac{N_A}{A} \sigma \cdot d}) = \text{number of } \underline{\text{interacting}} \text{ particles (reaction/absorption)}$$

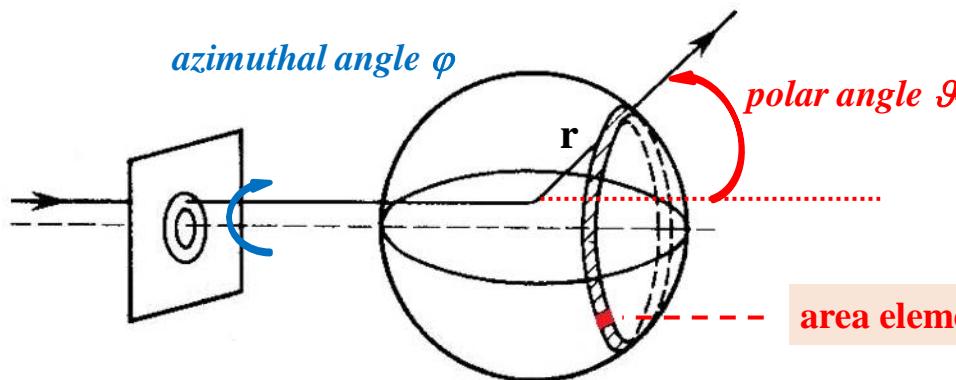
linear extinction coefficient  $\mu \equiv (\rho \cdot \frac{N_A}{A}) \cdot \sigma$   $\rho$ : status of target A

mass absorption coefficient  $\lambda^{-1} \equiv \frac{\mu}{\rho} = \frac{N_A}{A} \cdot \sigma$  independent of state of aggregation of target A

mixture/compound total cross section  $\sigma_{\text{total}}(E) = \sum \sigma_{\text{partial}}(E)$  [1 barn =  $10^{-24}$  cm $^2$ ]

## CROSS SECTION III

*differential cross section includes angular information of scattering*



**solid angle element**

$$\Delta\Omega \equiv \Delta A / r^2 \text{ [steradian (sr)]}$$

area element  $\Delta A = r \Delta\theta \cdot r \sin\theta \Delta\phi$

**azimuthal symmetry**

$$\Delta\Omega = 2\pi \sin\theta \Delta\theta \quad \text{φ integration}$$

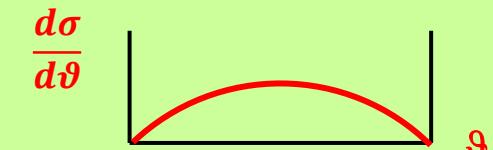
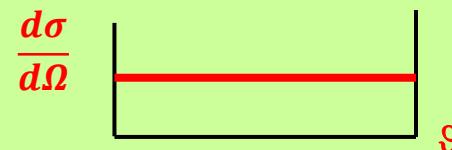
**full sphere**

$$\Omega = 4\pi r^2 / r^2 = 4\pi \quad (\text{,,}4\pi\text{“ detector})$$

**fraction of full solid angle**  $\Delta\Omega / 4\pi$

$$\frac{d\sigma}{d\Omega} = \frac{1}{2\pi \cdot \sin\theta} \cdot \frac{d\sigma}{d\theta}$$

$$\frac{d\sigma}{d\theta} = \text{const.} \quad \text{isotropy in } \theta$$



# UNITS

	<b>atoms</b>	<b>nuclei or particles</b>
length	$1 \text{ nm} = 10^{-9} \text{ m}$ $\approx 0.5 \cdot 10^{-10} \text{ m} = 0.05 \text{ nm}$	$1 \text{ fm} = 10^{-15} \text{ m} (= 1 \text{ Fm})$ $\approx 0.8 \cdot 10^{-15} \text{ m} = 0.8 \text{ fm}$
energy	eV  - binding energy - visible light - X-rays	MeV  $13.6 \text{ eV} \cdot Z^2 / n^2$ 1 – 2 eV up to $\approx 100 \text{ keV}$
momentum	eV/c	MeV/c
time	$1 \text{ fs} = 10^{-15} \text{ s}$ $2p \text{ hole in K atom} \approx 6 \text{ fs}$	$1 \text{ ys} = 10^{-24} \text{ s}$ $\Delta \text{ baryon } 6 \cdot 10^{-24} \text{ s}$
mass	a.m.u. $\equiv m(^{12}\text{C})/12$  rest mass $m_0$	MeV/c <sup>2</sup>  $931.5 \text{ MeV}/c^2 = 1.66 \cdot 10^{-27} \text{ kg}$ $938.3 \text{ MeV}/c^2 \approx 1 \text{ a.m.u.}$ $939.6 \text{ MeV}/c^2 \approx 1 \text{ a.m.u.}$ $0.511 \text{ MeV}/c^2 = 9 \cdot 10^{-31} \text{ kg} \approx 1/1823 \text{ a.m.u.}$
angular momentum (Spin)	$j = 0, 1/2, 1, 3/2, \dots \hbar$	$[j] = [E \cdot t]$
magnetic moment	$\mu_B = 5.8 \cdot 10^{-11} \text{ MeV} \cdot T^{-1}$	$\mu_N = 3.2 \cdot 10^{-14} \text{ MeV} \cdot T^{-1}$
cross section	$\sigma$	$10^{-24} \text{ cm}^2 = 1 \text{ barn (b)}$ $1 \text{ a. u.} = r_B^2$

# CONSTANTS

speed of light *definition!*       $c \equiv 299\,792\,458 \text{ m/s}$        $\approx 0.3 \text{ cm/ns}$

elementary charge ( $\pm$ )       $e = 1.6 \cdot 10^{-19} \text{ C}$

Avogadro constant       $N_A = 6.02 \cdot 10^{23} / \text{mol}$

Planck constant       $h = 6.6 \cdot 10^{-34} \text{ J}\cdot\text{s}$

$\hbar = h/2\pi$       analogue  $\lambda, \dots$

$\hbar = 6.582 \cdot 10^{-22} \text{ MeV}\cdot\text{s}$

fine-structure constant       $\alpha = e^2/4\pi\epsilon_0\hbar c$        $= 1/137$

classical electron radius       $r_e = e^2/4\pi\epsilon_0 m_e c^2 = \alpha \hbar c m_e c^2$        $= 2.82 \text{ fm}$

conversion constant       $\hbar c = 197 \text{ MeV}\cdot\text{fm}$  ( $\hbar=h/2\pi$ ), analogue  $\lambda, \dots$

conversion constant       $hc = 12.4 \text{ keV}\cdot 10^{-10} \text{ m}$

# RELATIONS

wave propagation

$$c = \lambda v$$

Photon energy

$$E = h\nu = \hbar \omega$$

uncertainty relation

$$\Delta p \cdot \Delta x \geq \hbar$$

$$\Delta E \cdot \Delta t \geq \hbar$$

life time  $t \Leftrightarrow \Delta E \equiv \Gamma$

$$\Gamma \cdot \tau = \hbar/2$$

$$\text{MeV} \cdot \text{s}$$

Bohr formula

$$E_B = -mc^2 \cdot \frac{(Z\alpha)^2}{2n^2}$$

$$Ryd = m_e c^2 \cdot \frac{\alpha^2}{2} = 13.6 \text{ eV}$$

Bohr radius

$$r_B = \frac{\hbar c}{\alpha m_e c^2} mc^2 = r_e \alpha^{-2}$$

$$= 0.53 \cdot 10^{-10} \text{ m}$$

Virial theorem

$$2 \cdot \langle T_{kin} \rangle = n \cdot \langle V_{tot} \rangle$$

$\langle \dots \rangle$  average of ...

count rate

$$N = N_{in} \cdot \rho d \frac{N_A}{A} \cdot \sigma$$

# RELATIVISTIC KINEMATICS

## *massive particles*

total energy

$$E_{\text{total}} = \sqrt{p^2 c^2 + m_0^2 c^4}$$

$$= \gamma m_0 c^2$$

kinetic energy

$$E_{\text{kin}} = E_{\text{total}} - m_0 c^2$$

momentum

$$p = \gamma m_0 c \cdot \beta$$

rest mass

$$m_0 \neq 0 \quad \textit{range in matter}$$

charge

$$Q \neq 0 \quad \textit{deflection in el.-mag fields}$$

life time

$$\tau = \gamma \tau_0 \quad \textit{decay length } l = v \tau$$

## *el.-mag. radiation*

$$E_{\text{total}} = pc$$

$$= h\nu$$

$$= E_{\text{kin}}$$

*h Planck constant  
= minimal action*

$$p = \frac{E}{c}$$

$= 0$       *attenuation in matter*

$= 0$       *no deflection*

$= \infty$

**relativistic factor**

$$\gamma = \frac{1}{\sqrt{1-\beta^2}}, \quad \beta = \frac{v}{c} \quad \lim_{v \rightarrow c} \gamma \xrightarrow{v \rightarrow c} \infty$$