



An Introduction to the Basics of PET Imaging

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Outline

Introduction

- *PET Basics*
- *Example Measurement*

Overview Processing Workflow

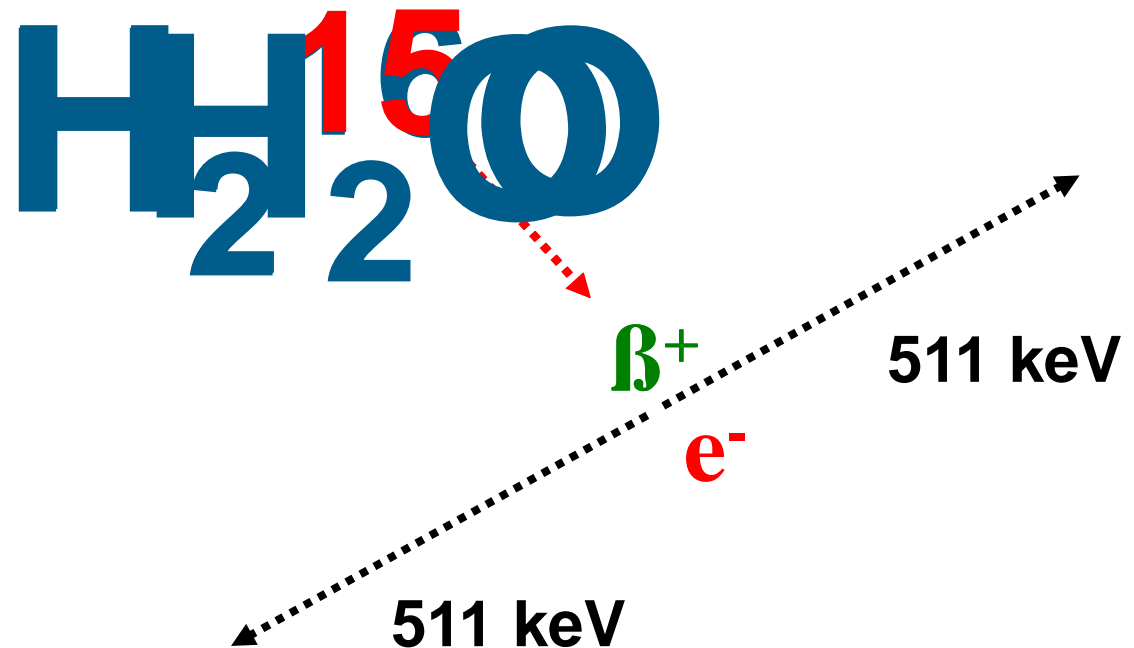
Required Data Corrections in Detail

- *Attenuation*
- *Randoms*
- *Normalisation*
- *Compton Scattering*
- *Decay & Deadtime Correction*
- *Calibration*

Example of Functional Imaging Using PET

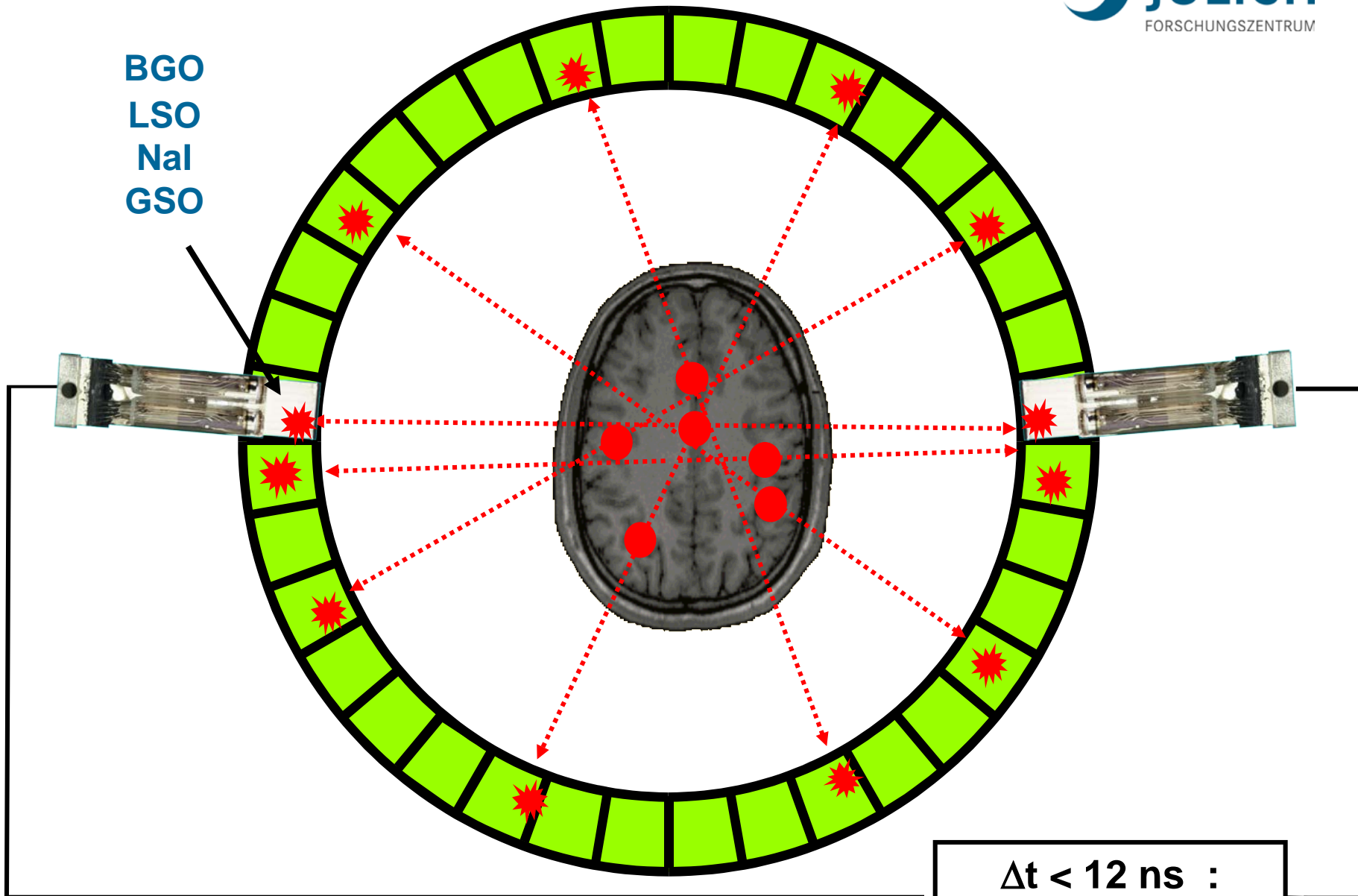
- **Mental activity needs energy.**
- **Substrates providing energy (glucose and oxygen) must be transported to the brain.**
- **This transport can be observed with PET.**

Using “radiating” water
Water is distributed within the body
blood flow becomes visible
corresponding to blood flow



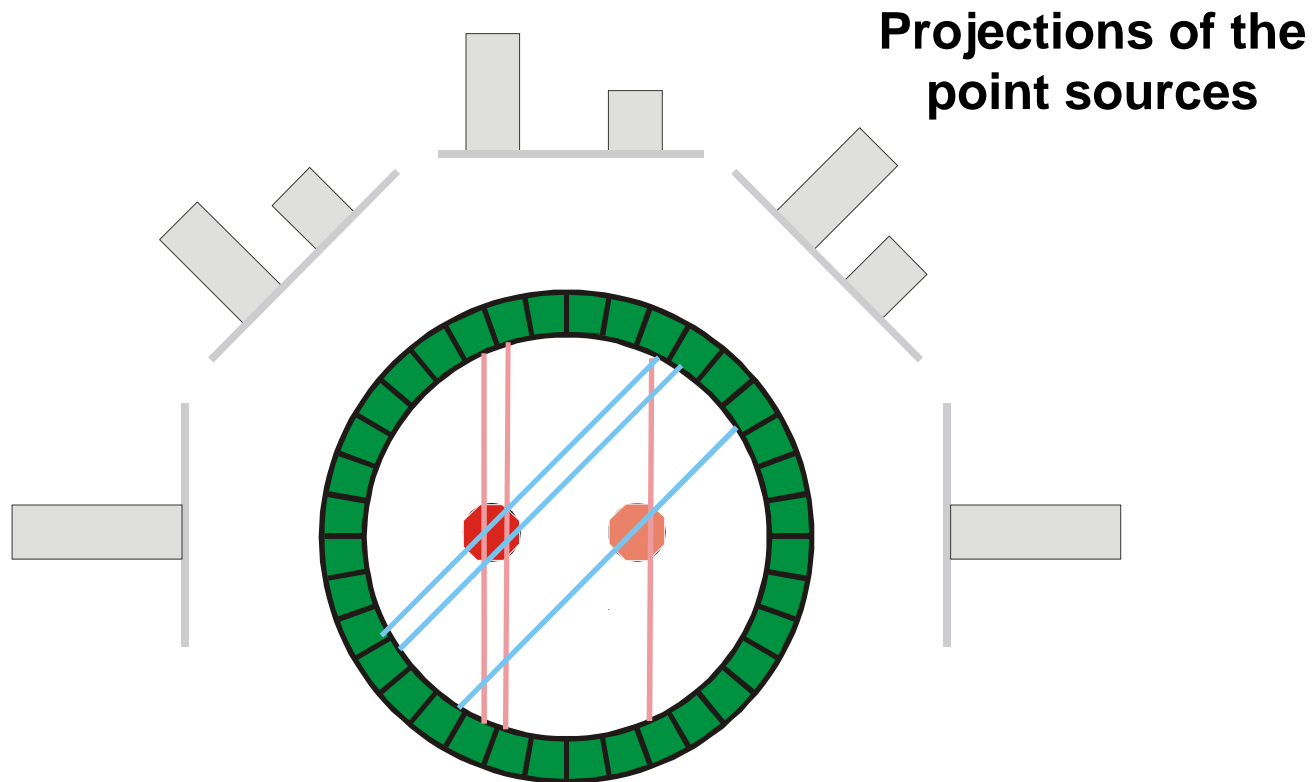


BGO
LSO
NaI
GSO



$\Delta t < 12 \text{ ns}$:
coincidence o.k.

The ring detector records pairs of annihilation photons by looking into the object from different views



**Two point sources
emitting pairs of annihilation photons**

Projections seen from around the head - activity used: ^{18}F -fluoro-deoxy-glucose

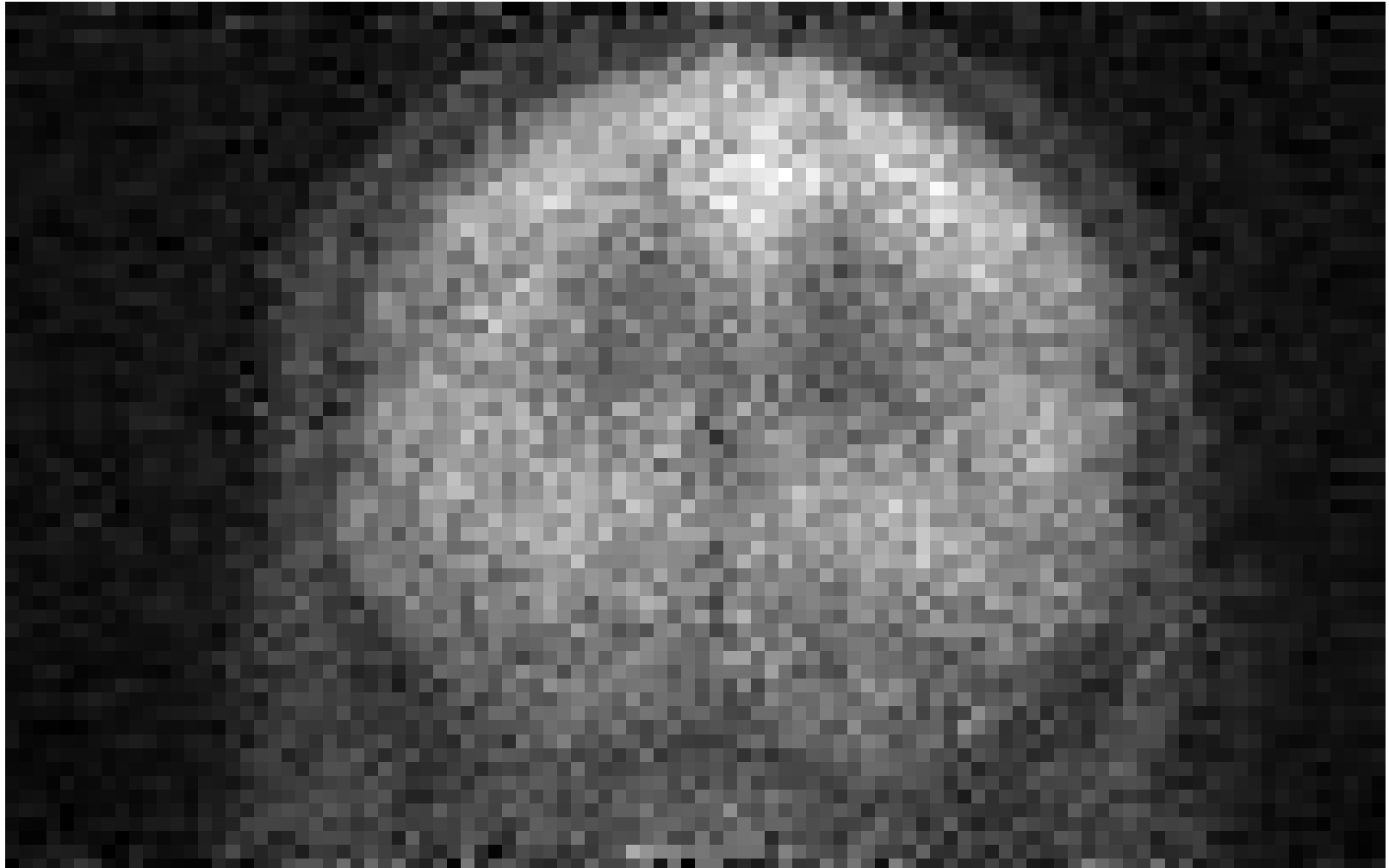


Image Reconstruction: Backprojection of the measured projection data and superposition

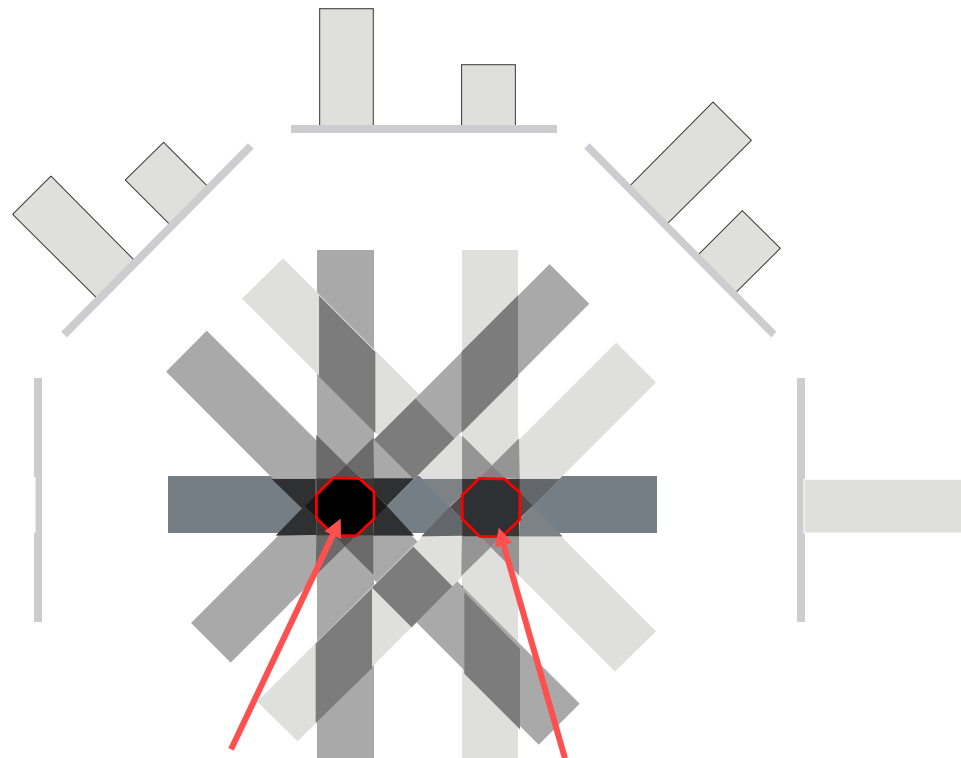
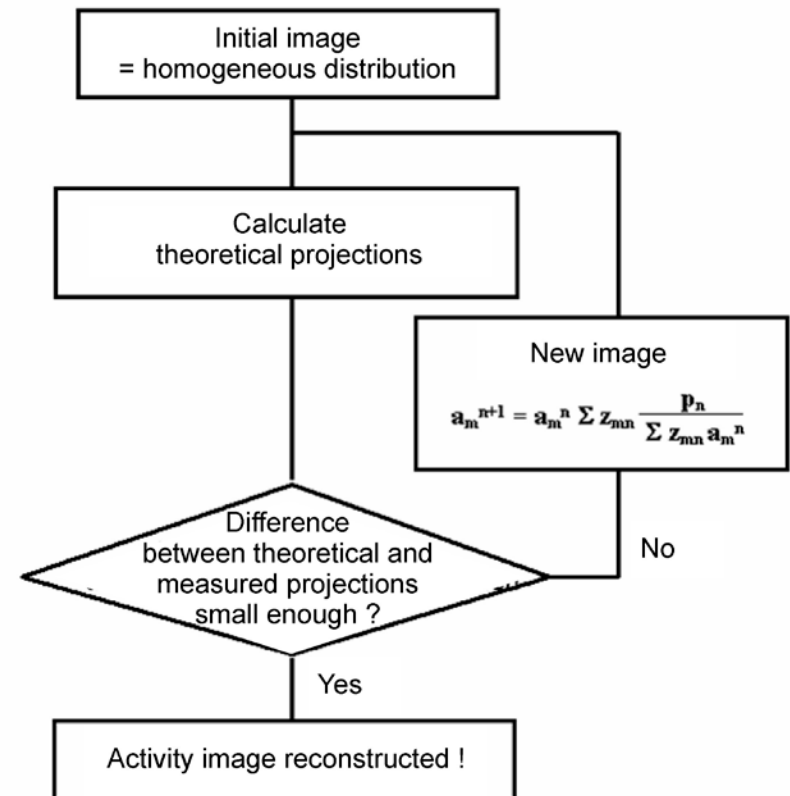
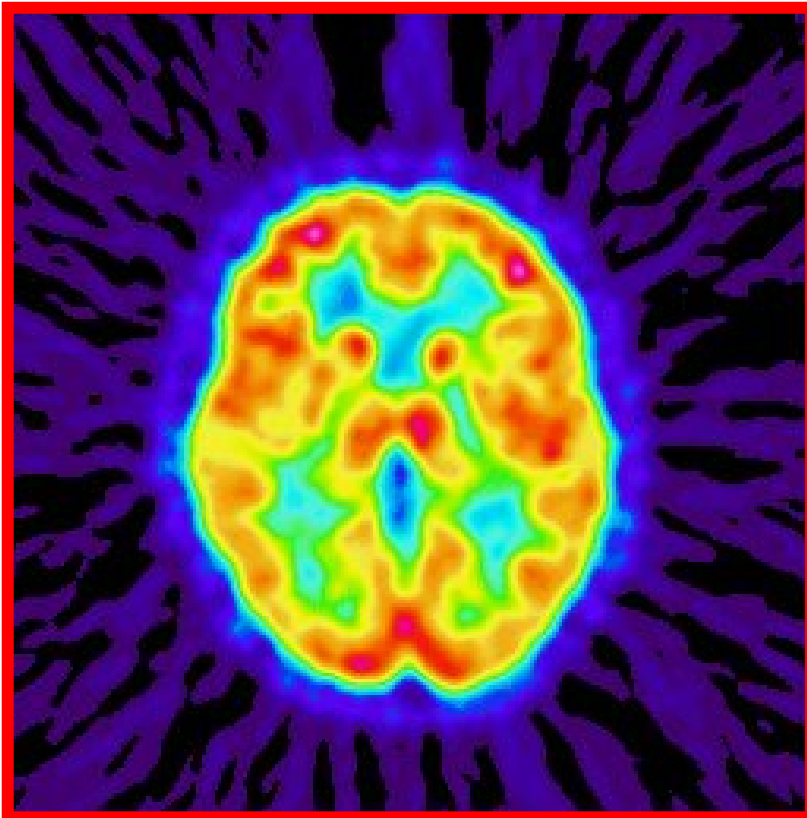


Image of point sources

Analytic Reconstruction by Filtered Backprojection

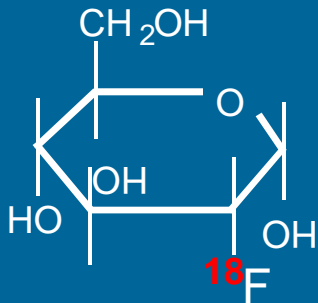
Algebraic Reconstruction by Iterative Solving of Matrix System



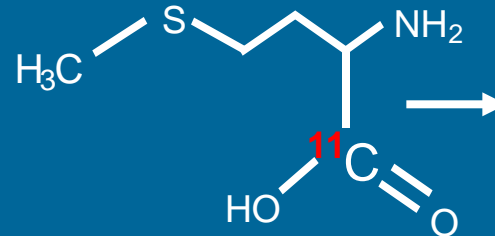
Metabolic Functions Visualised by “Natural” Tracer Molecules Labelled with Positron Emitters

$\text{H}_2^{15}\text{O} \rightarrow$ Perfusion

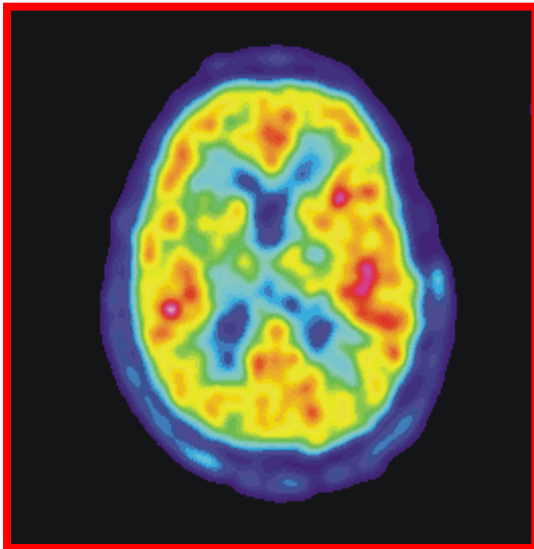
$^{15}\text{O}_2 \rightarrow$ Oxygen Consumption



Glucose Consumption

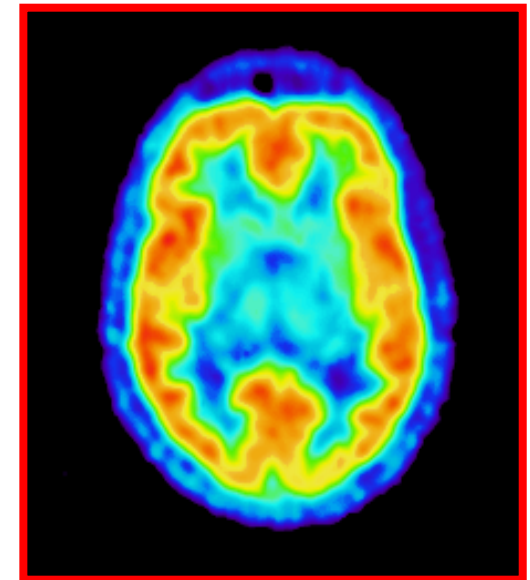
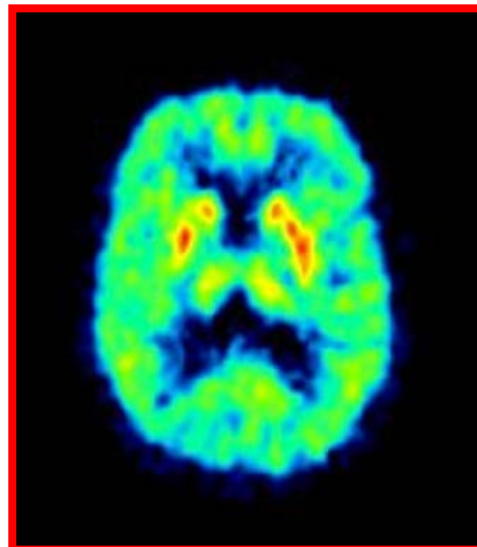


Transport
of Amino Acids



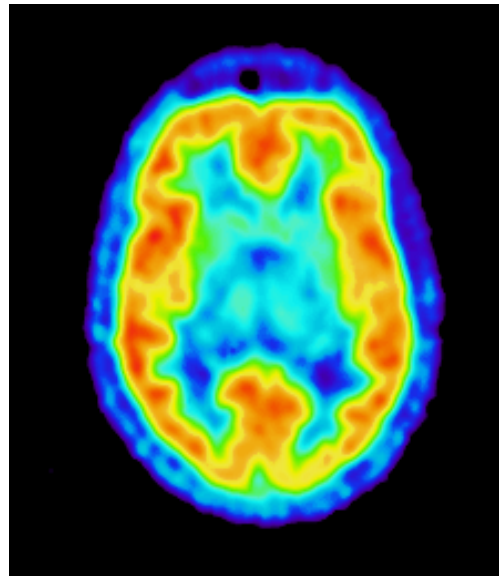
H_2^{15}O
Cerebral blood flow

^{11}C -SDZ GLC756:
dopamine
receptors



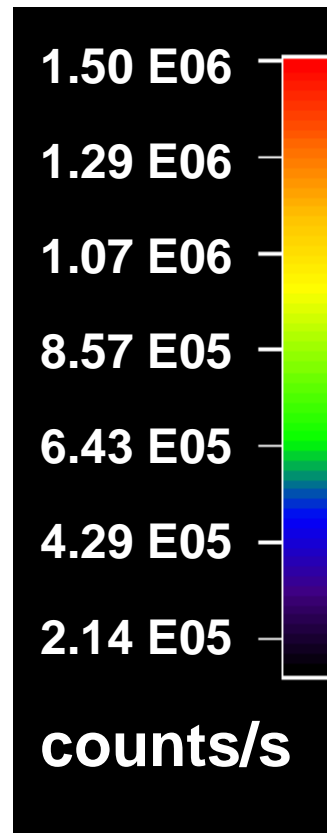
^{18}F -Altanserin:
serotonin
receptors

Visualisation of Radioactivity

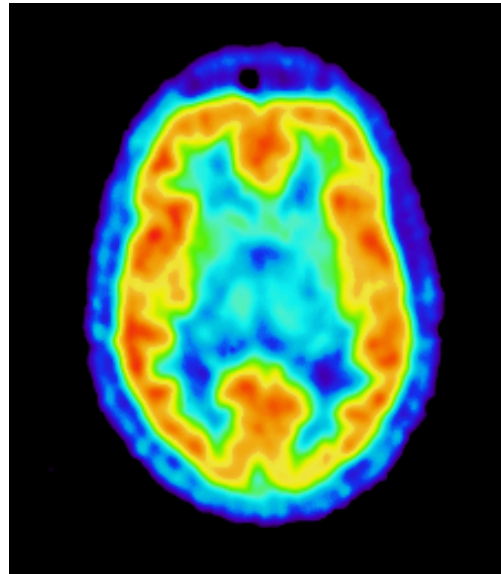


^{18}F -Altanserin

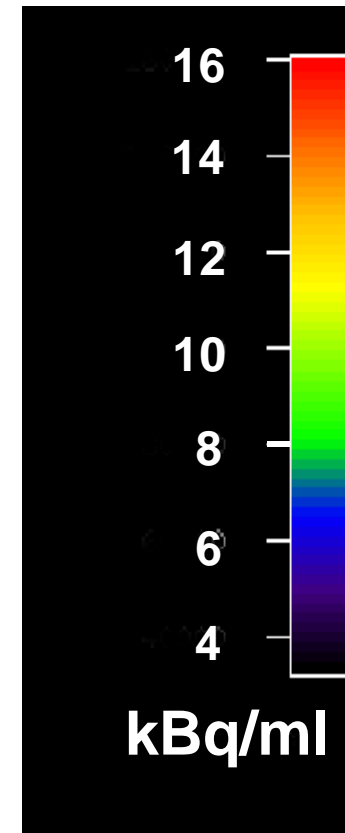
⇒ **serotonin receptors**



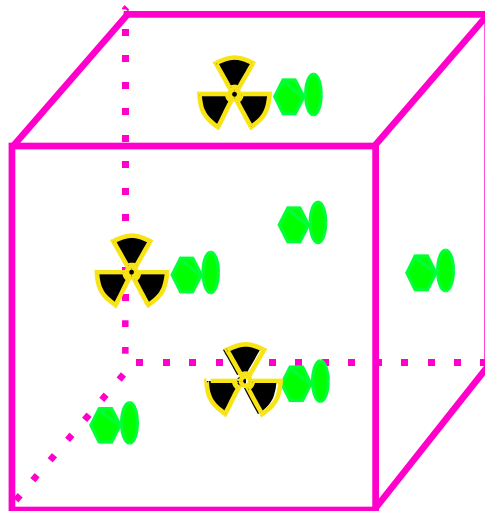
Quantification of Radioactivity Concentration



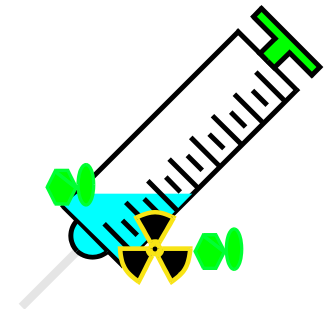
Measurement of ^{18}F -antiserin uptake



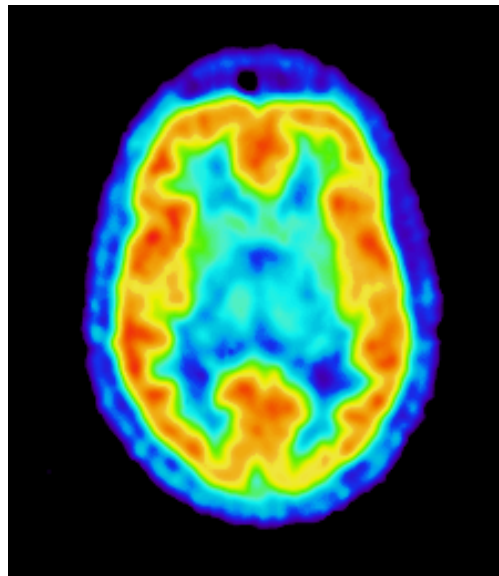
From Radioactivity Concentration (kBq/ml) to Mass Concentration ($\mu\text{mol/ml}$)



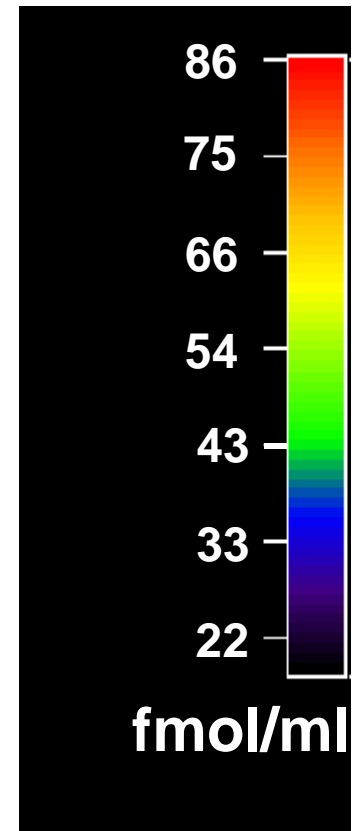
$$\frac{m_{\text{Tissue}}}{C_{\text{PET}}} = \frac{m_{\text{Syringe}}}{C_{\text{Syringe}}}$$



Quantification of Mass Concentration

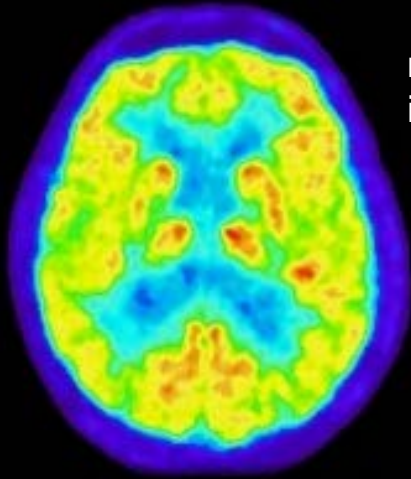


Measurement of altanserin concentration

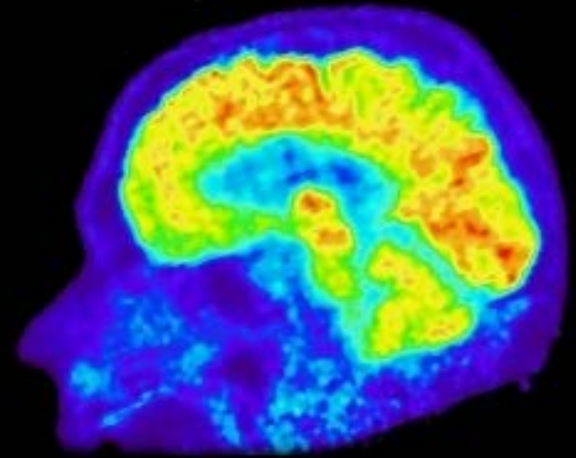
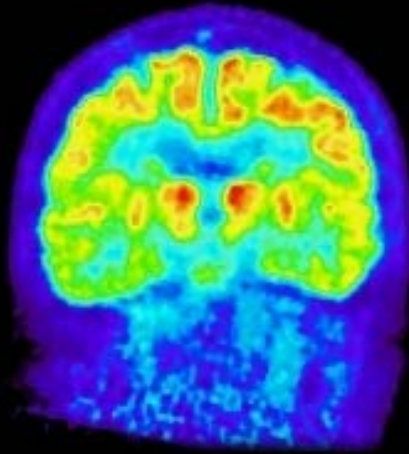


Simultaneous PET-MR patient measurements

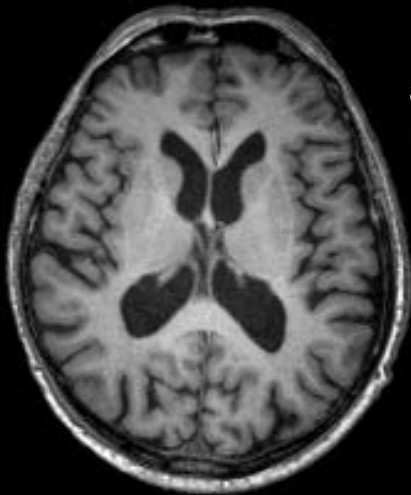
¹⁸Flour-Deoxy-Glucose-PET



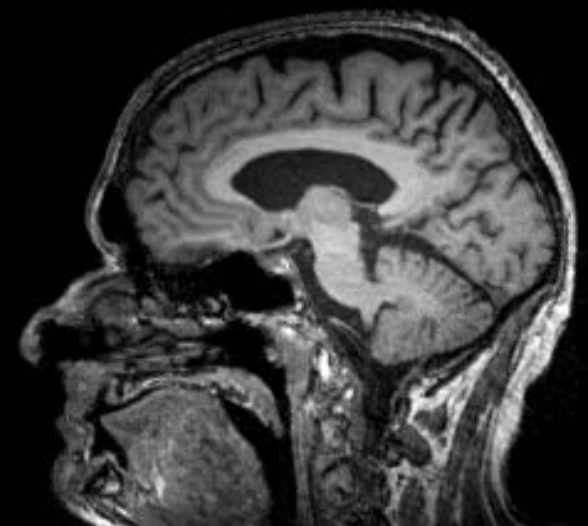
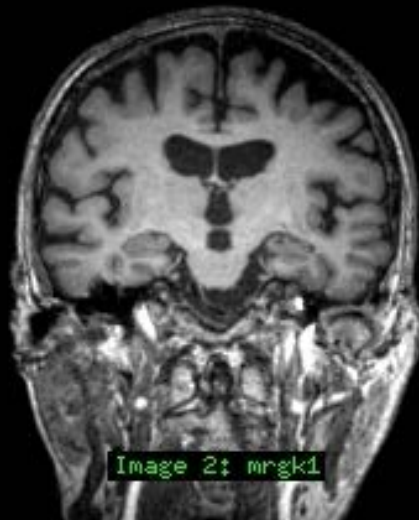
metabolic
information



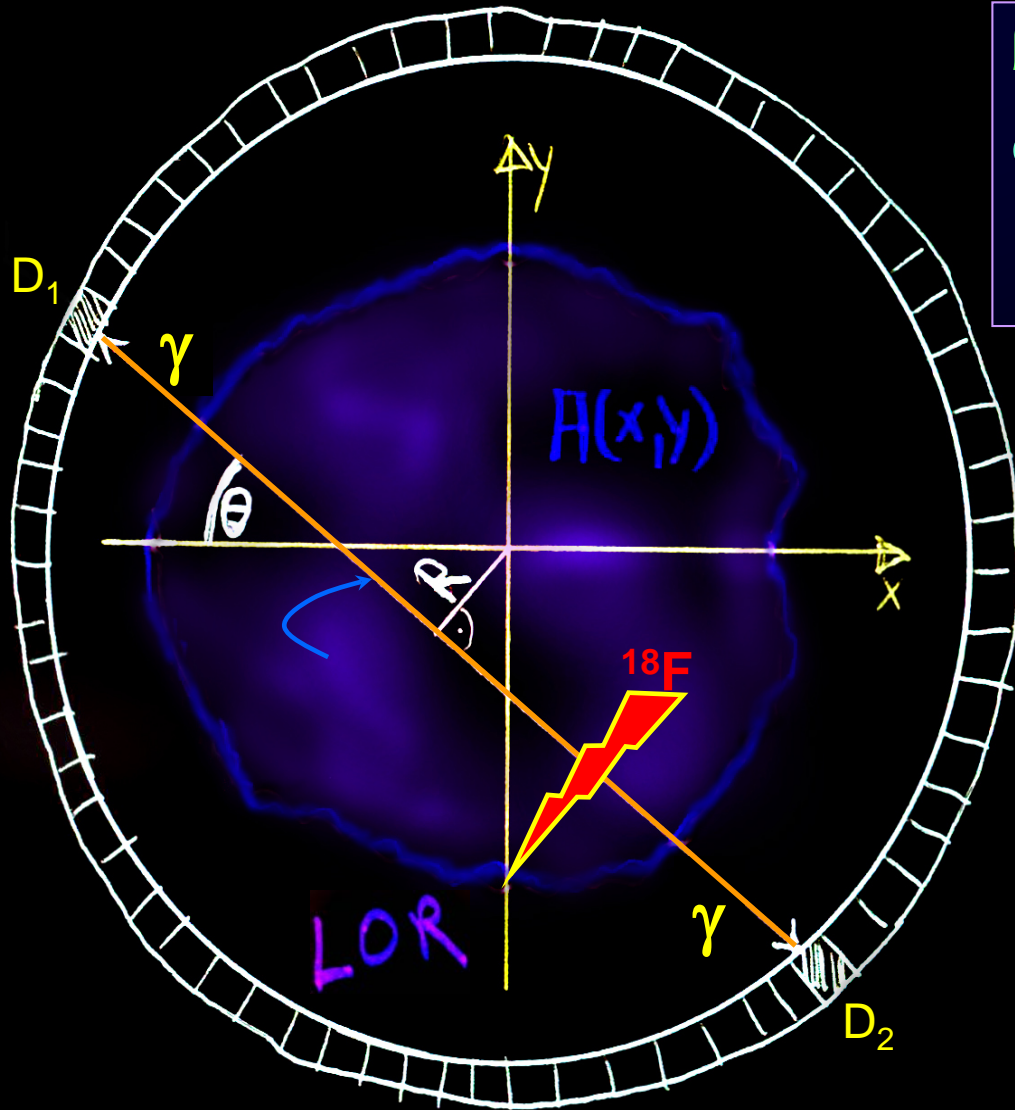
simultaneous MR (T1 MPRAGE)



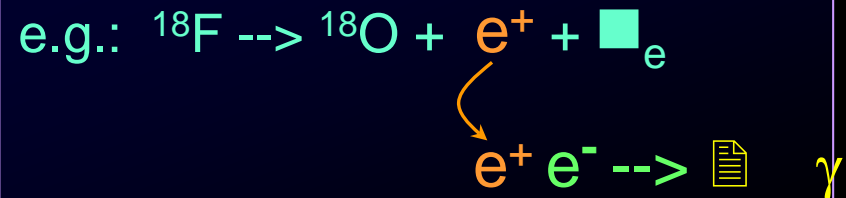
anatomical
information



First Principle: Positron-Emission-Tomographie (PET)



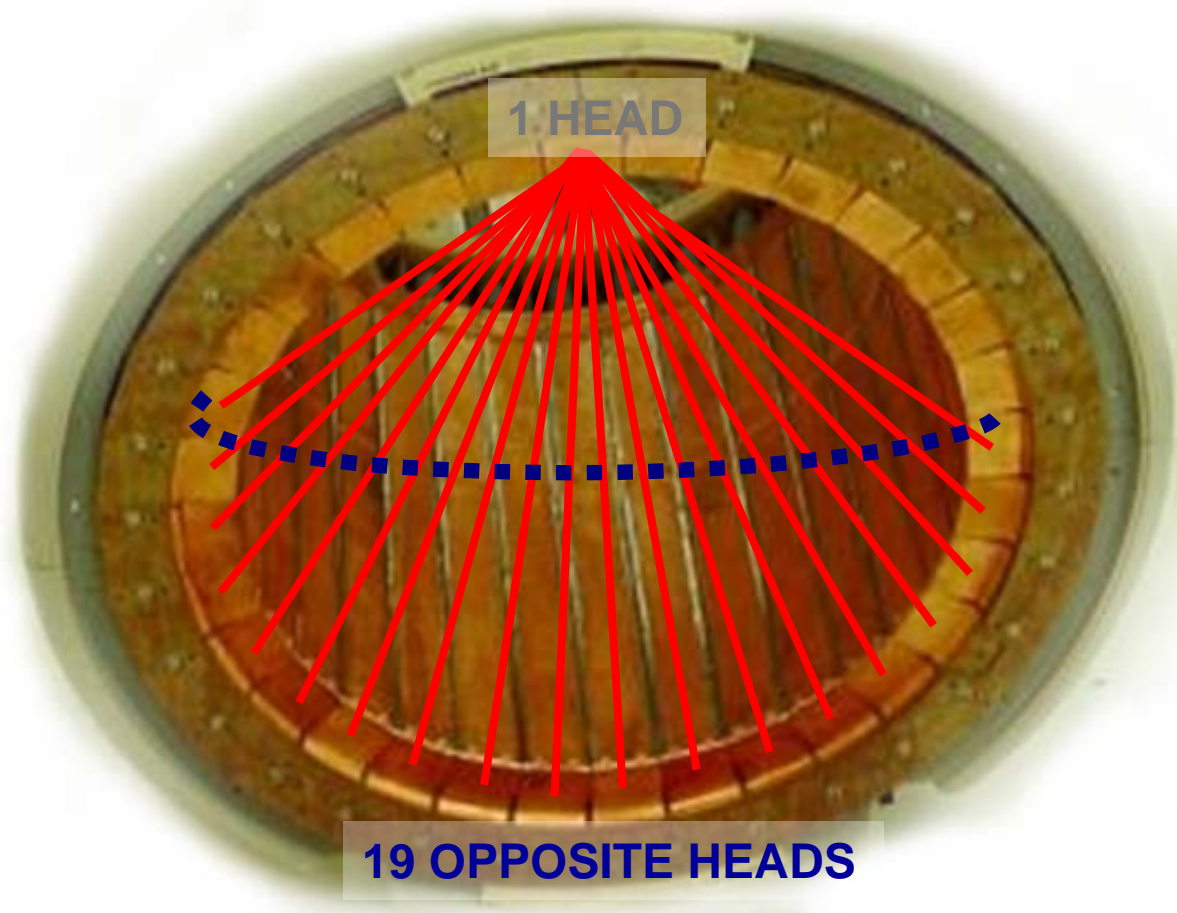
β^+ decay process of metabolic tracer:



detector
combination
(D_1, D_2)

LOR
line of response
(R, θ)

3D data acquisition



144 crystals / block
6 blocks / modul
32 moduls

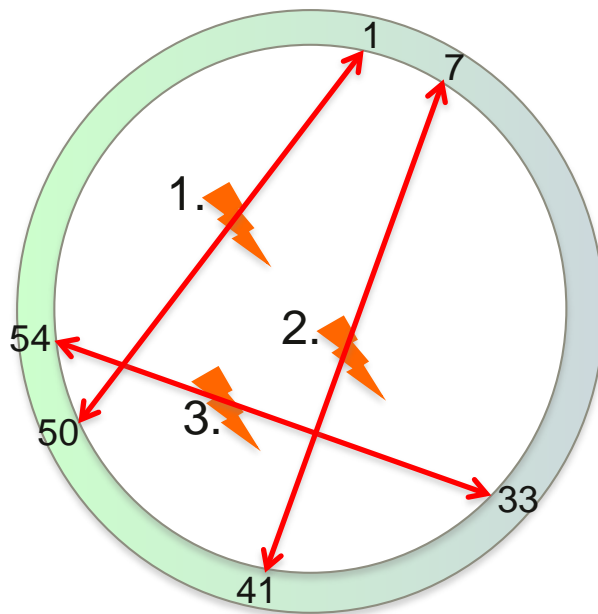
→ **27648**
detector crystals

→ **227 million**
detector
combinations
(Lines-Of-
Response)

BrainPET Data Formats (I)

List Mode (LM) Data:

list of detected coincidences
in chronological order



store pairs of
detector numbers

1. event: (1 ,50)
2. event: (7 ,41)
3. event: (33,54)

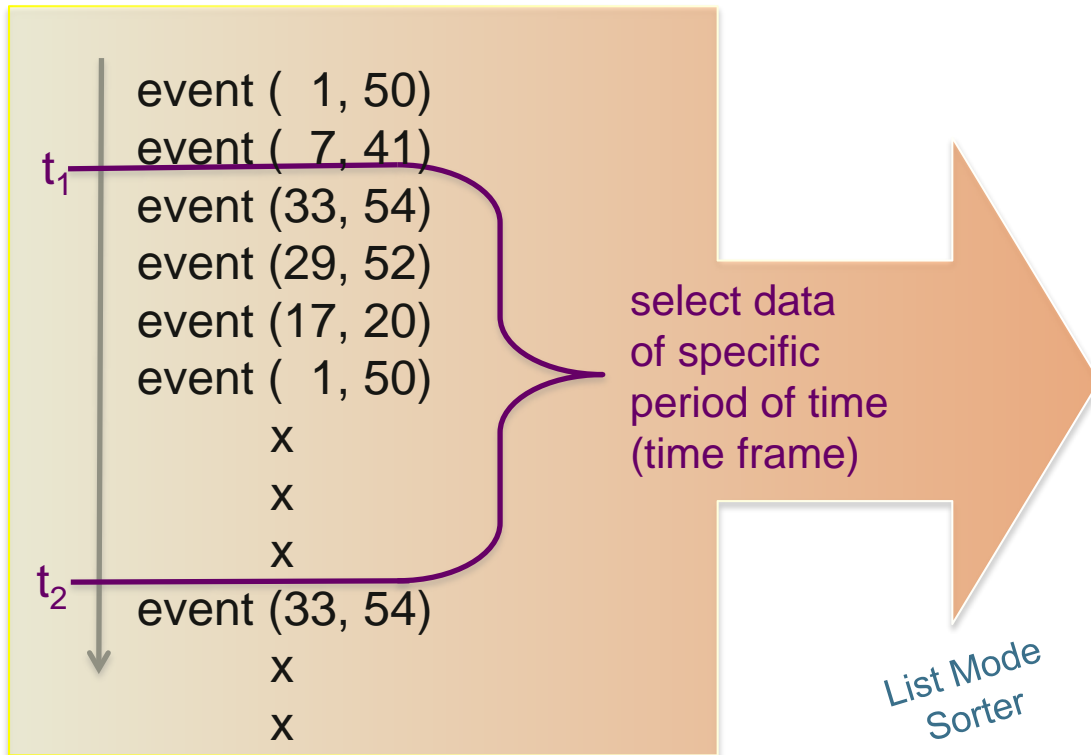
Acquisition
Time

additional tags are
periodically inserted:

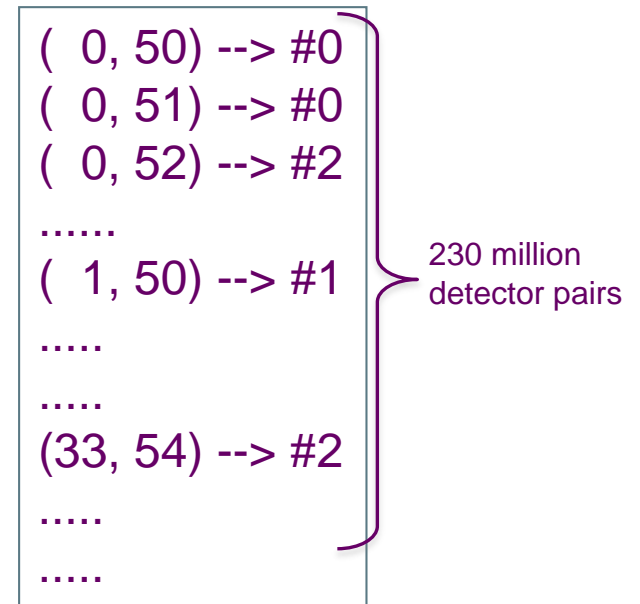
- time tags
- count rate tags
- external trigger tags

BrainPET Data Formats (II)

List Mode (LM) Data



Line-of-Response (LOR) Data:
sum of detected coincidences
for any detector pair

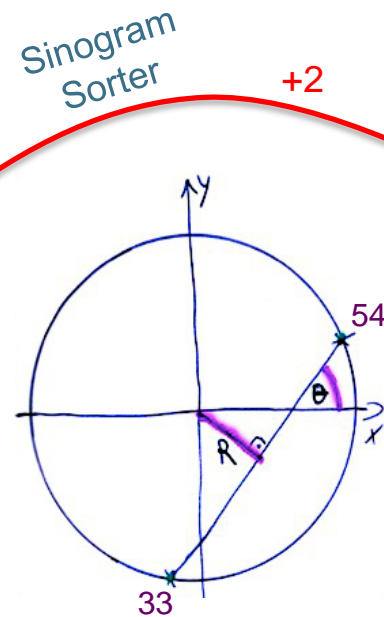


BrainPET Data Formats (III)

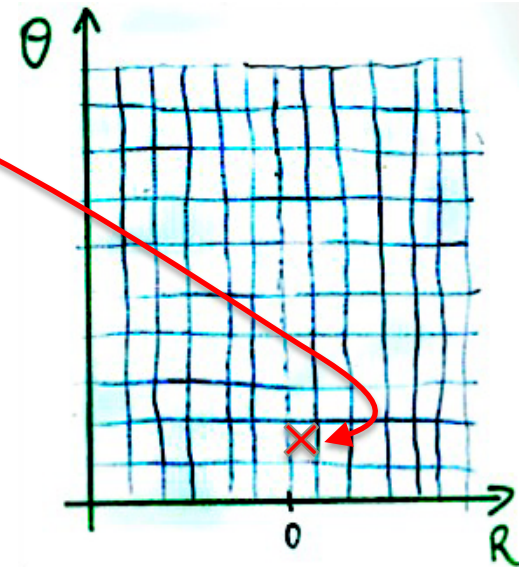
Sinogram Data:
geometrical sorting
of LOR data into projections

LOR Data

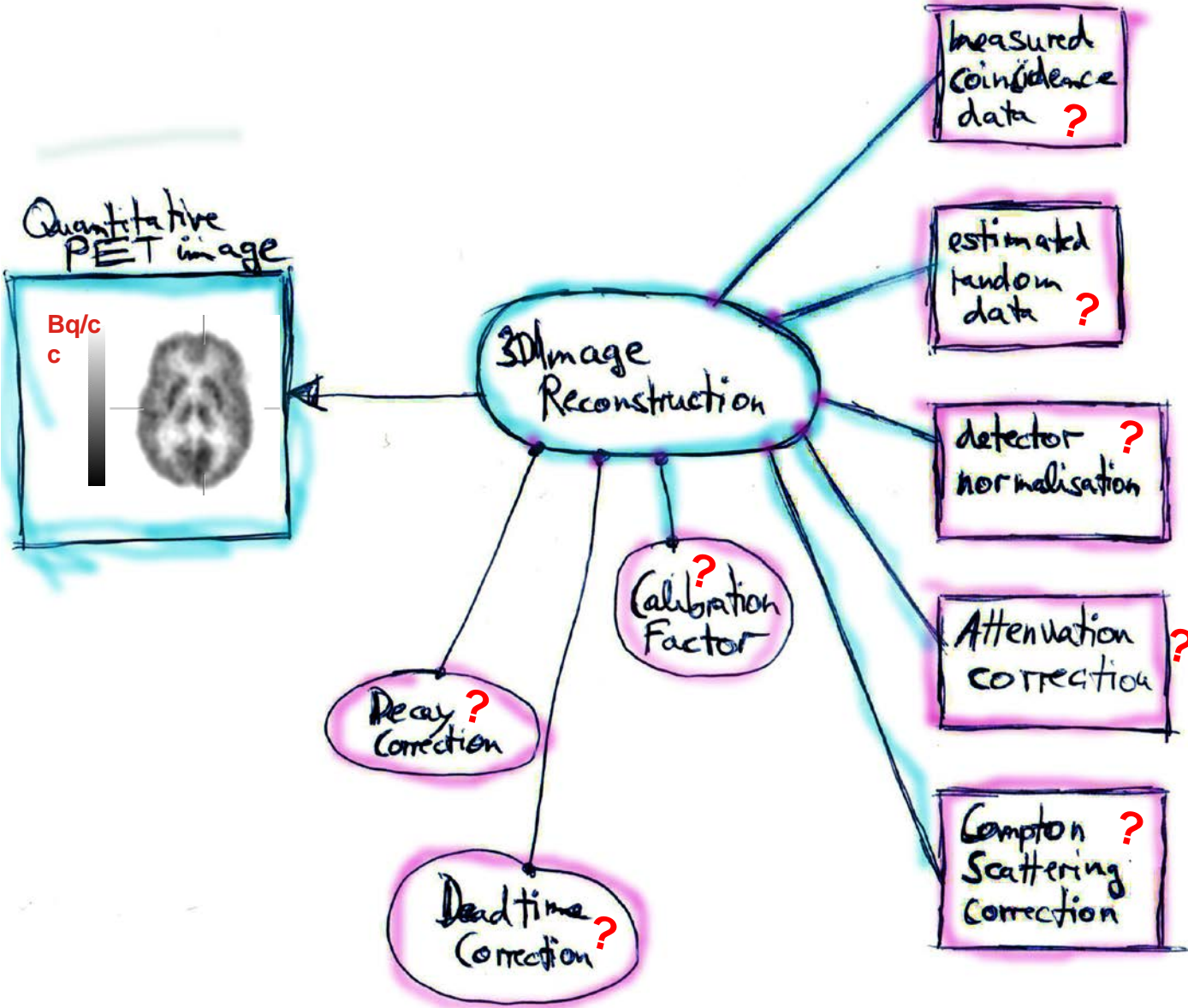
- (0, 50) --> #0
- (0, 51) --> #0
- (0, 52) --> #2
-
- (1, 50) --> #1
-
-
- (33, 54) --> #2
-
-



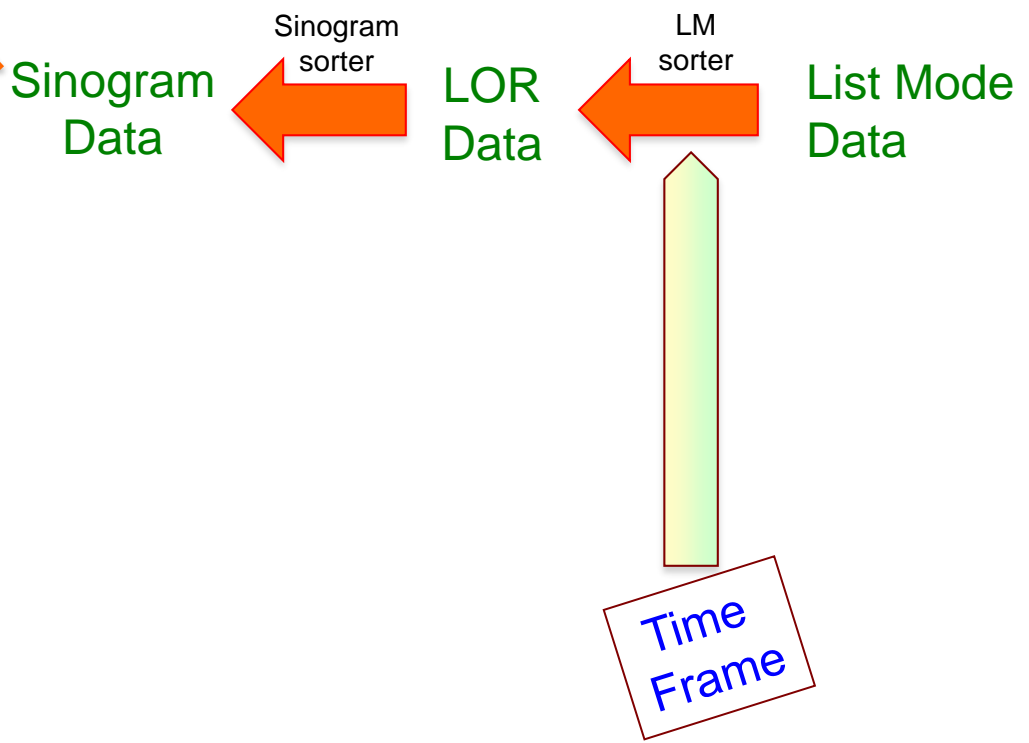
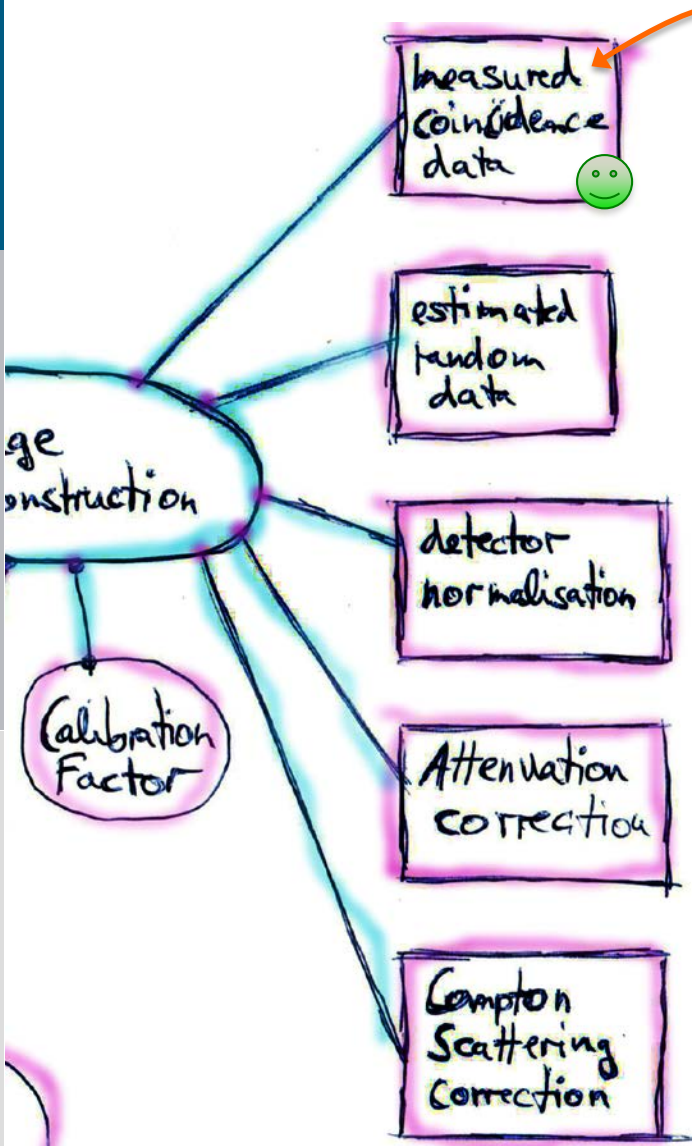
$$\{D_1, D_2\} \rightarrow \{R, \theta\}$$



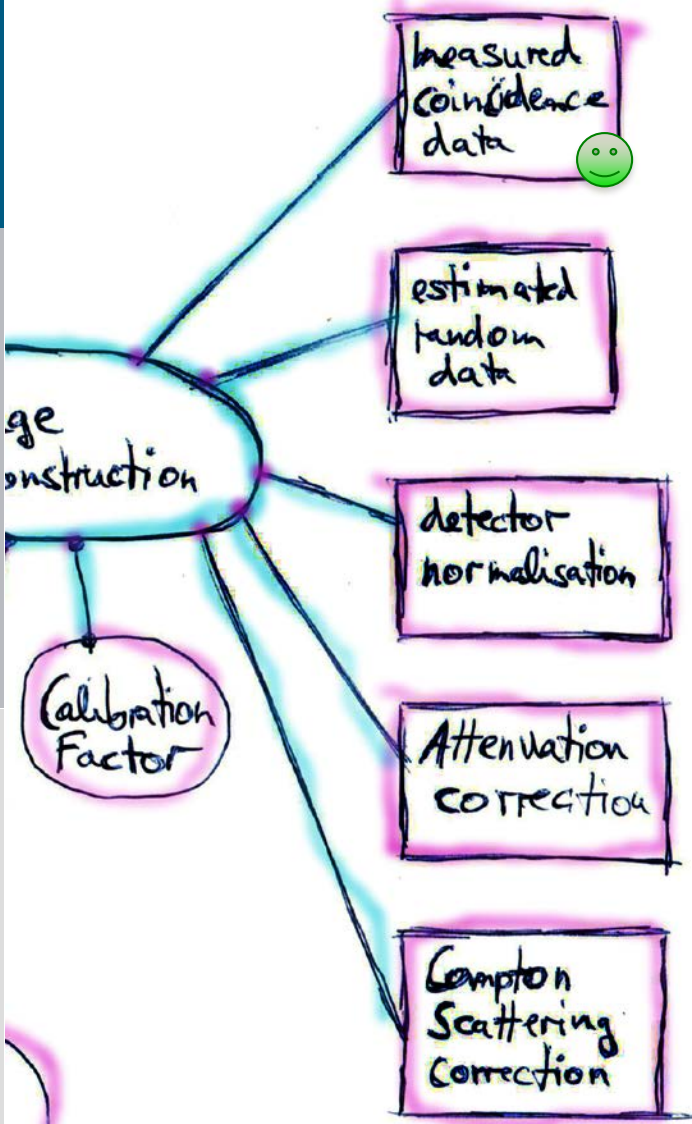
Inputs for Quantification



Measured Coincidence Data (Prompts)

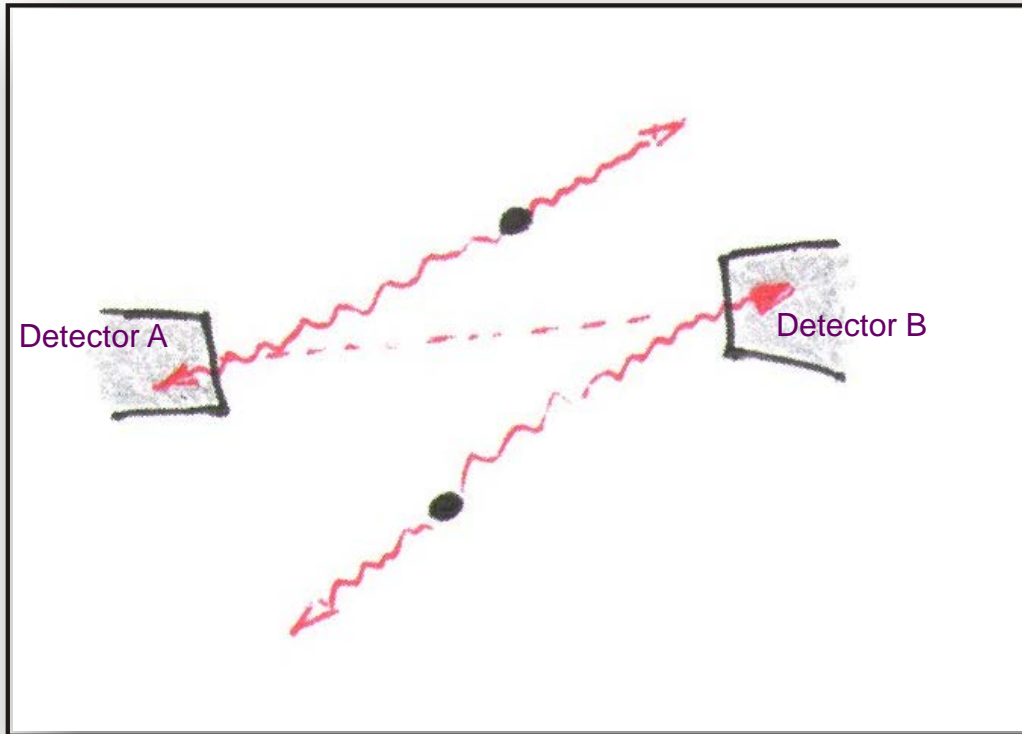


Estimated Random Data



Randoms Correction ??

Unavoidable Random Coincidences



Events (measured) =

Events (true)

+

Events (random)

(signal)

(background,
exact value unknown)

Probability of Catching Randoms

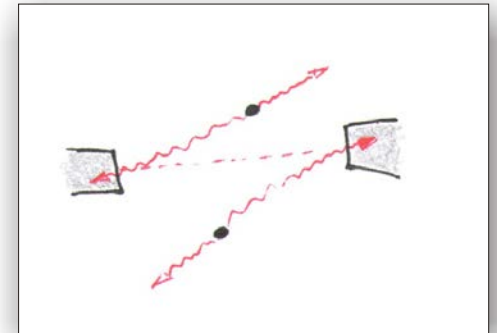
- Expected Rate of Randoms

$$R_{AB} = 2 \tau S_A S_B$$

R : Random Rate for Detector Pair (A,B)

S_A, S_B : Single Count Rates of detectors

τ : Coincidence Timing Window (12 ns)



- Direct Measurement: “*Delayed Window*”

Acquire Pseudo Coincidences due to Timing Offset T_{off}

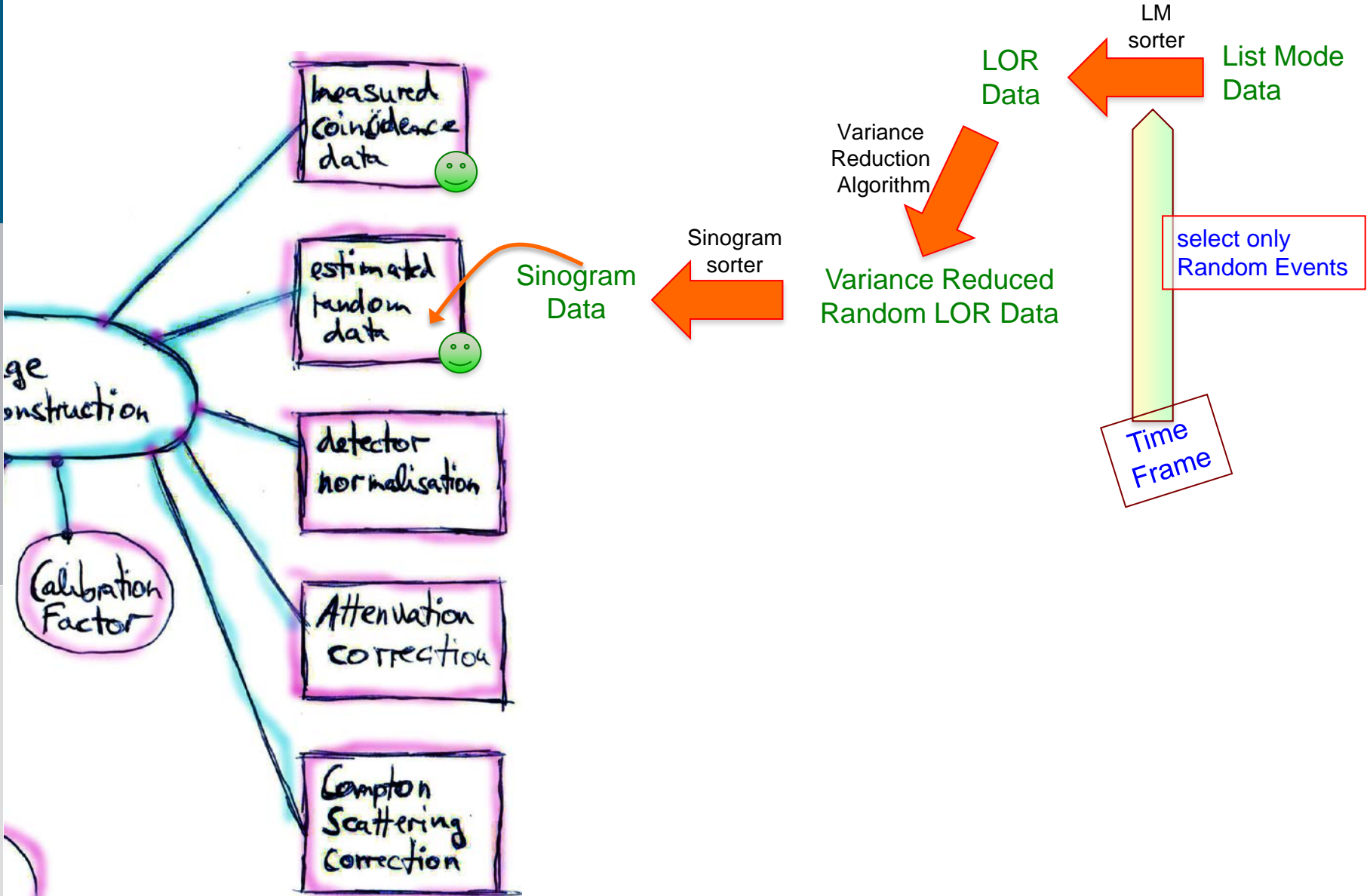
true coincidences: $|t_a - t_b| <$

random coincidences: $|t_a - t_b + T_{\text{off}}| <$

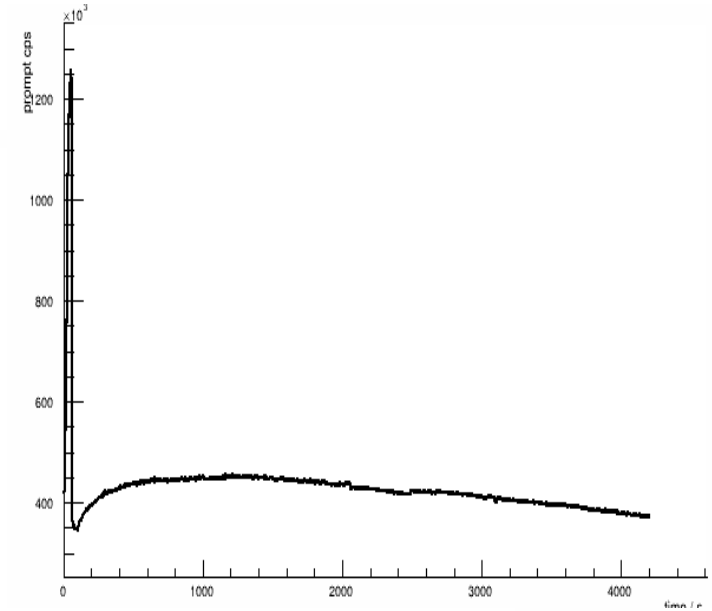
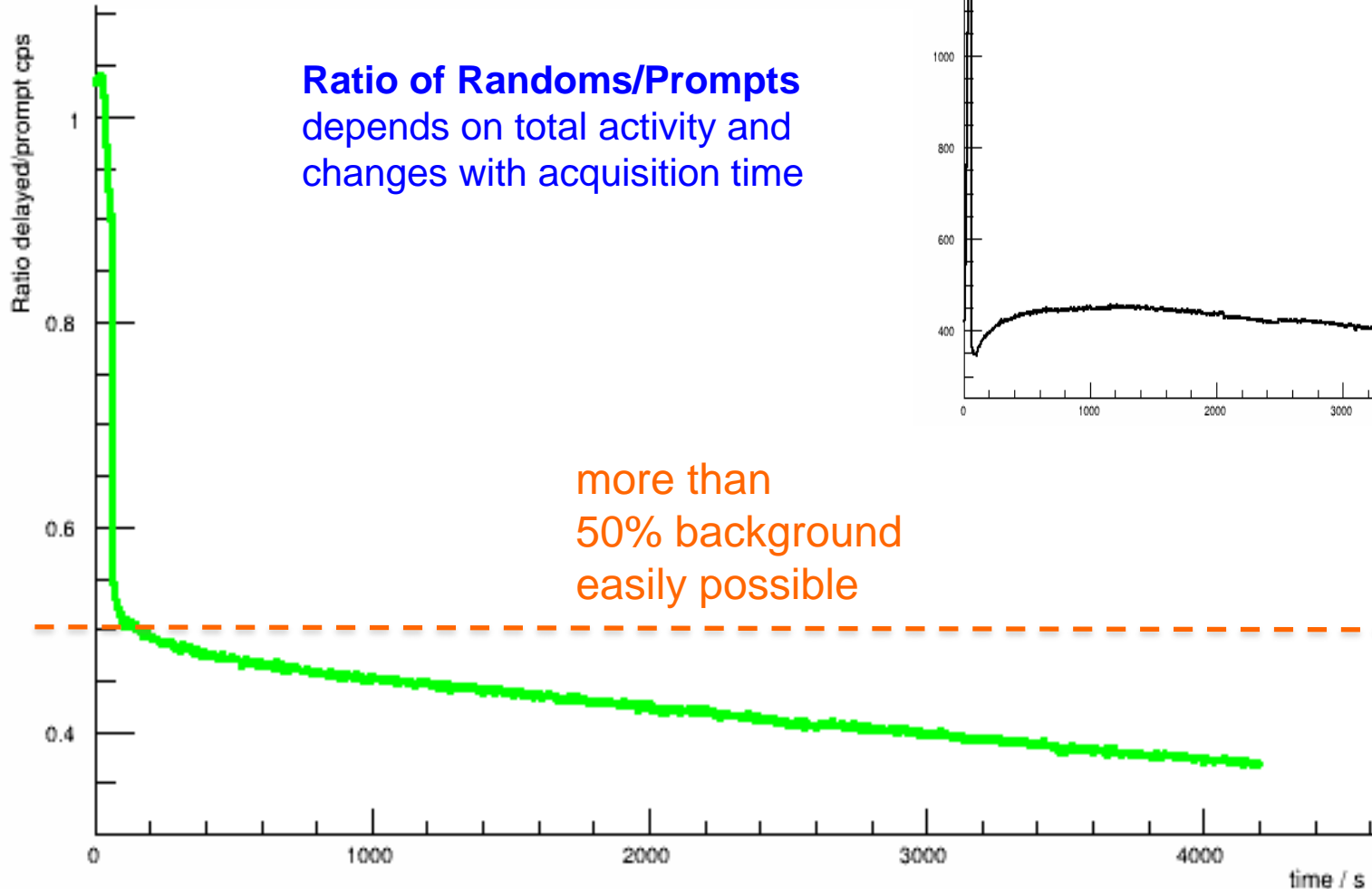
Detected Random Coincidences

also inserted into List Mode Stream during Acquisition

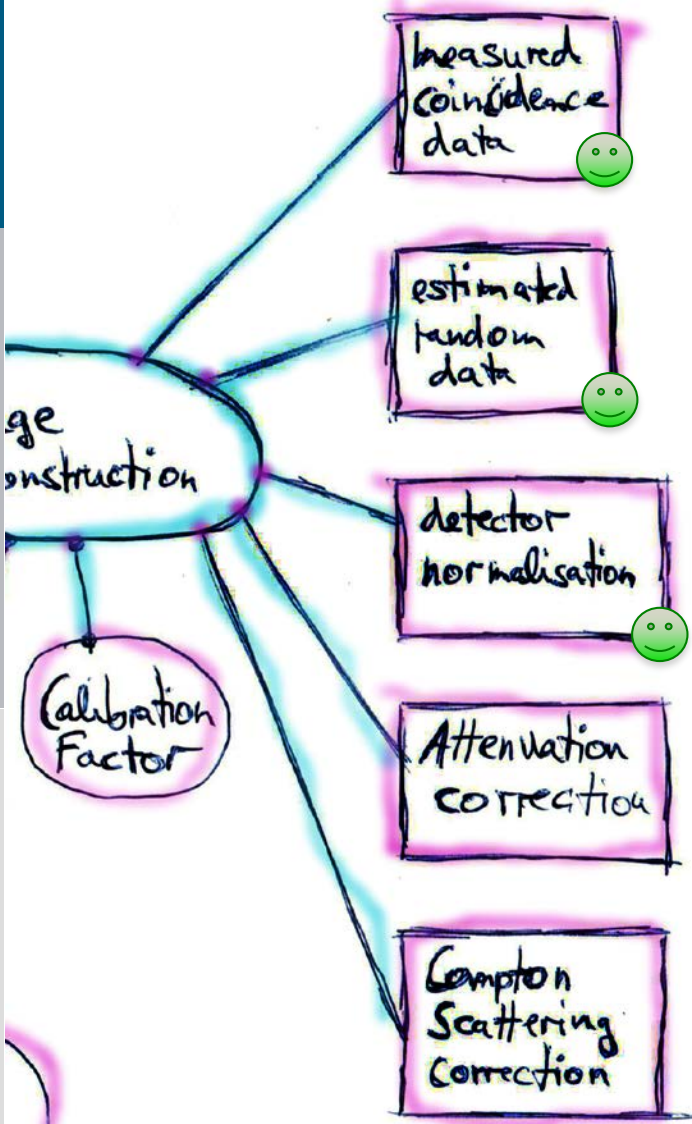
Estimation of Randoms



Example: Patient Measurement

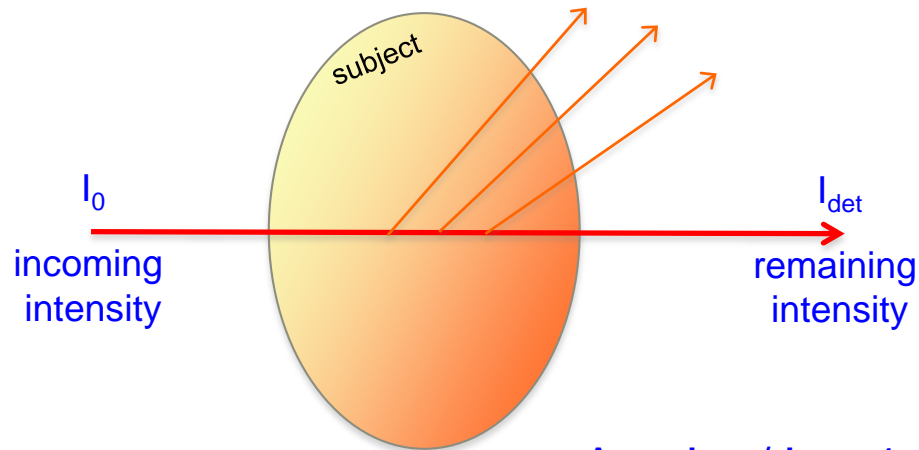


Attenuation



Attenuation ??

Subject & any material causes attenuation of emitted radiation

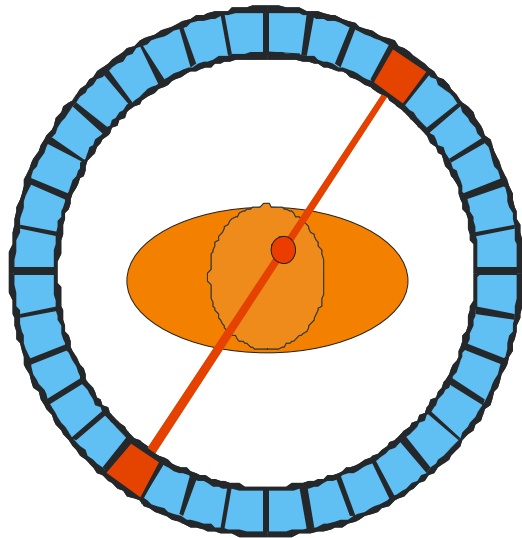


$$A_x = I_{det} / I_0 < 1$$

A_x mainly depends on
electron densities along
path
Compton scattering is the
dominant effect causing
attenuation
(deflection of radiation)

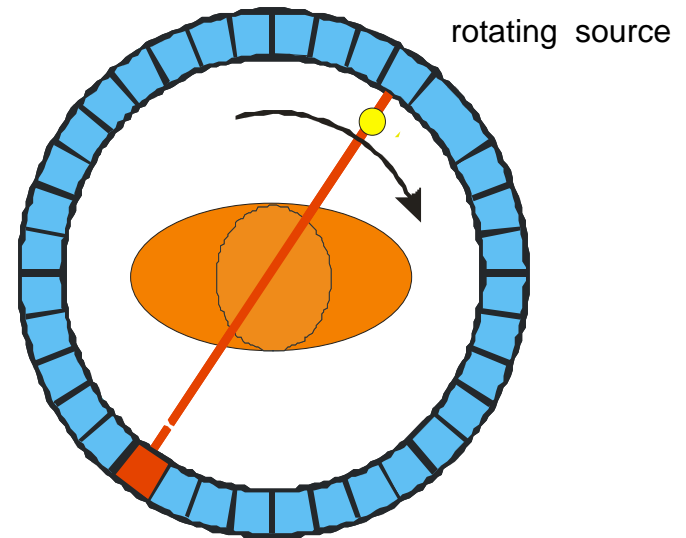
Attenuation Correction (direct measurement)

Emission Measurement



$$I_{\text{LOR}} = \int A(x,y) dl * \text{ACF}_{\text{LOR}}$$

Transmission Measurement



$$\text{ACF}_{\text{LOR}} = \exp(- \int \mu (x,y) dl')$$

ACF → attenuation correction factor

A → activity distribution

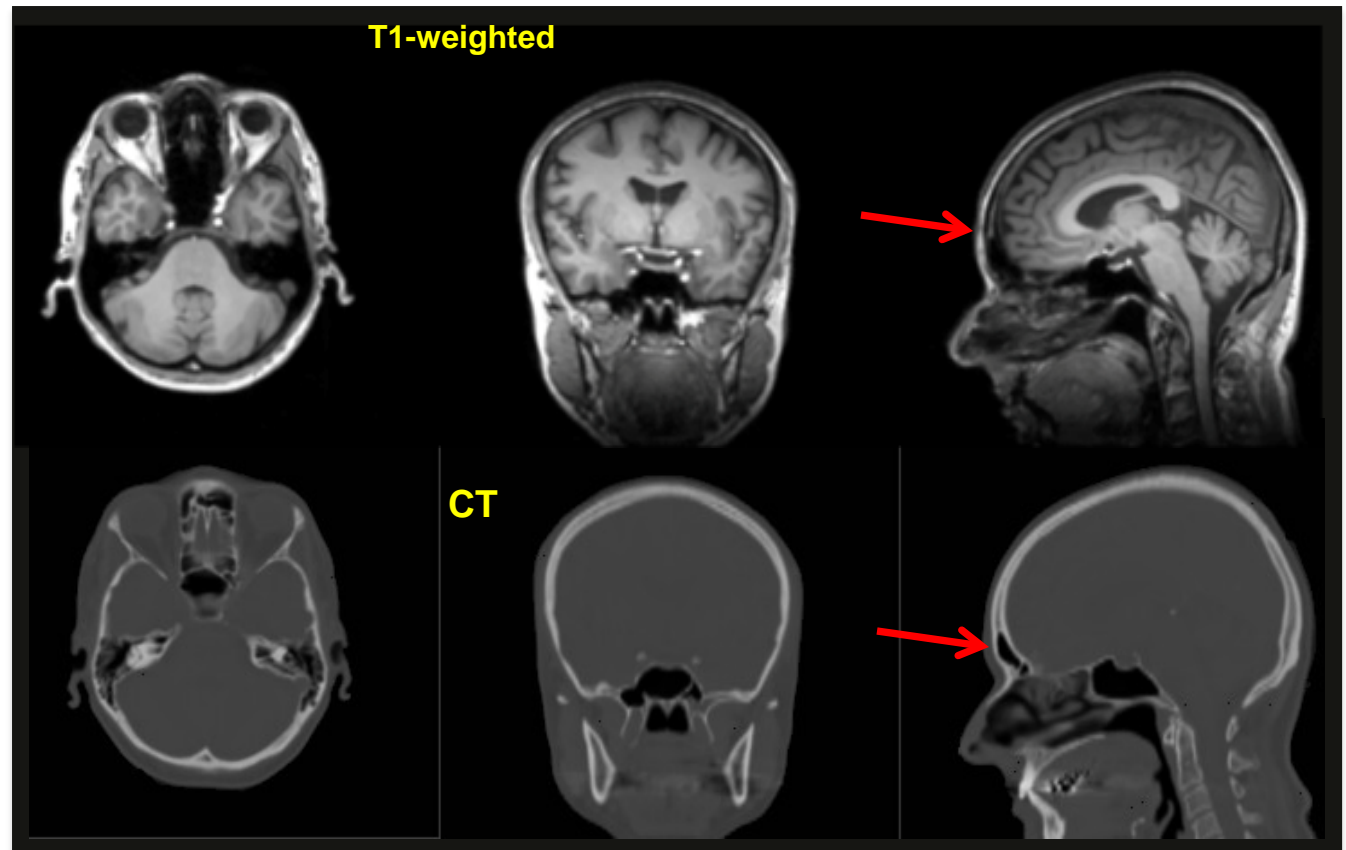
μ → attenuation values

Attenuation Correction (from MR measurement)

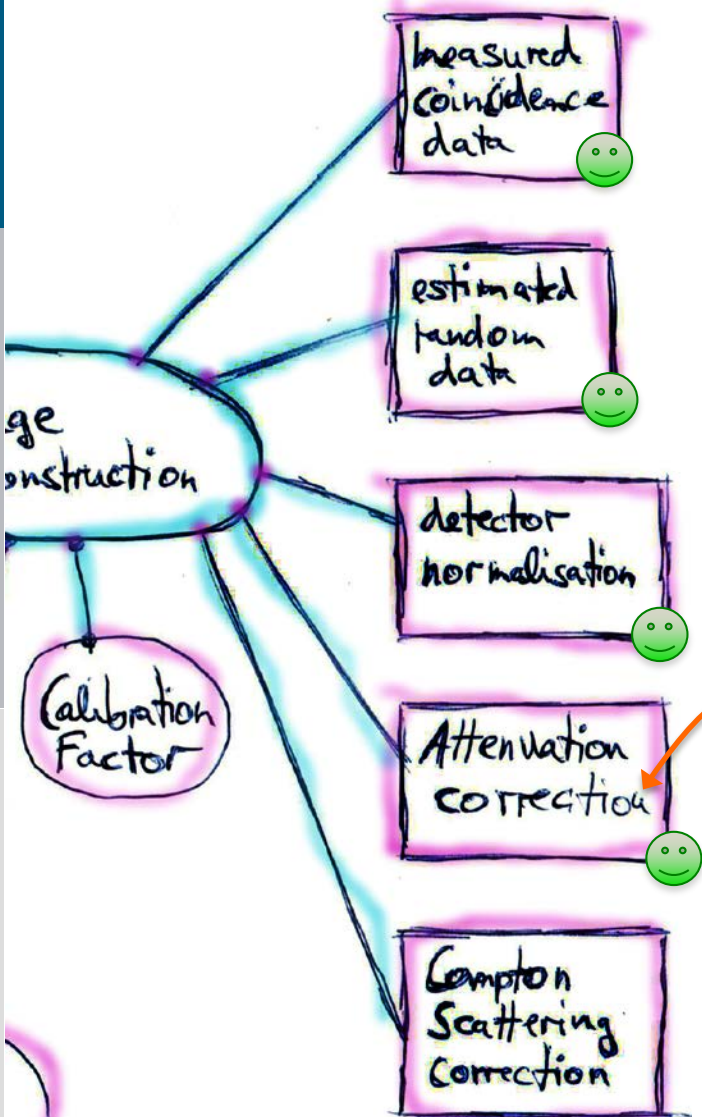
Challenge:

MR information provides no direct estimate of photon attenuation

(e.g. bone + cavities -> no Signal in Standard-MR-Seq.)

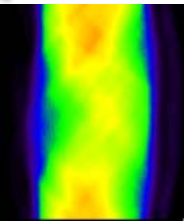
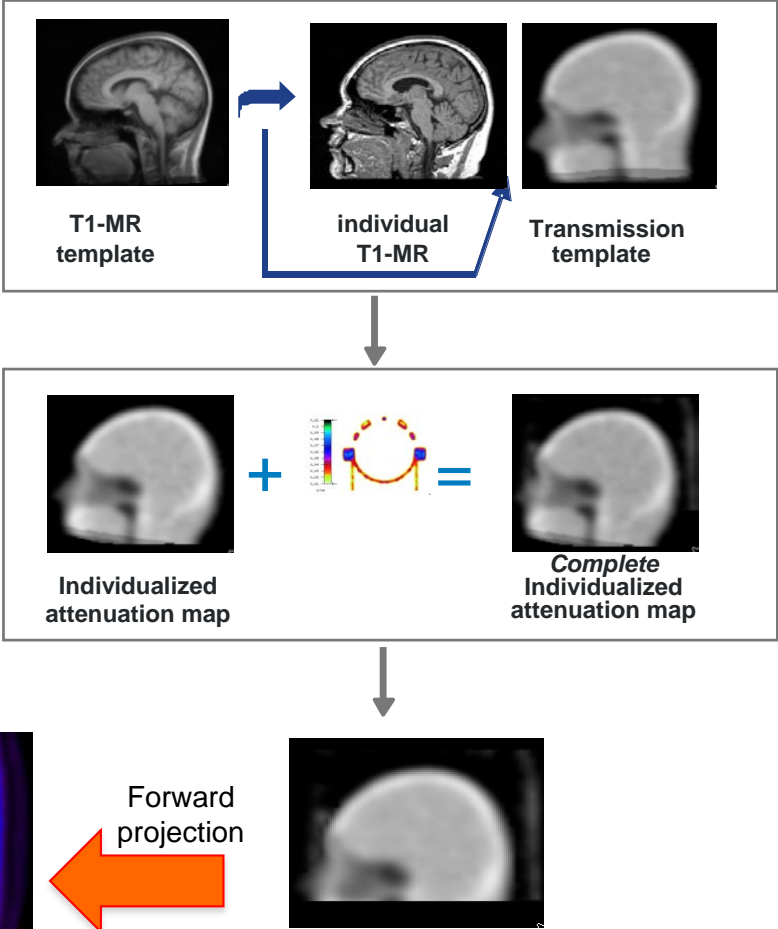


Attenuation Correction



Template based Approach

Rota Kops E et al, IEEE 2009 Proceedings: pp. 2530

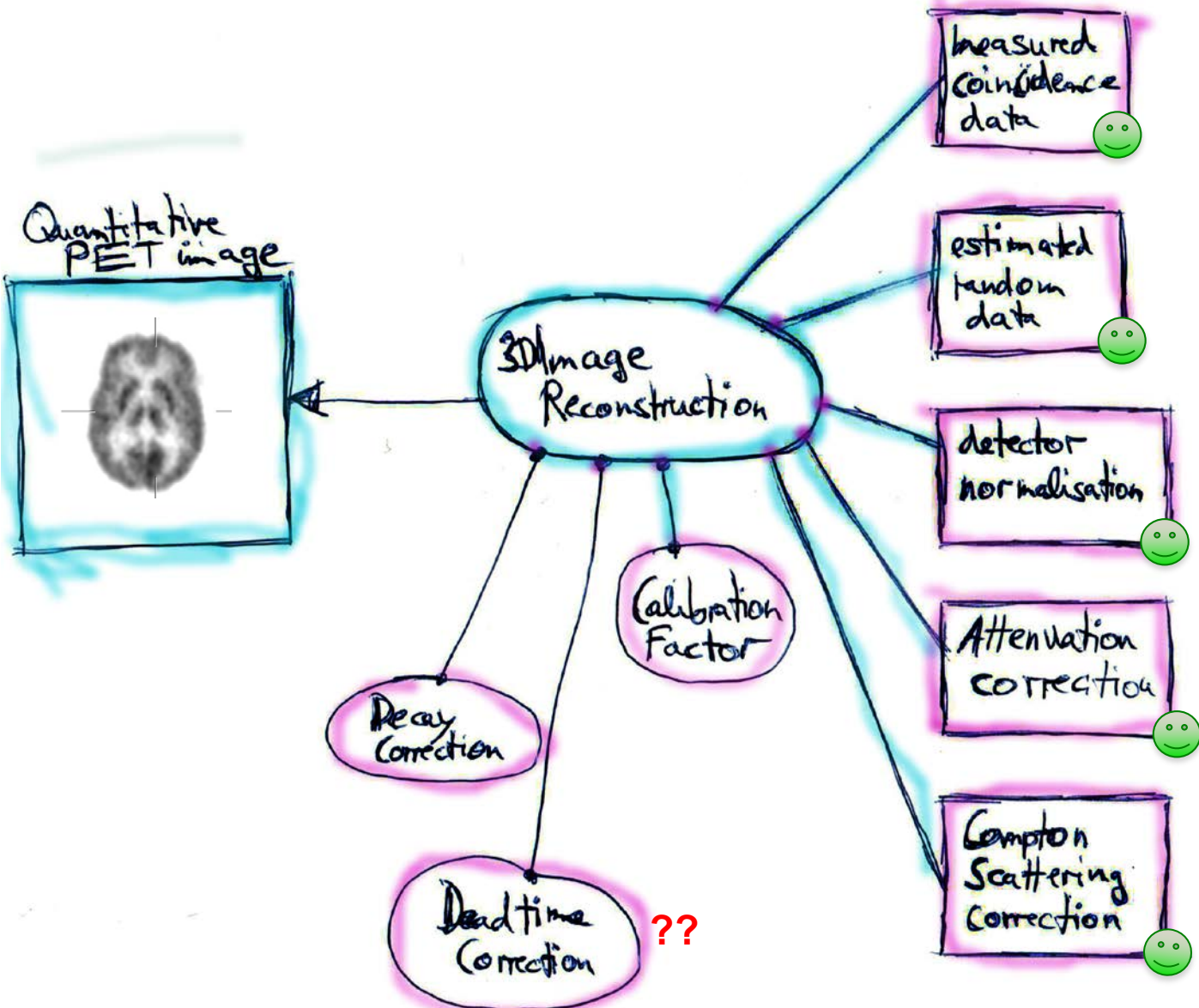


Sinogram Data

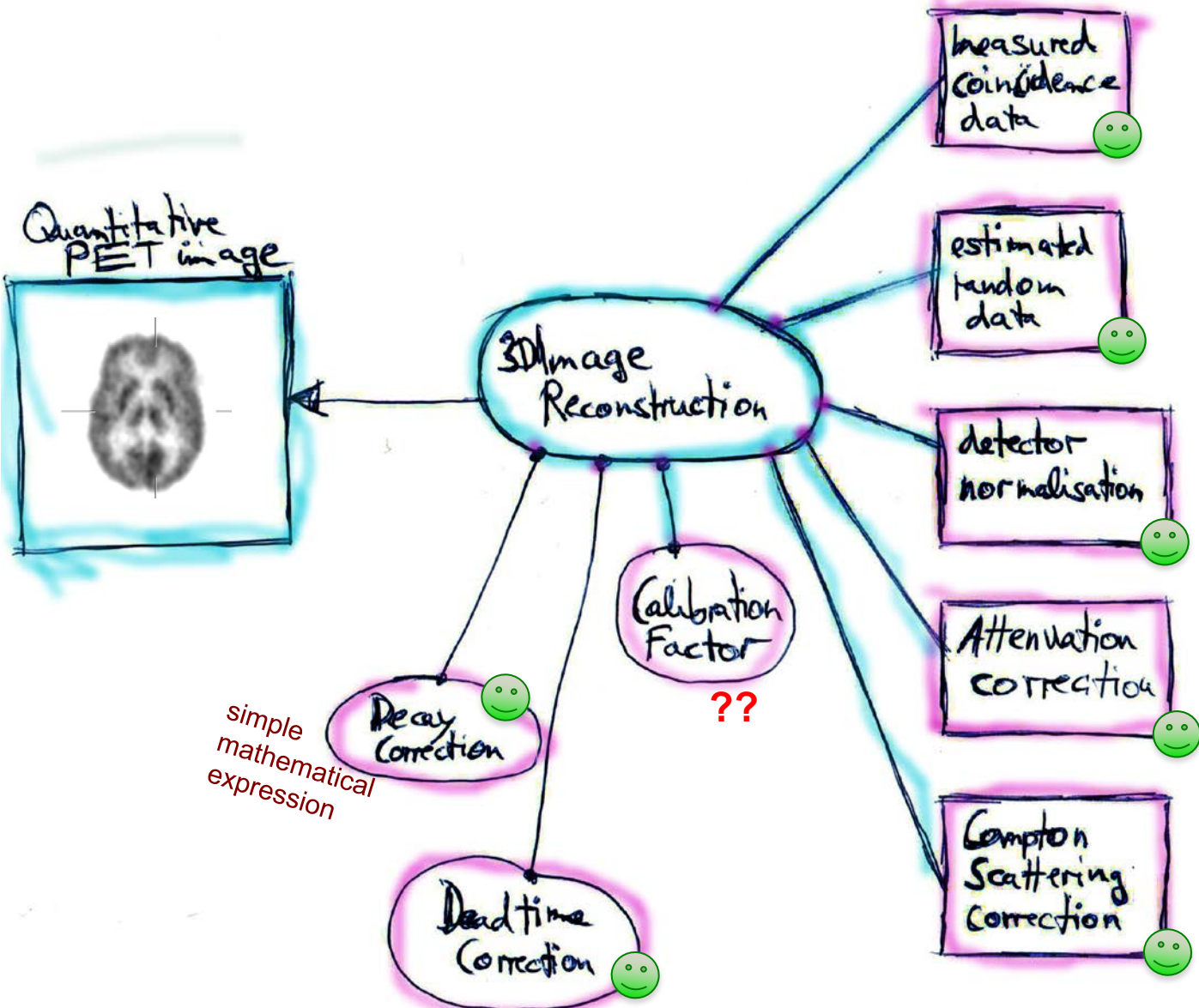
Forward projection



Deadtime Correction

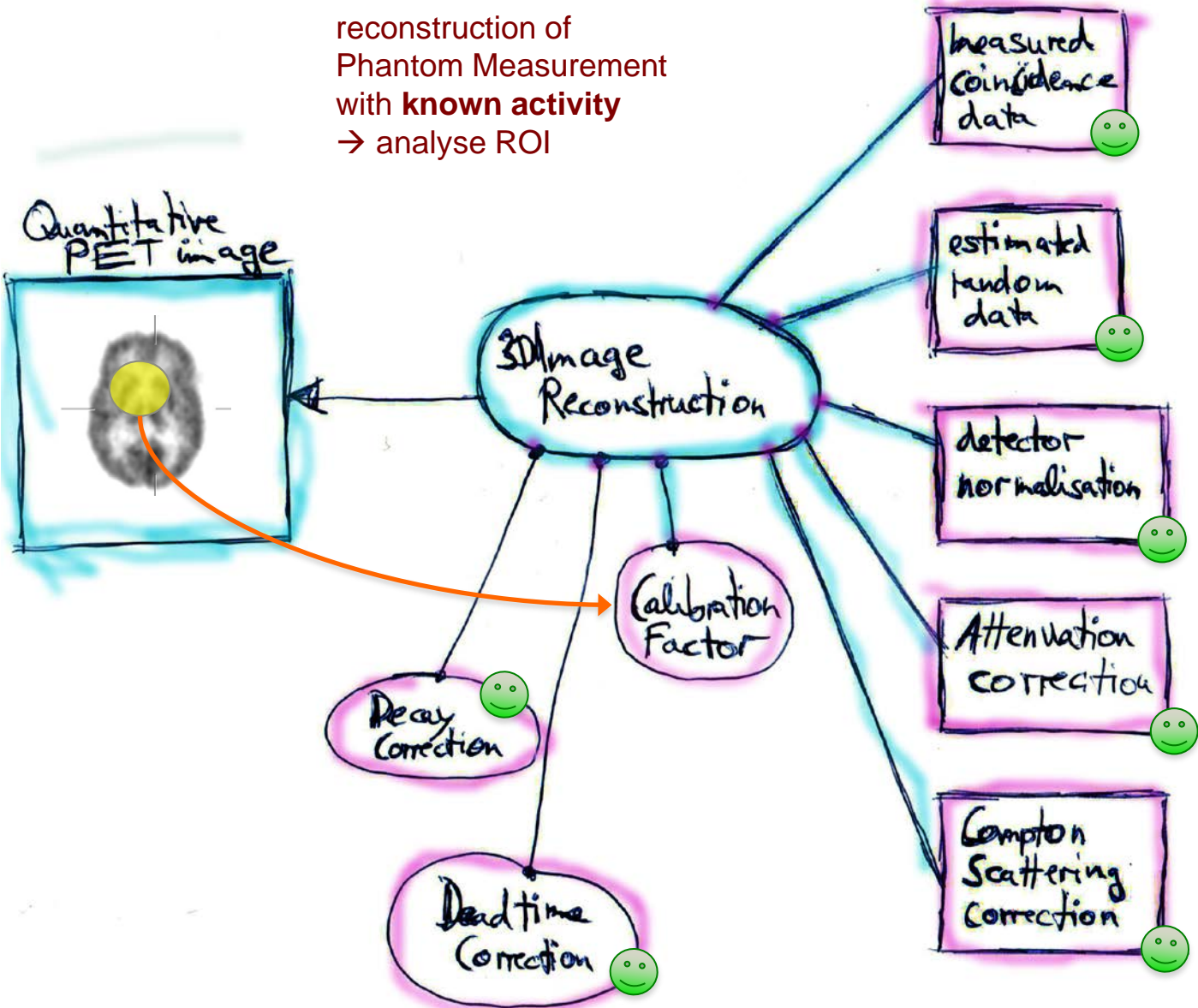


Deadtime Correction

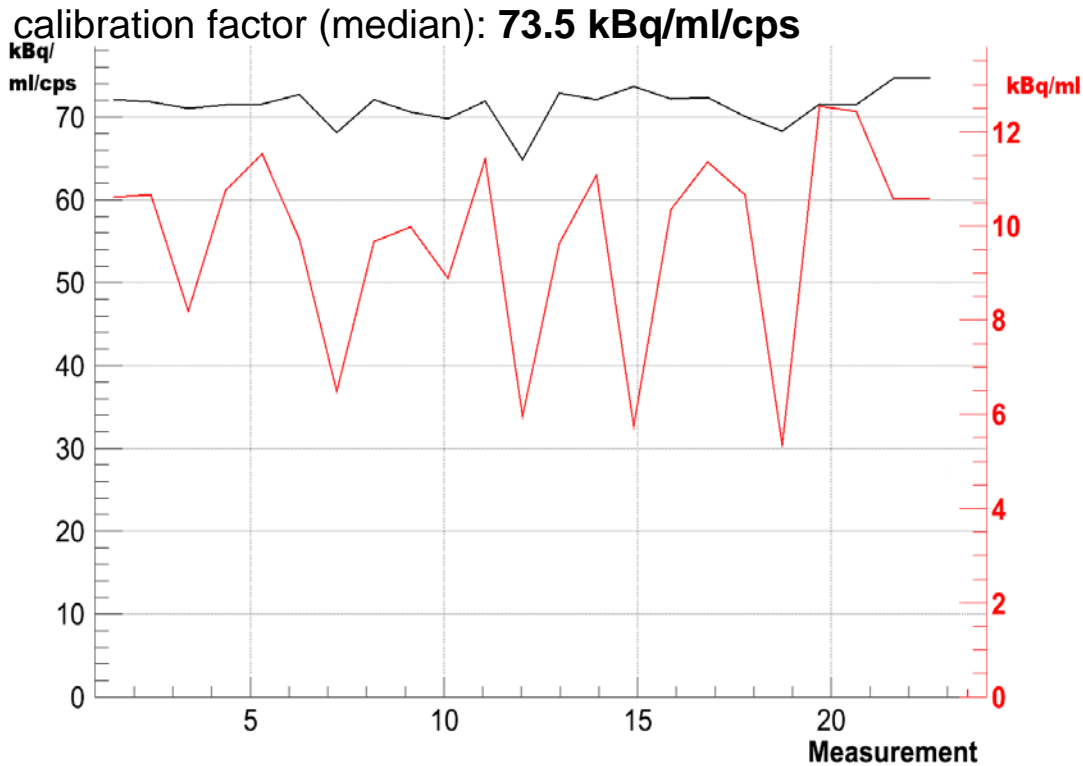


Calibration Measurement

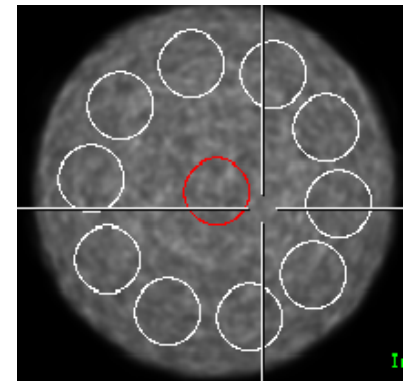
reconstruction of
Phantom Measurement
with **known activity**
→ analyse ROI



Calibration Measurements



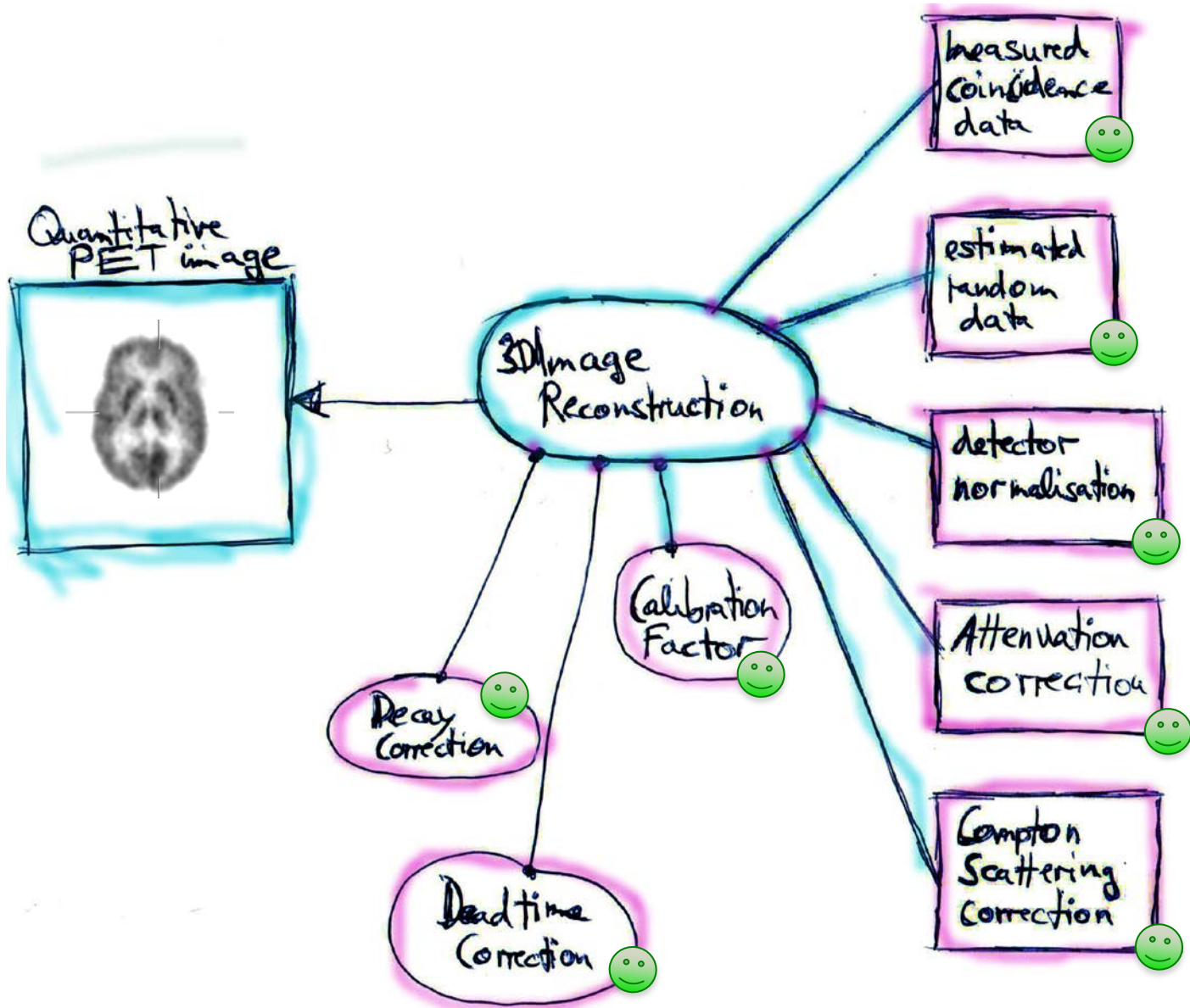
cylinder phantom
(filled with ^{18}F)



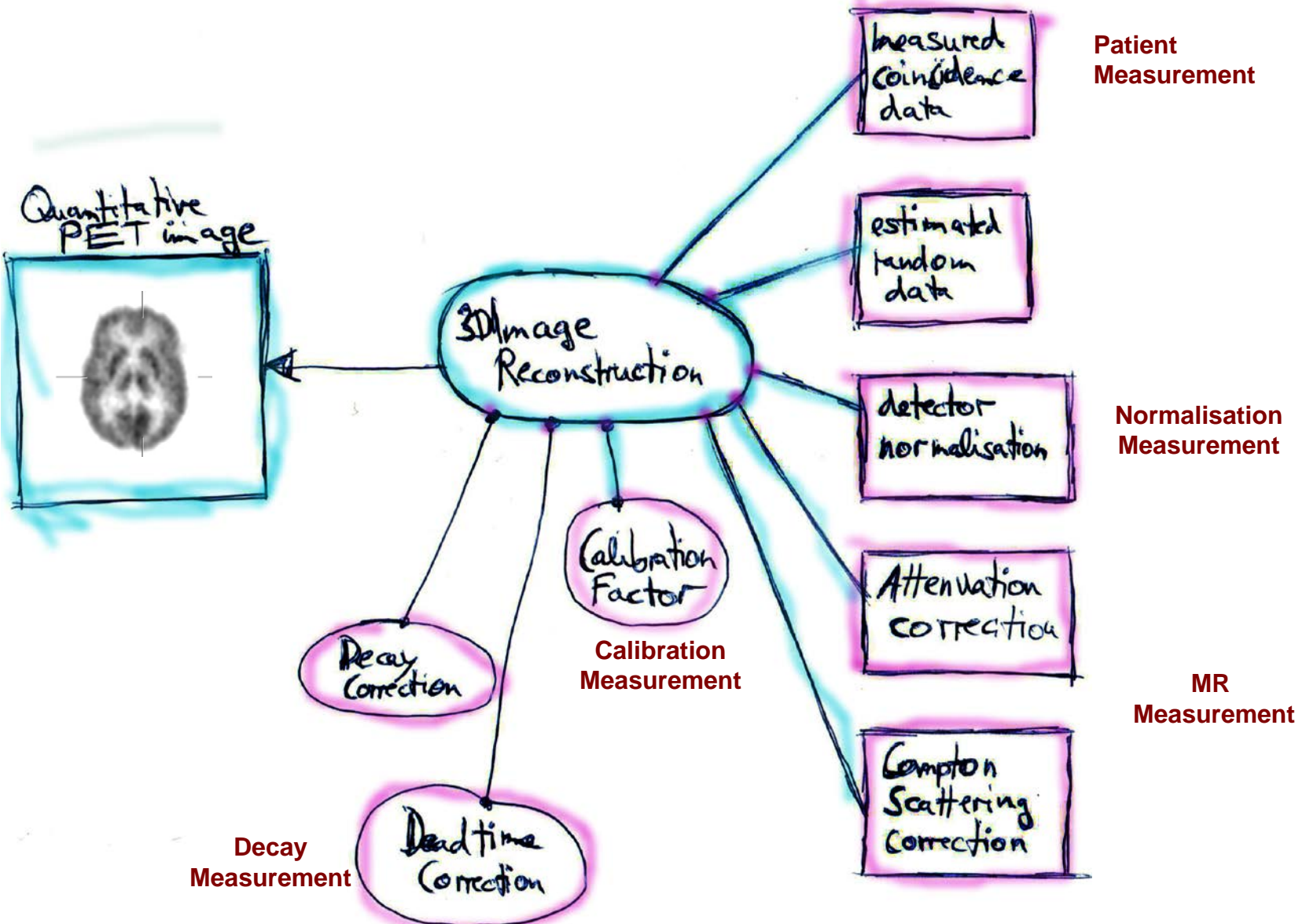
region of
interest

calibration factor

activity
concentration
within phantom

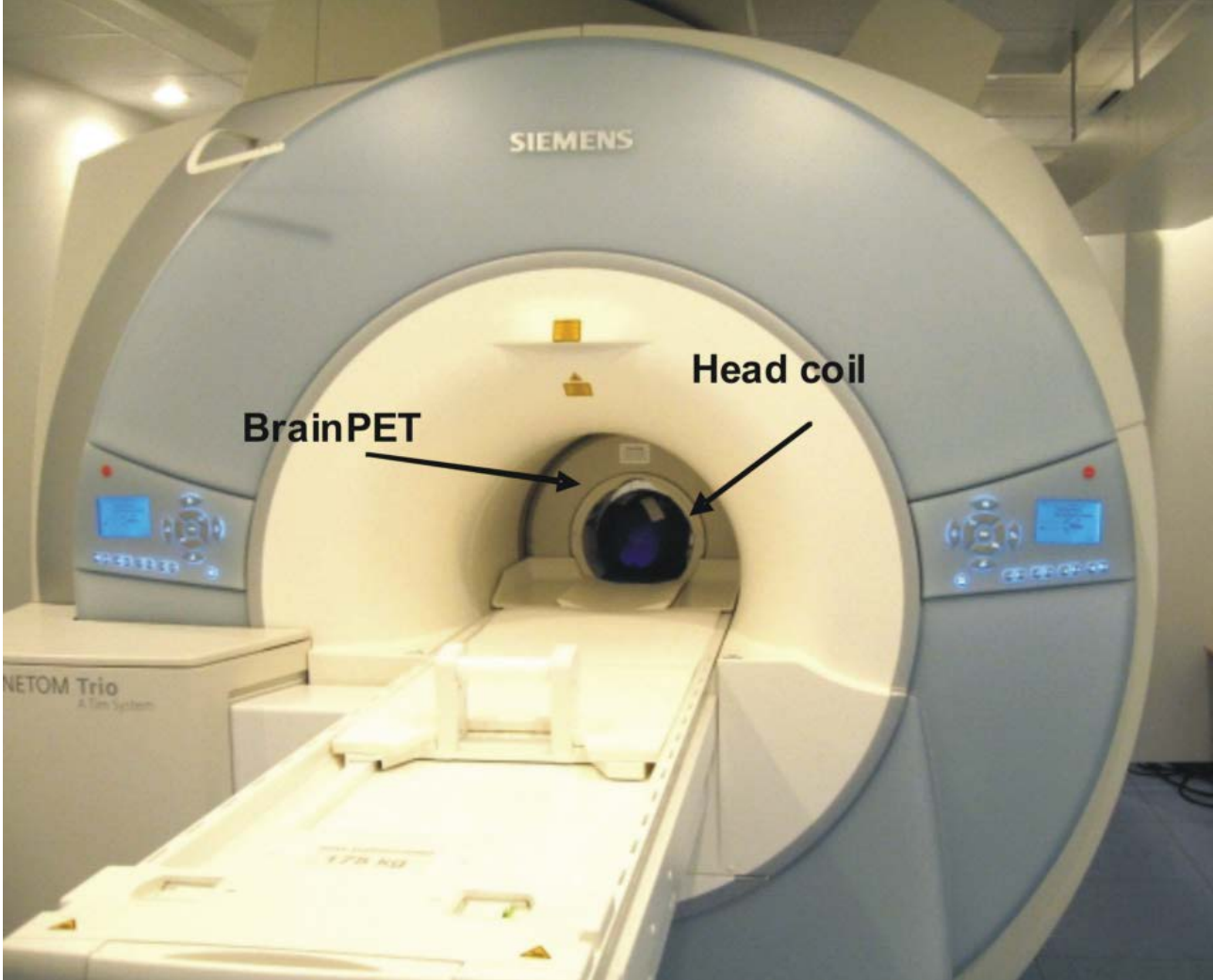


Overview of Inputs for Quantification



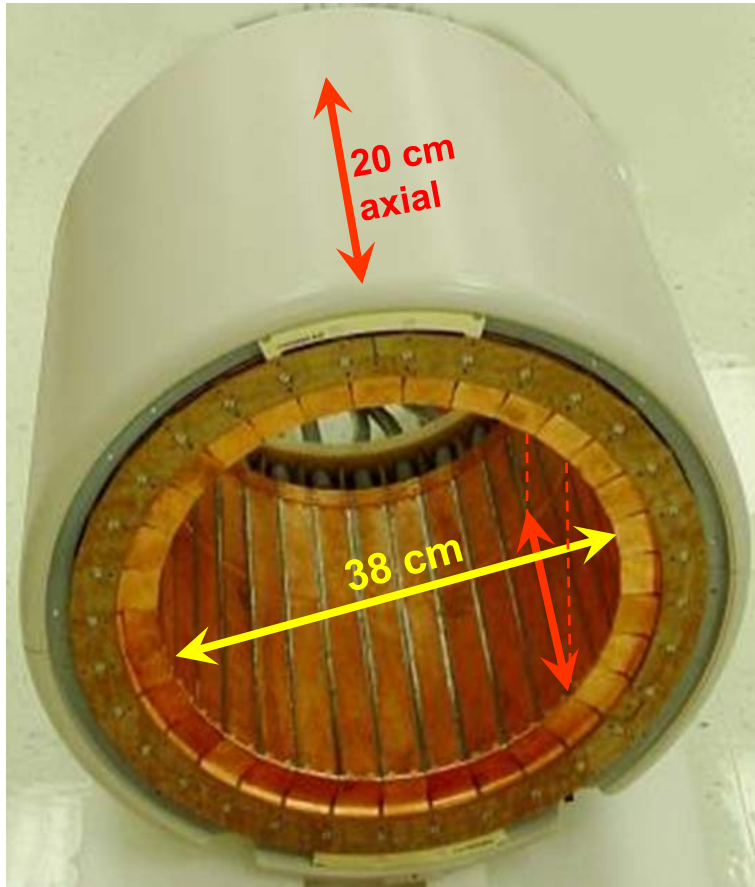
Quantitative PET Imaging with Hybrid MR-PET Scanners

BrainPET in 3T-Tim-Trio MR

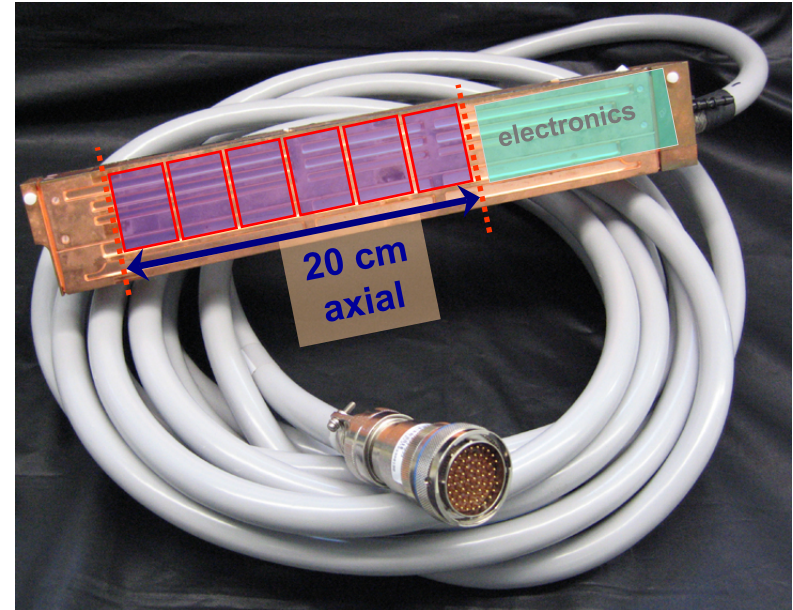


BrainPET insert

scanner with 32 heads

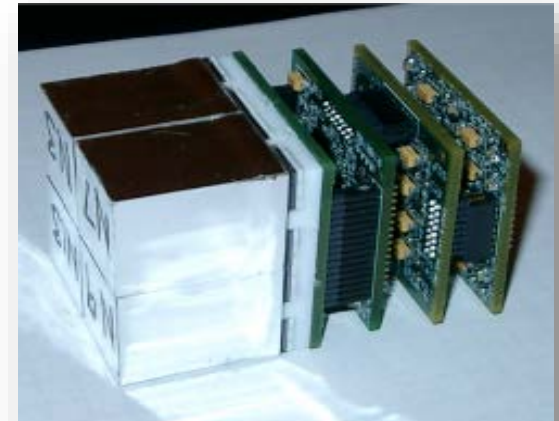
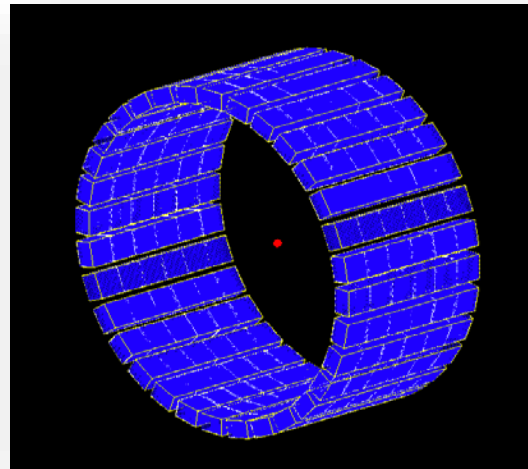


single detector head

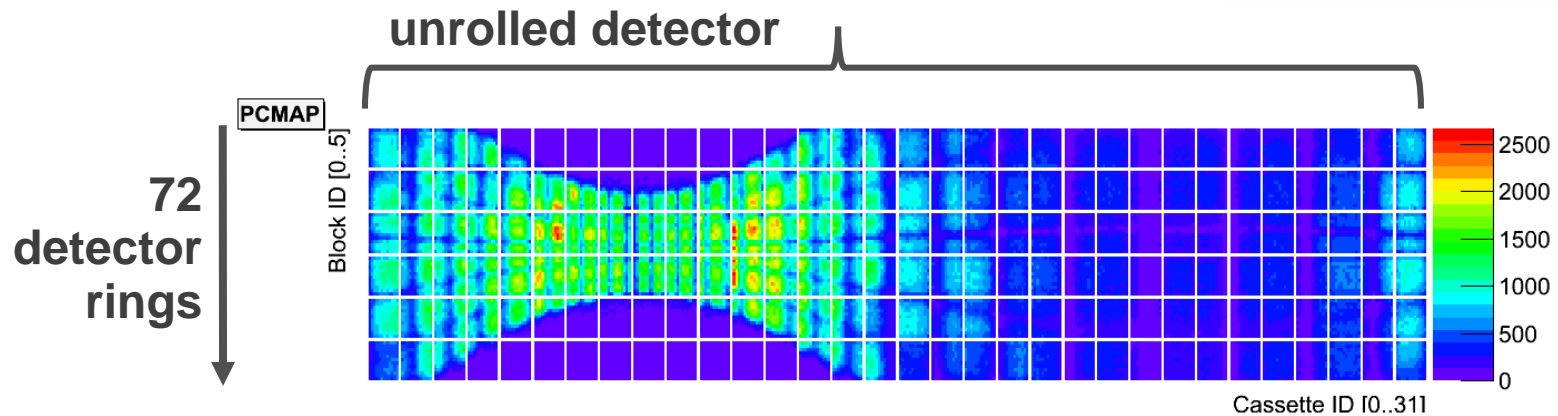


- copper shielded against MR influence
- 6 PET detector blocks / head
- 12 x 12 crystals / block
- 2.5 x 2.5 x 20 mm³ LSO crystal
- 3 x 3 APD / block

Design and Structure of the BrainPET

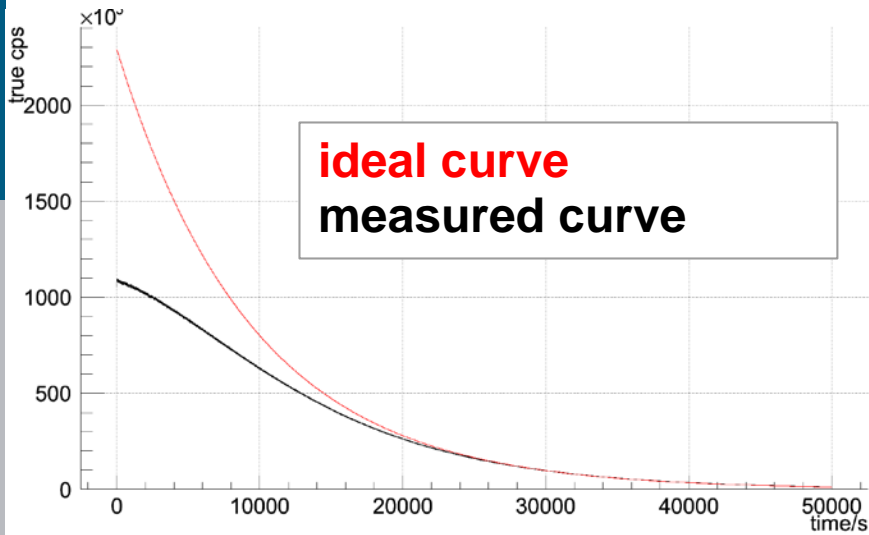


12x12 crystals, 3x3 APDs

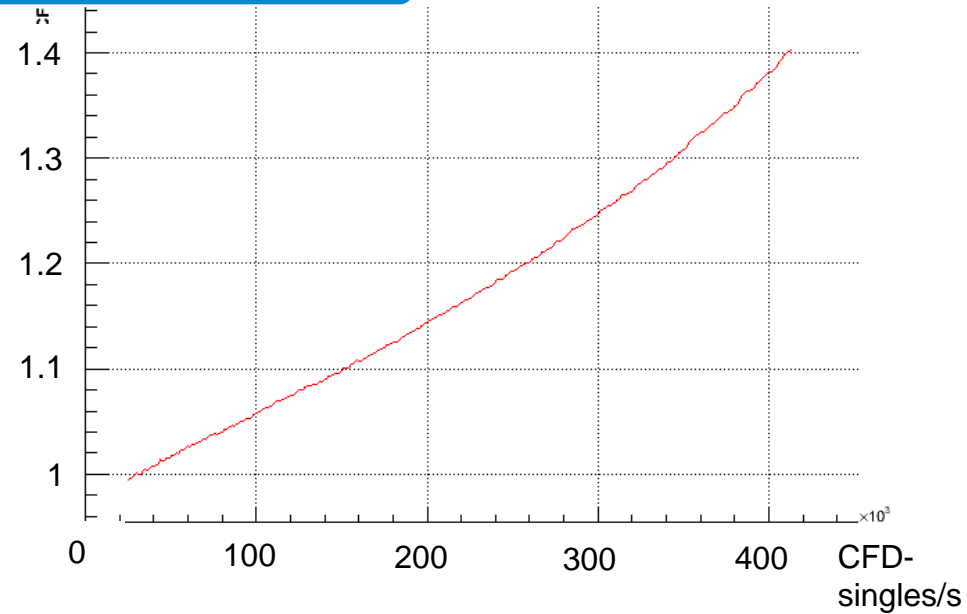


Measurement Effect: Deadtime

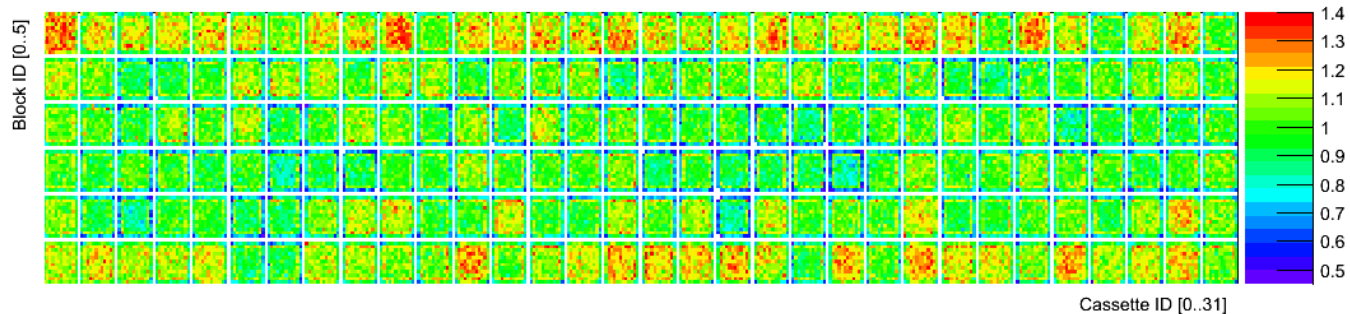
PET countrate:



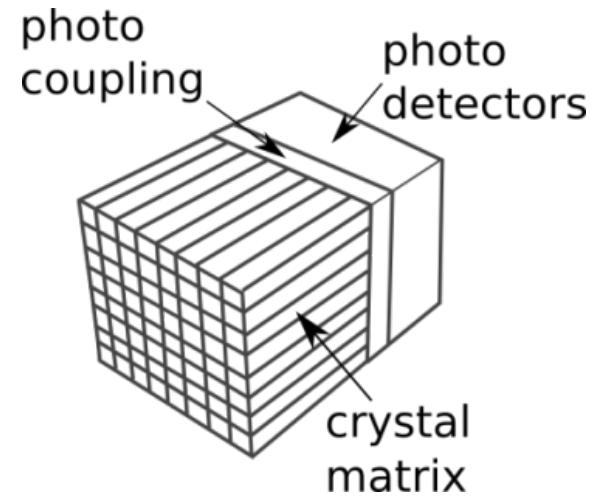
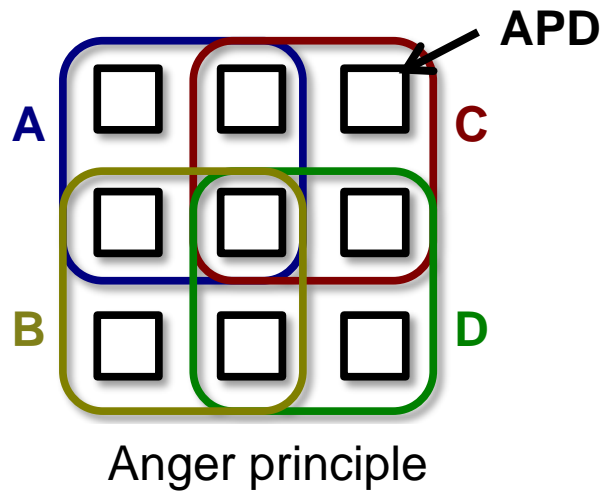
deadtime effect:



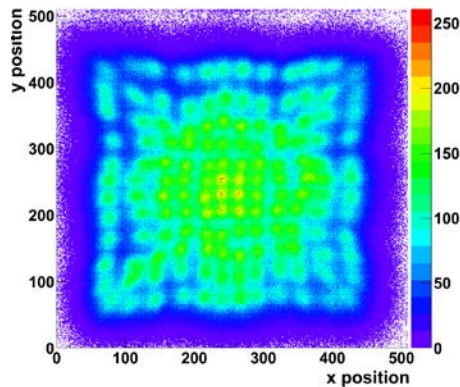
deviation from global correction factor:



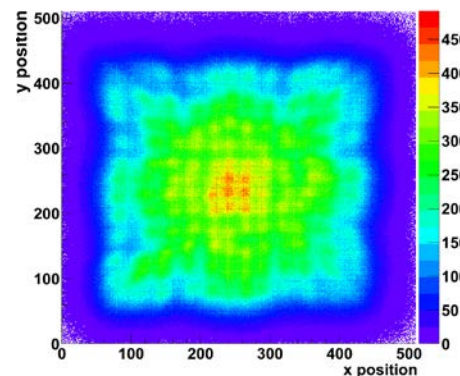
Measurement Effect: Pile-up



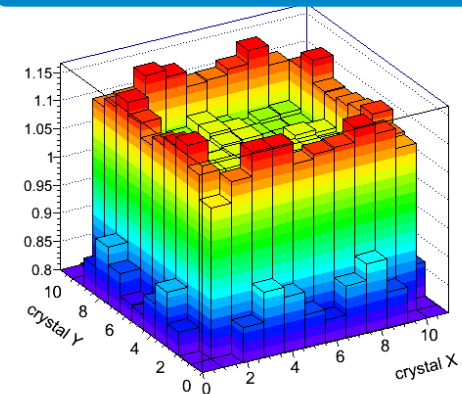
at low countrate:



at high countrate:

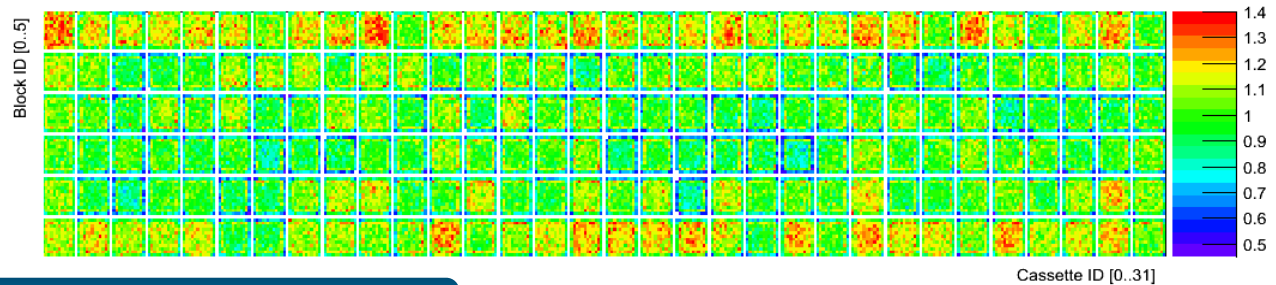


ratio (crystal level):

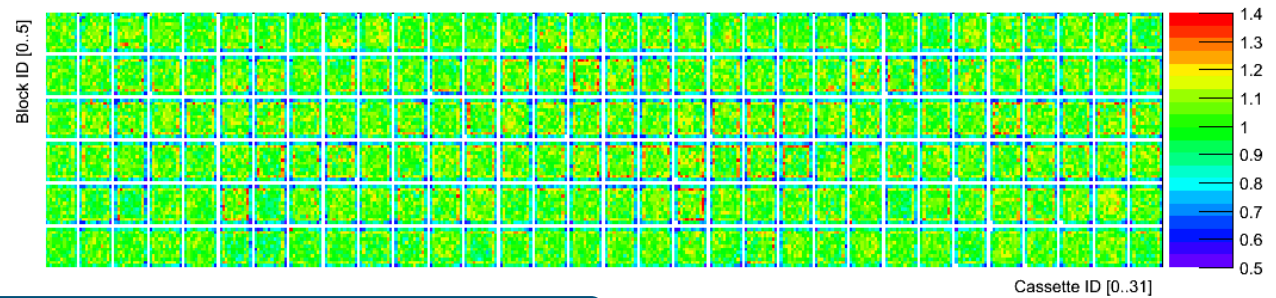


Dynamic Correction

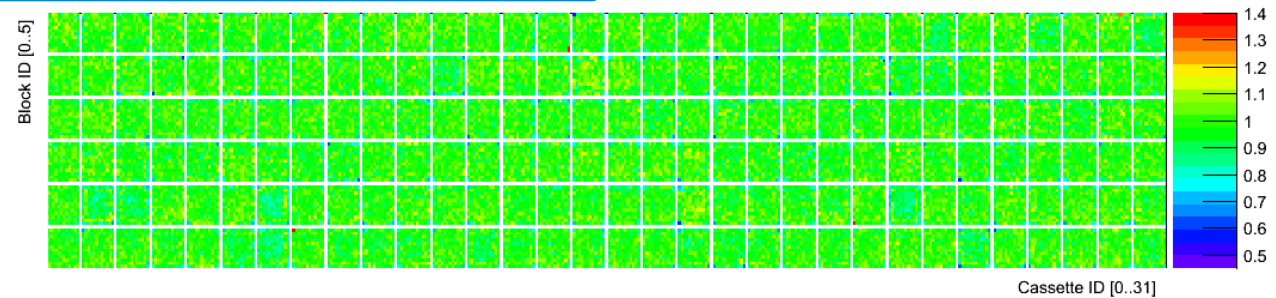
global correction value:



only block-based correction:

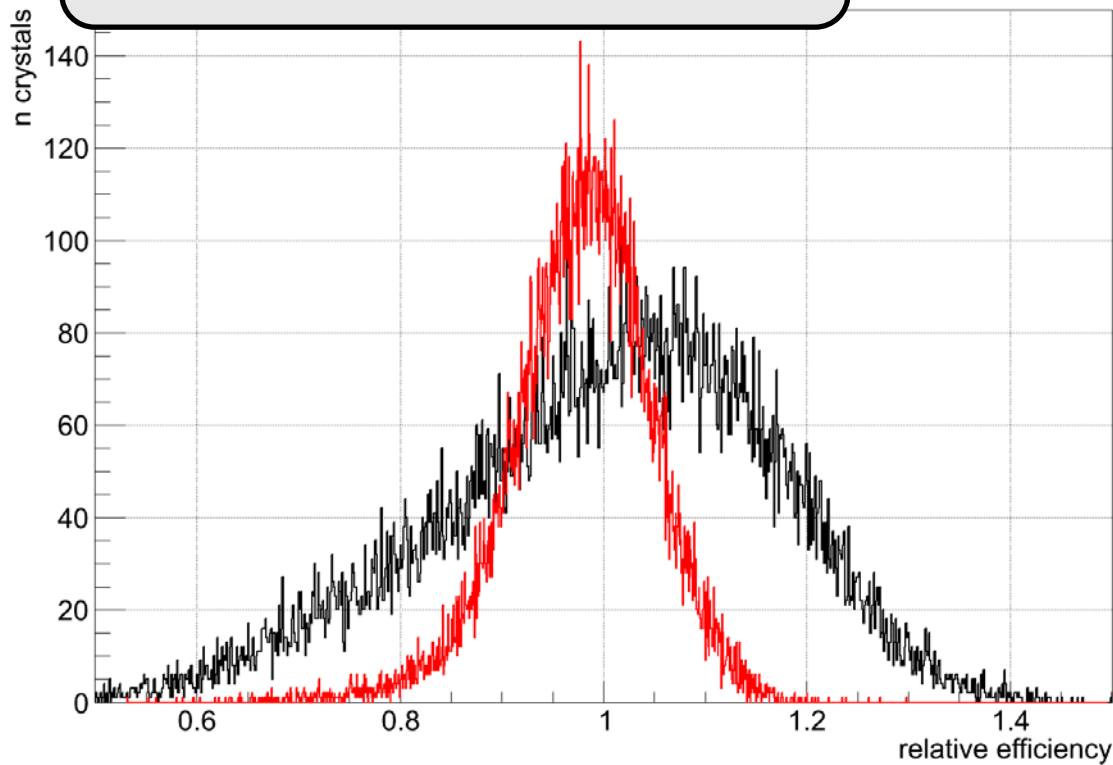


block-based and Pile-up correction:

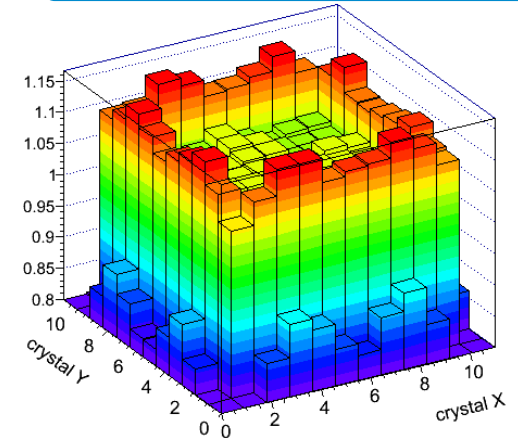


Dynamic Correction

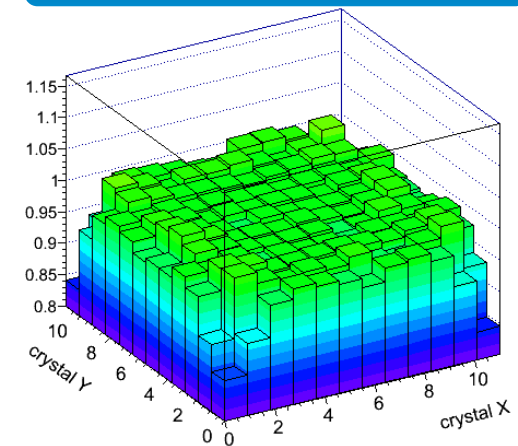
Global Correction + Norm Dynamic Correction



before correction:



after correction:



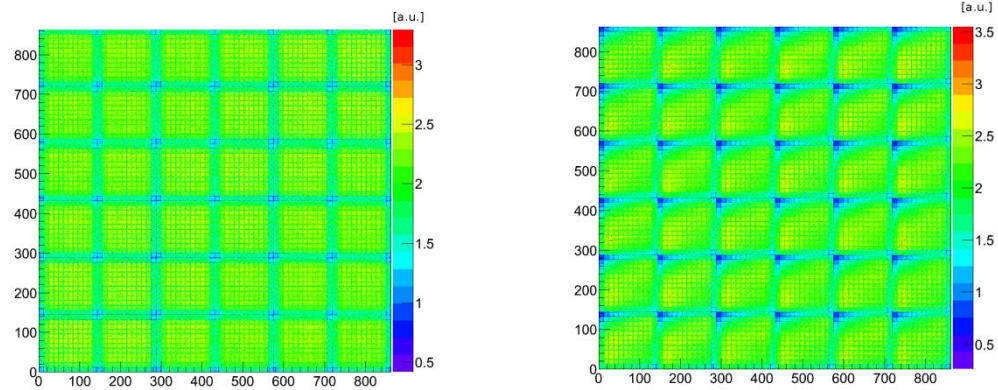
Weirich C., Scheins J., Gaens, M., Herzog H., Shah N.J. *Combined Deadtime and Pileup Correction for the MR-compatible BrainPET scanner*. Conference Record of the IEEE NSS/MIC Seoul, South Korea, 2013

Integration: Norm, Deadtime and Pile-up

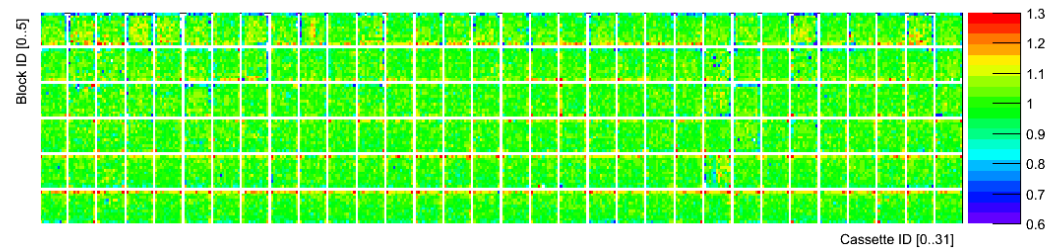
Correction Value c_{ij} :

$$c_{ij} = \frac{1}{g_{ij} \epsilon_{stat,i} \epsilon_{stat,j} \epsilon_{dyn,i} \epsilon_{dyn,j}}$$

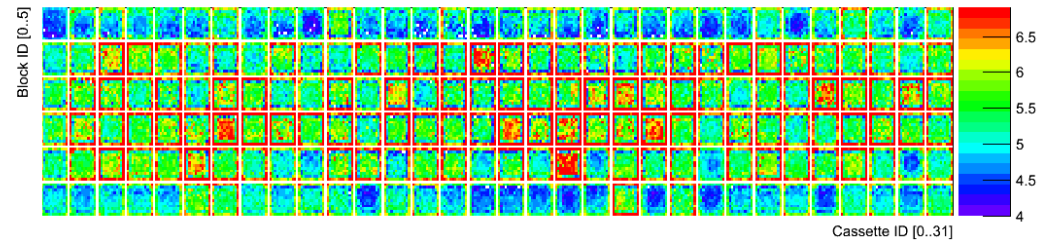
Geometric
Component g_{ij} :



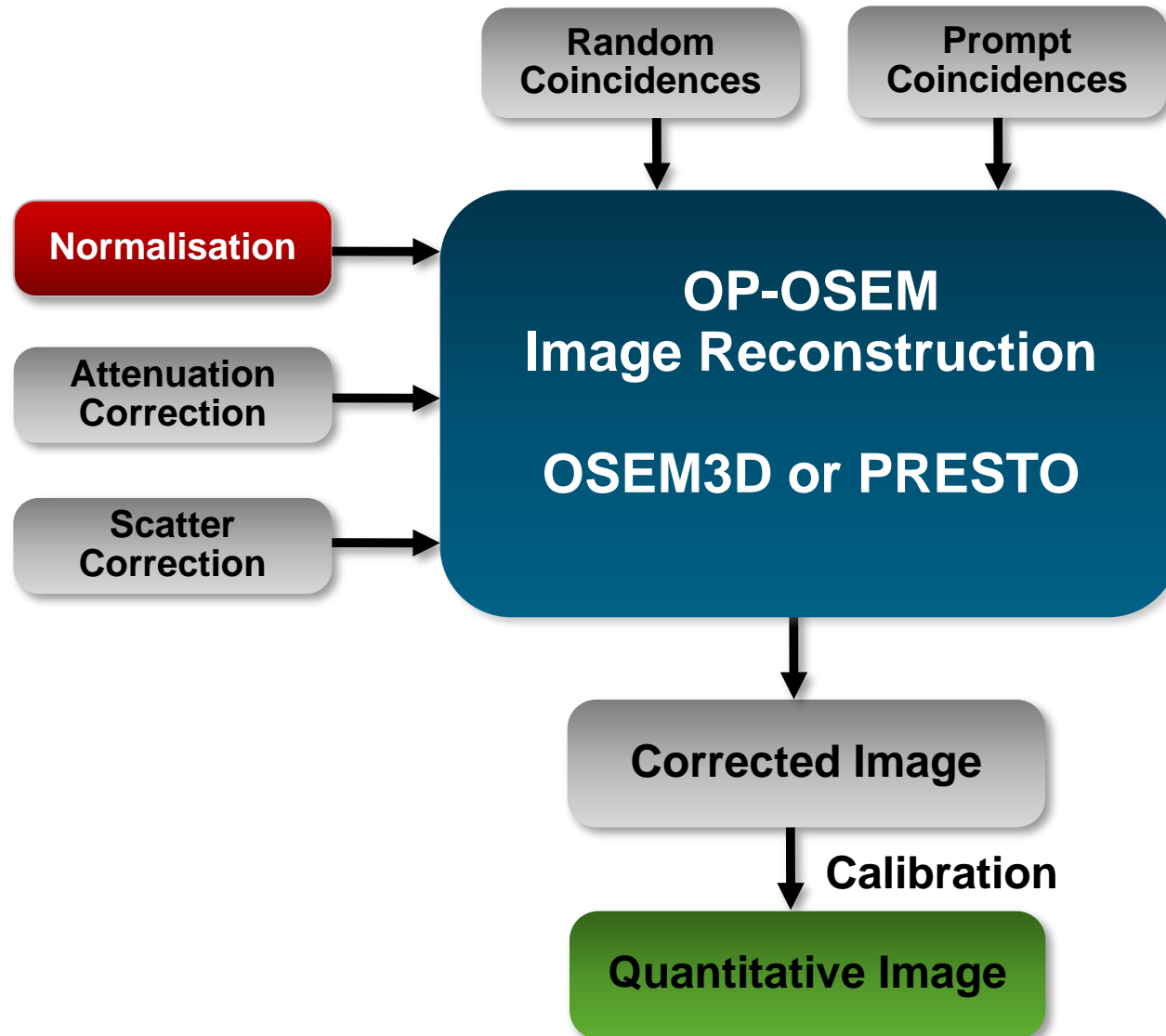
Static
Crystal Efficiency $\epsilon_{stat,j}$:



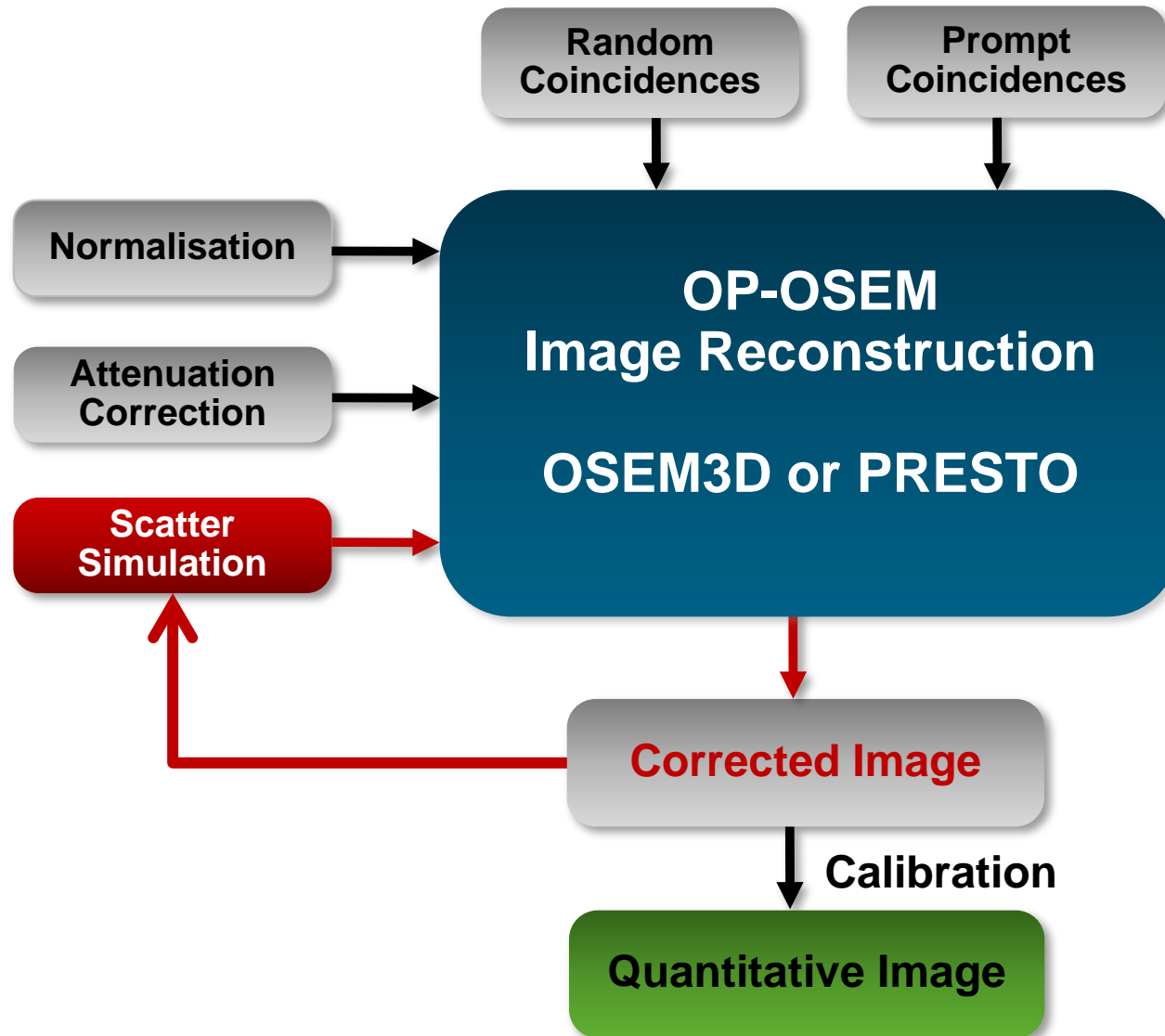
Dynamic
Crystal Efficiency $\epsilon_{dyn,i}$:



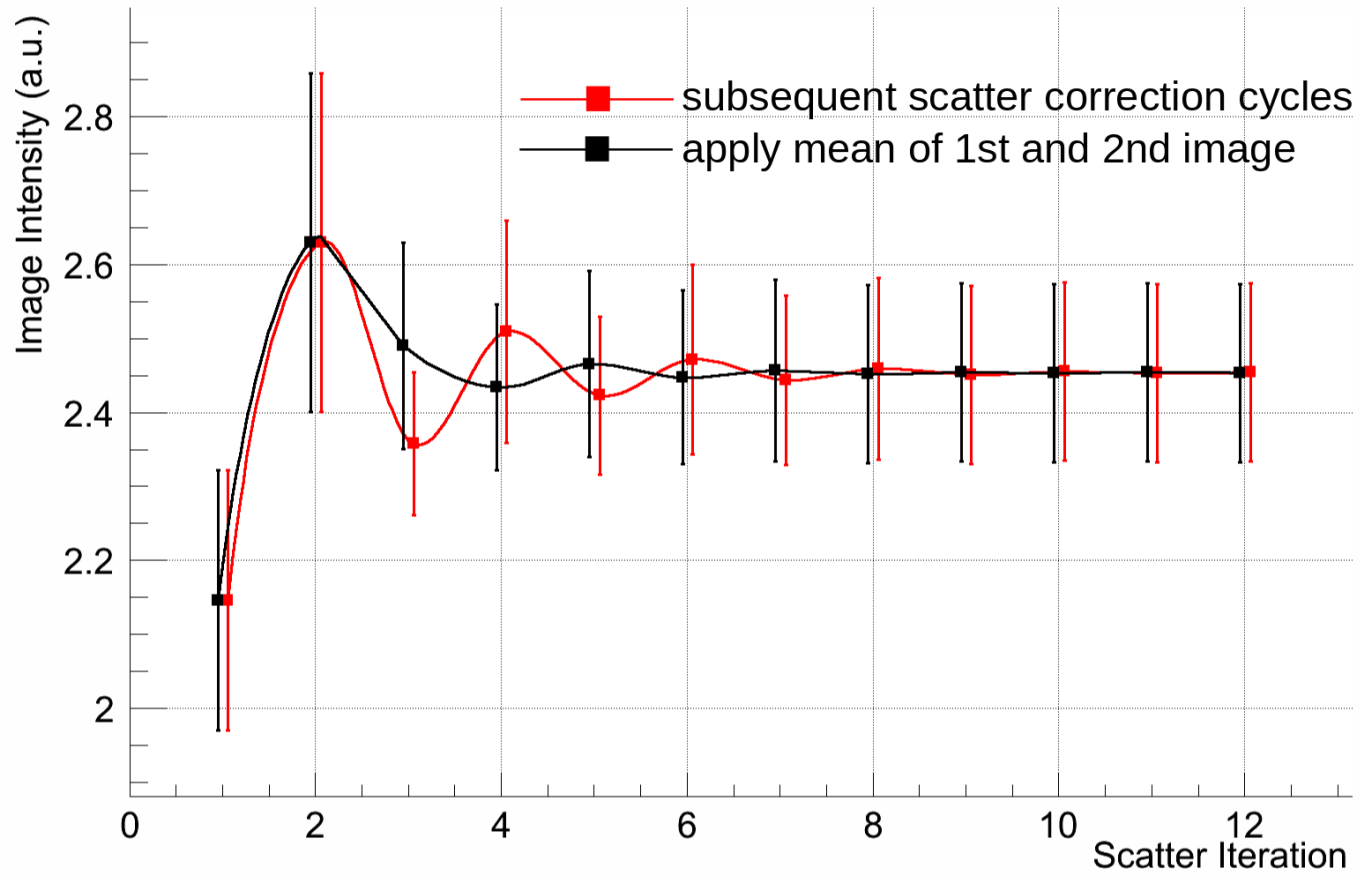
Reconstruction: Quantitative Imaging



Scatter Correction



Scatter Correction



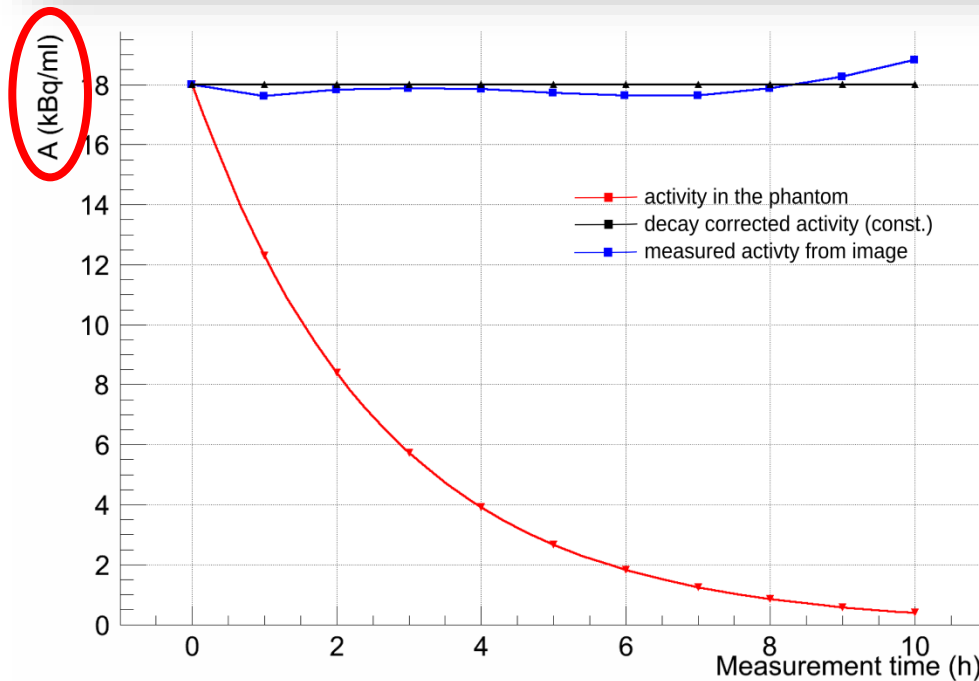
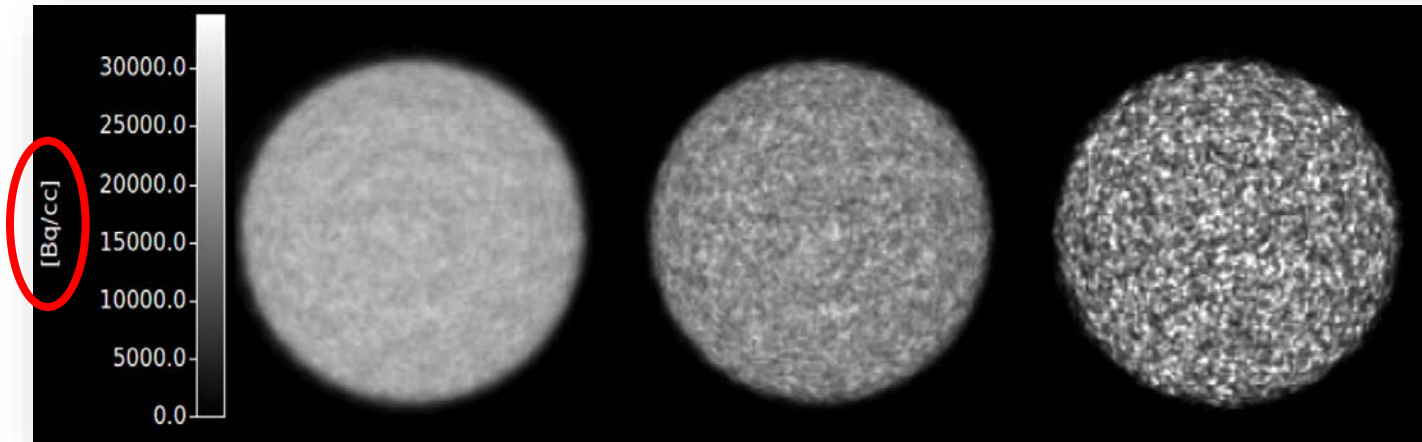
I. Hong

Validation in Phantom Studies



Weirich, C., Daun, A., Scheins, J., Tellmann, L., Herzog, H., Shah, N.J. *Long Term Quantitative Stability of the MR Compatible BrainPET Insert.* Conference Record of the IEEE NSS/MIC, 2011

Validation in Phantom Studies



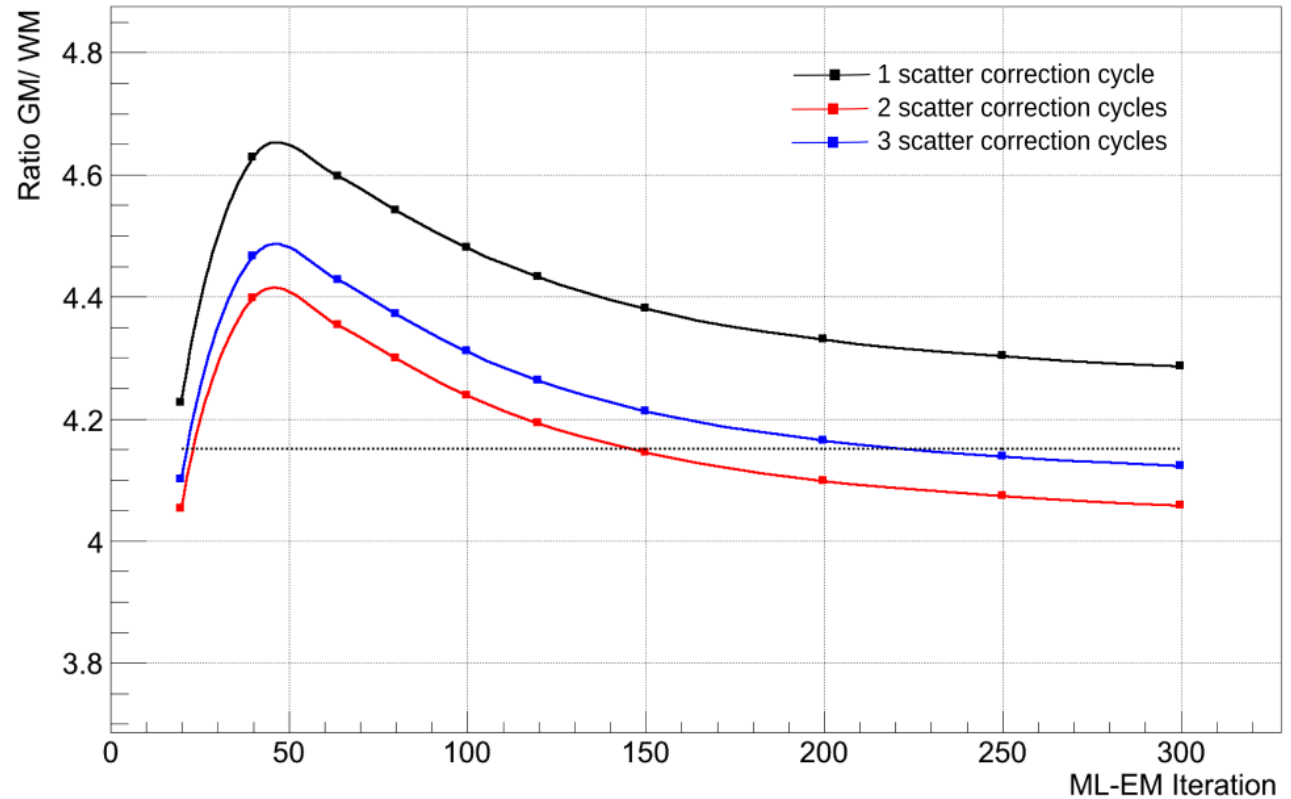
✓ Image homogeneity

✓ Absolute quantification

Scatter Correction

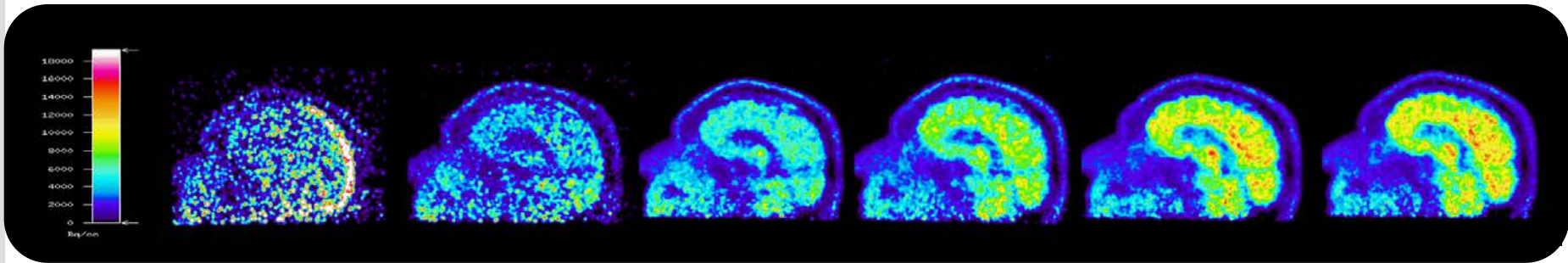
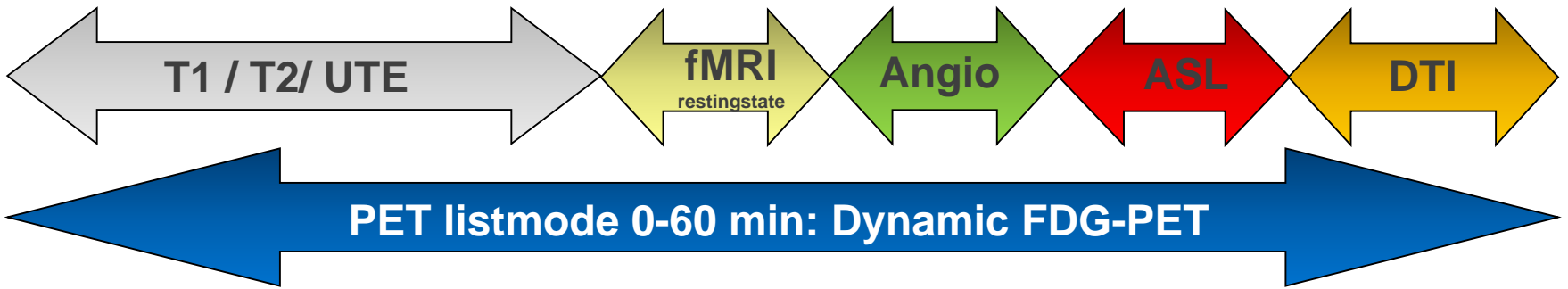
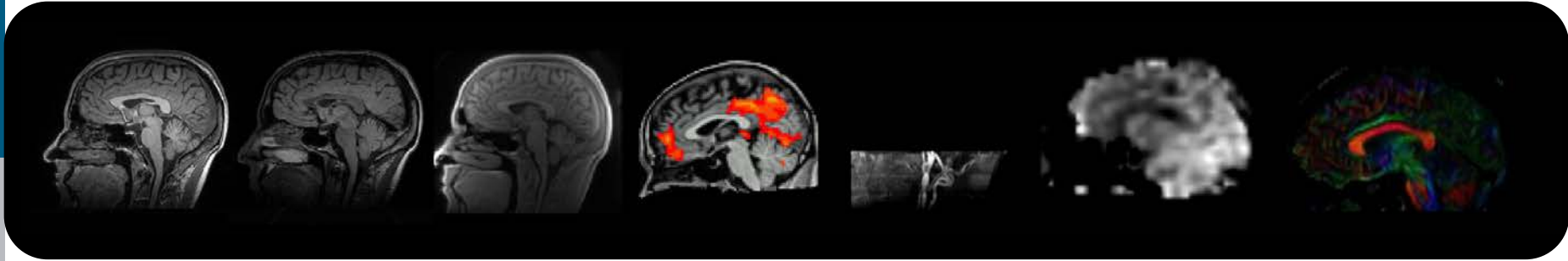


**GM/WM:
4.15 / 1**



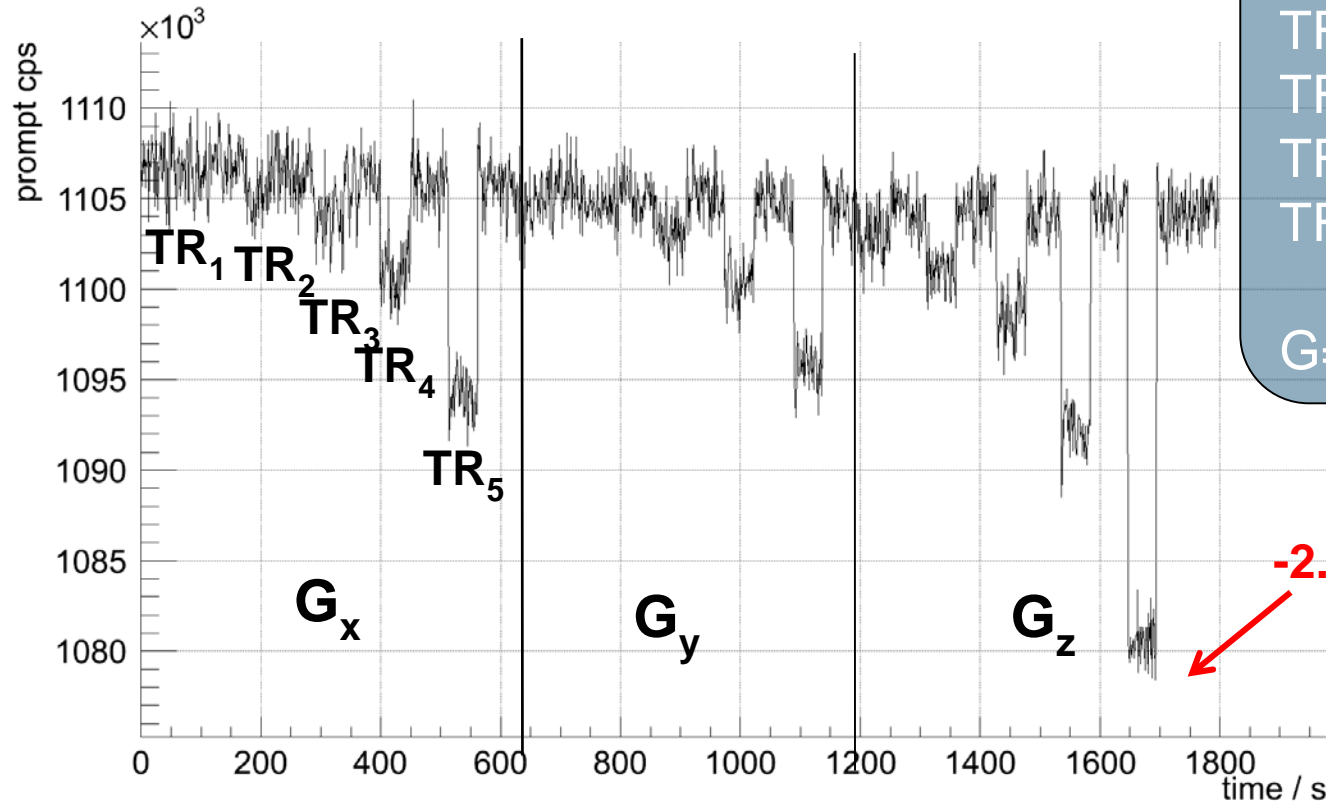
Hybrid MR-PET

dynamic FDG-PET with MRI



Influence of MRI on PET Countrate

Here: varying gradient repetition time (TR)



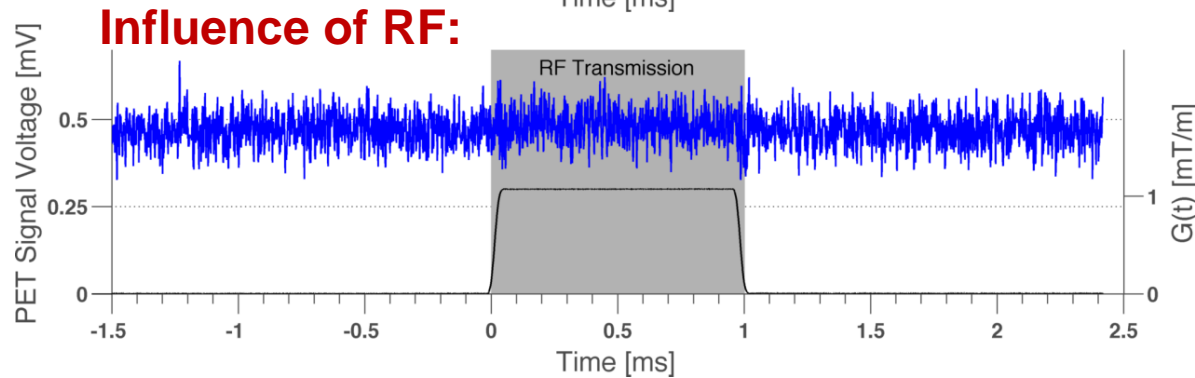
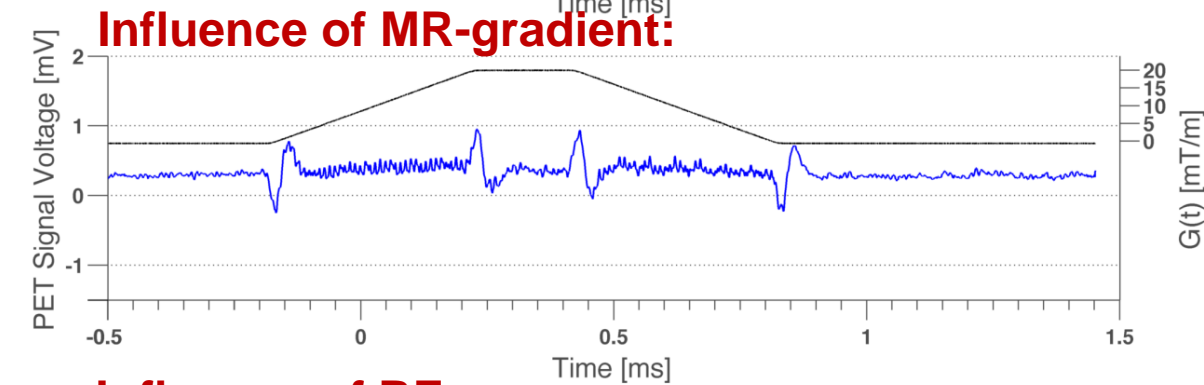
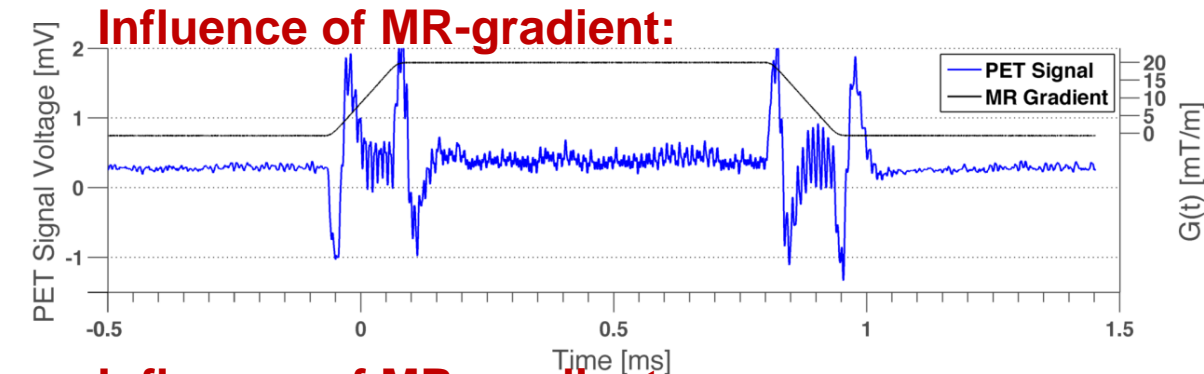
$TR_1 = 20.0 \text{ ms}$
 $TR_2 = 10.0 \text{ ms}$
 $TR_3 = 5.0 \text{ ms}$
 $TR_4 = 2.5 \text{ ms}$
 $TR_5 = 1.2 \text{ ms}$
 $G = 20 \text{ mT/m}$

-2.15 %

Weirich C., Brenner D., Tellmann L., Herzog H., Shah N.J. *Systematic Investigation and Correction of MR Influences on Simultaneous PET Measurements*. ISMRM, vol. 1, 2011

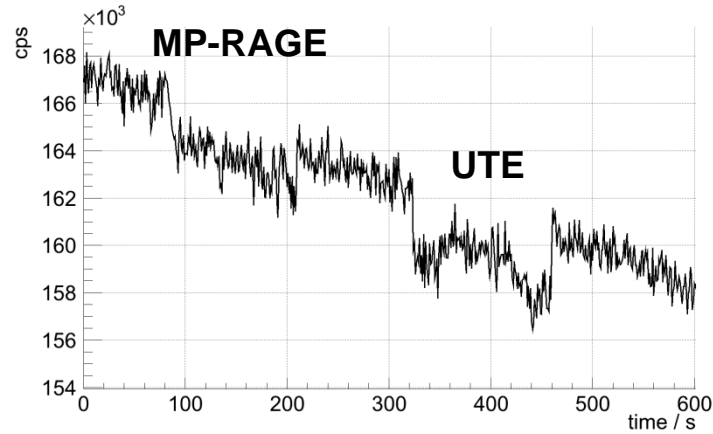
Brenner D., Weirich C., Scheins J., Besancon E., Tellmann, L., Herzog, H., Shah NJ., *New Insights into PET Count Rate Reduction during Simultaneous MR-PET Measurements*. ISMRM 2012

Analysis of PET Detector Signals

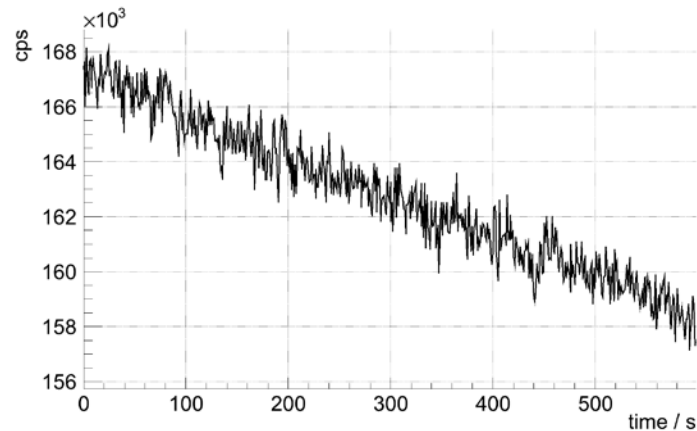


Correction of MR Influences

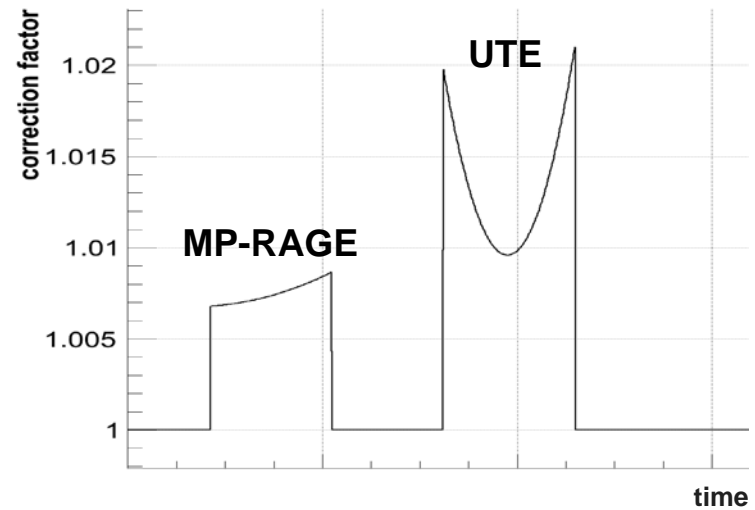
Uncorrected Countrate:



Corrected Countrate:

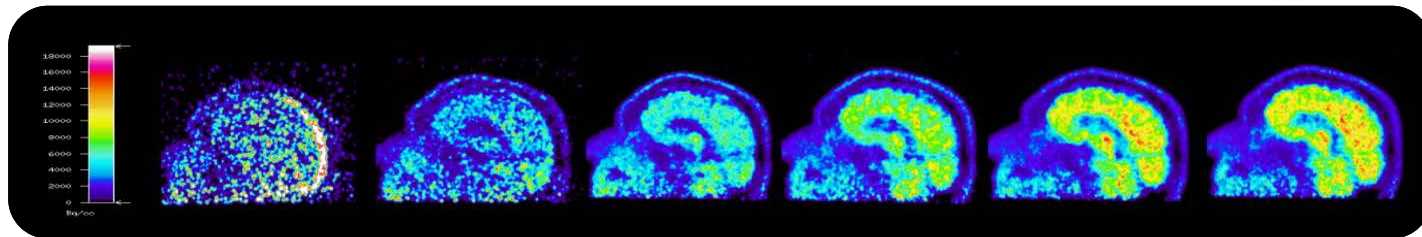
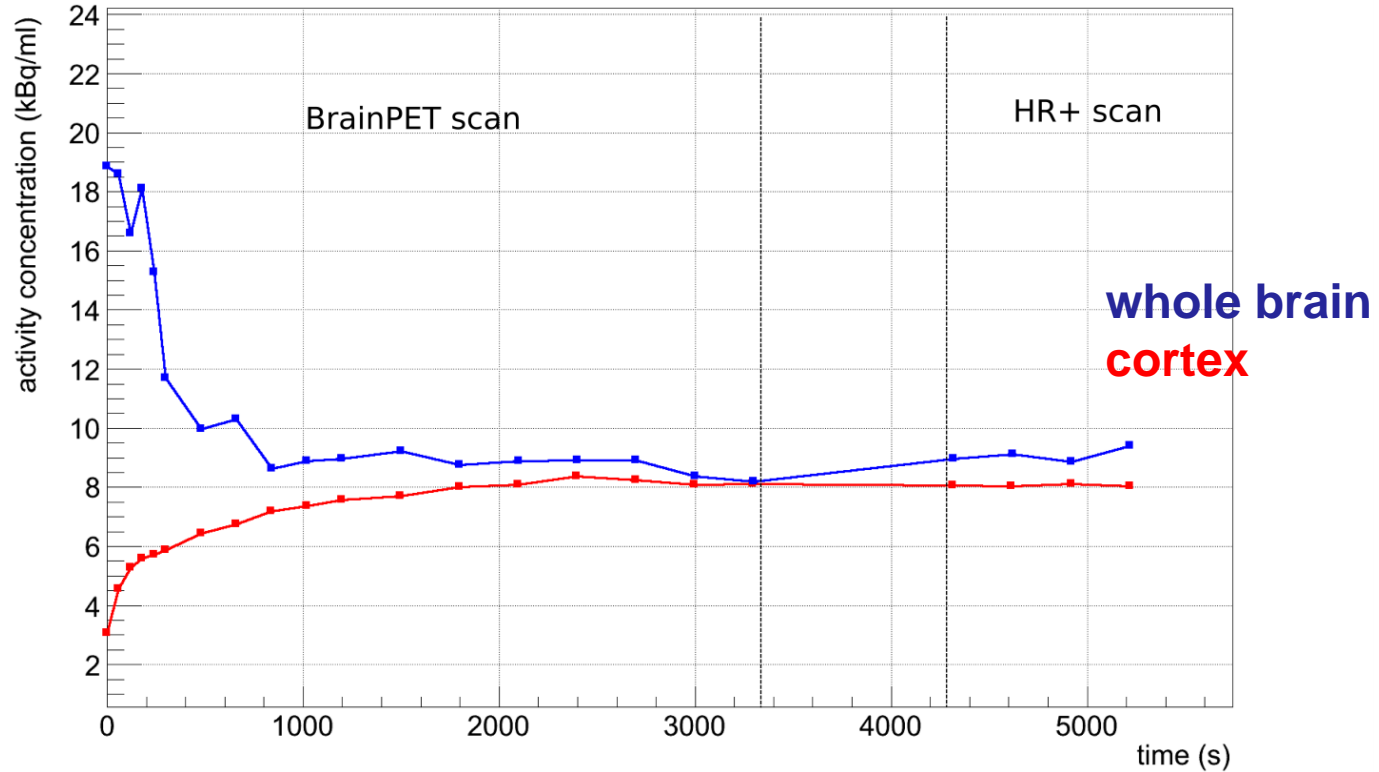


Correction Factor



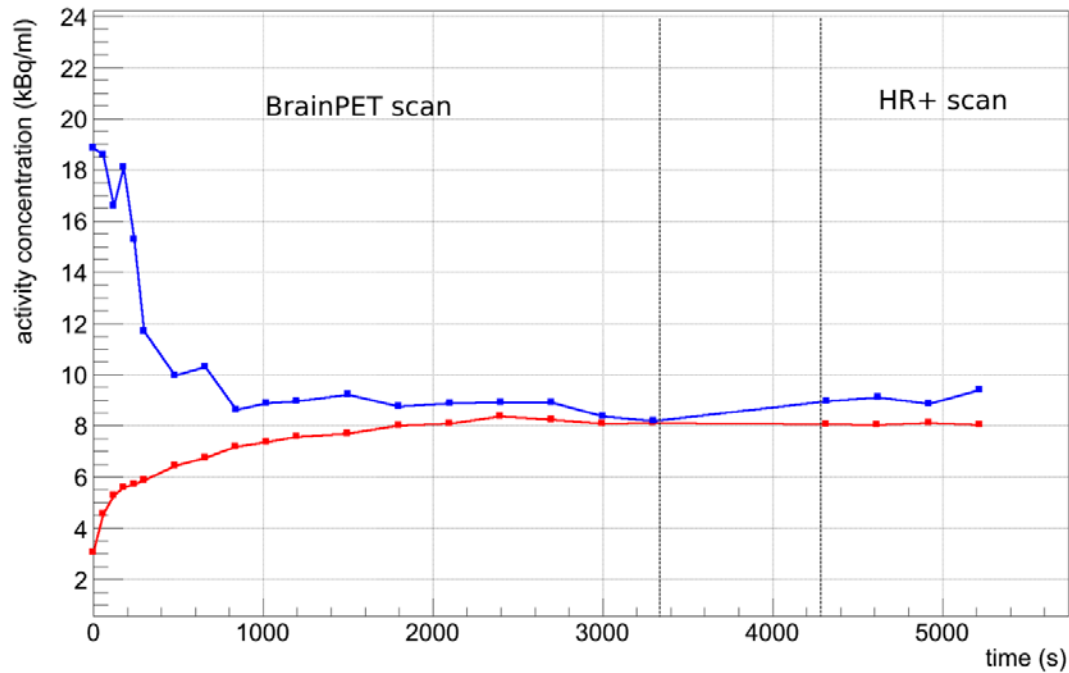
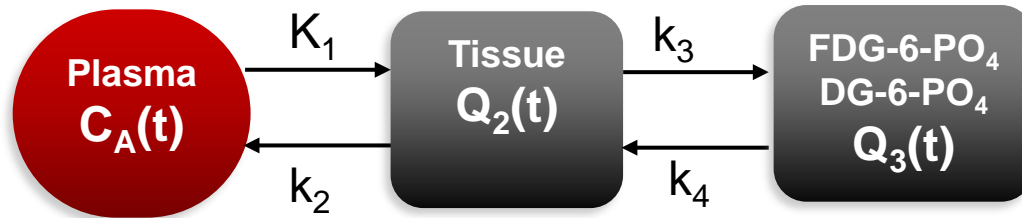
Weirich, C., Brenner, D., Scheins, J., Tellmann, L., Herzog, H., Shah, N.J. *Analysis and Correction of Count Rate Reduction during Simultaneous MR-PET Measurements with the BrainPET Scanner*, IEEE Transactions on Medical Imaging, (2012)

Cross Calibration of PET Scanners



Parametric Image

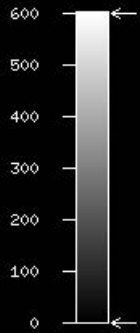
Quantitative Energy Consumption of the Human Brain



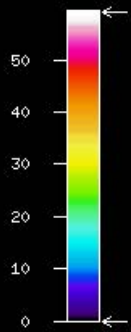
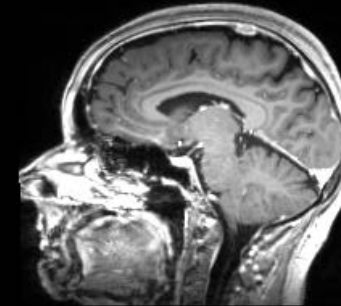
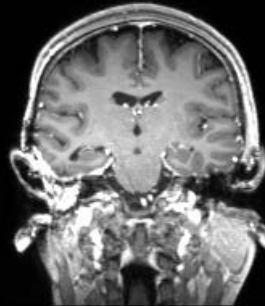
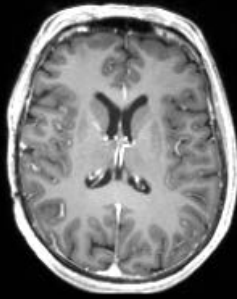
Patlak...

Parametric Image

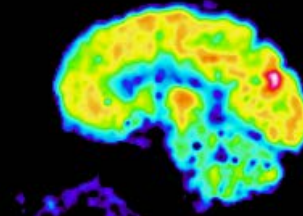
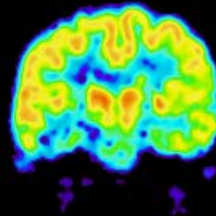
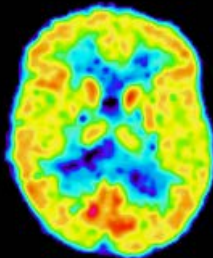
Quantitative Energy Consumption of the Human Brain



MP-RAGE

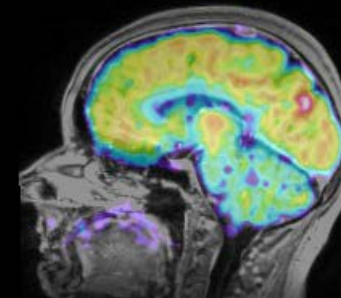
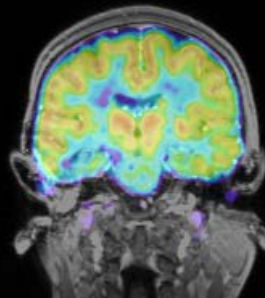
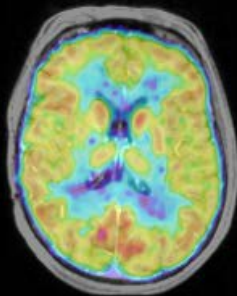


rCMRglu



$\mu\text{mol}/\text{min}/100\text{g}$

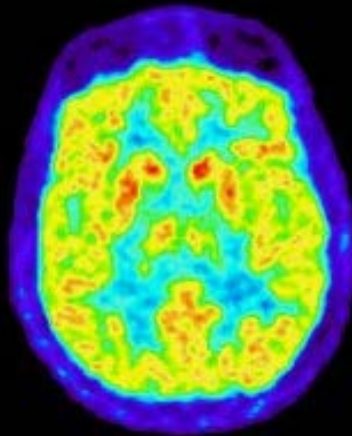
Fusion



Impact of the Quantification Workflow

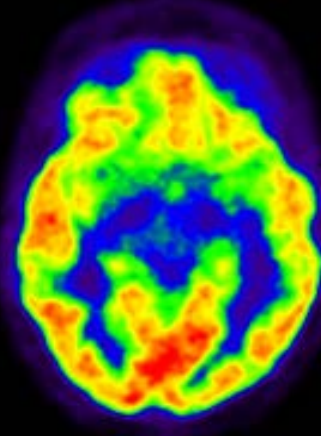
in vivo PET-Scans with different tracers:

FDG



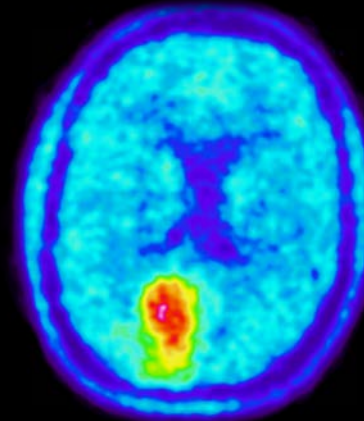
glucose uptake

Flumazenil



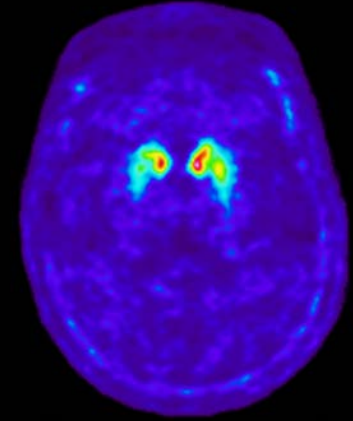
epilepsy

FET



tumour

FP-CIT



Parkinson's disease

Total number of *in vivo* scans:

Studies....

- ✓ Quantitative PET imaging from counts to parametric images
- ✓ Corrections were designed, implemented and optimised
- ✓ Integrated reconstruction workflow has been implemented
- ✓ Quantification error has been determined in phantom studies
- ✓ Human studies are carried out applying the 3T MR-BrainPET
- ✓ Long term stability of the system has been shown